

Constraining Higgs sector by low energy experiments

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Focus: CP conserving Higgs sector (2HDM)

• Direct searches

• Precision measurements or indirect searches

• High energy colliders: LEP, TEVATRON, HERA, ... LHC, LC, PLC

• Low energy experiments: $b \rightarrow s\gamma$, $g - 2$ for muon, leptonic τ decay

Standard Models

SM = 1HDM \Leftrightarrow one Higgs SU(2) doublet

One scalar (spin zero) doublet ϕ

Basic parameter v - vacuum expectation value of scalar field

one Higgs boson

one unknown parameter describing whole sector:

mass or selfcoupling

interaction with gauge bosons: $M_V \sim gv$ ($v \sim 246$ GeV),
coupling $\sim M_V$

Yukawa interaction with fermions: $mf \sim gf$

Direct searches: $M_{H^{SM}}$ larger than 114.4 GeV.

2HDM \Leftrightarrow two Higgs SU(2) doublets

Two scalar (spin zero) doublets ϕ_1 and ϕ_2 with vev v_1 and v_2

(with $v^2 = v_1^2 + v_2^2$, often we use $\tan\beta = v_2/v_1$)

Degrees of freedom: 8 fields - 3 (for long.components of W/Z) = 5 \Rightarrow

five physical Higgs bosons, spin=0, 3 - neutral, two charged !!

Other characteristics: quantum numbers - C, P, ...

Number of parameters? Depends on the form of potential, between 8 to 14 (minus 1 for v-constraint, minus 1 for rephasing)

CP or not CP conservation in Higgs sector

• CP conservation: Higgs sector: $h, H, A, H_{\pm}^{\pm}; \tan\beta, \alpha (h, H)$

h, H - CP-even, A - CP-odd

• CP violation: mixing between h_1, h_2, h_3 , more mixing angles

and CP parity of Higgs bosons - not defined

- Flavour Changing Neutral Current may be large (in nature FCNC small)
 - CP-violation may be large (in nature - small effects)
- The potential problems related to ϕ_1, ϕ_2 mixing:

Various models of Yukawa interaction with fermions:
Model II: where one scalar doublet couples to up-type quarks, other to down-type quarks and charged leptons

$$(g_h^M)^2 + (g_H^M)^2 + (g_A^M)^2 = (g_{SM}^M)^2$$

Interaction with gauge bosons and fermions - Higgs bosons share obligations, eg

more on 2HDM

2HDM models without and with CP violation

2HDM Potential: quartic and quadratic terms separated:

$$\begin{aligned}
 V = & \frac{1}{2}\lambda_1(\phi_1^\dagger\phi_1)^2 + \frac{1}{2}\lambda_2(\phi_2^\dagger\phi_2)^2 \\
 & + \lambda_3(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) + \lambda_4(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) \\
 & + \frac{1}{2}[\lambda_5(\phi_1^\dagger\phi_2)^2 + \text{h.c.}] \\
 & + \{[\lambda_6(\phi_1^\dagger\phi_1) + \lambda_7(\phi_2^\dagger\phi_2)](\phi_1^\dagger\phi_2) + \text{h.c.}\} \\
 & - \frac{1}{2}\{m_{11}^2(\phi_1^\dagger\phi_1) + [m_{12}^2(\phi_1^\dagger\phi_2) + \text{h.c.}] + m_{22}^2(\phi_2^\dagger\phi_2)\}
 \end{aligned}$$

soft violation of Z_2 symmetry

No (ϕ_1, ϕ_2) mixing if Z_2 symmetry satisfied (NO FCNC & NO CPV):
 $\phi_1 \rightarrow -\phi_1, \phi_2 \rightarrow \phi_2$ (or vice versa) $\Rightarrow \lambda_6 = \lambda_7 = m_{12}^2 = 0$

14 parameters: $\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5, \lambda_6, \lambda_7, m_{11}^2, m_{22}^2, \text{Re } m_{12}^2, \text{Im } m_{12}^2$
 Hard violation of Z_2 symmetry: quartic terms with λ_6, λ_7 (below = 0)

Lee, Diaz-Cruz, Mendez, Haber, Pomarol, Barroso, Santos, Hollik, Djouadi, Ilana, Branco, Gunion, Akroyd, Arhrib, ...

Minimum (vacuum) at (here $\lambda_6 = \lambda_7 = 0$):

$$\phi_1 = \begin{bmatrix} 0 \\ \frac{1}{\sqrt{2}}v_1 \end{bmatrix} \quad \phi_2 = \begin{bmatrix} \frac{1}{\sqrt{2}}v_2 \\ 0 \end{bmatrix} e^{i\xi}$$

Note, that

$$m_{12}^2 = [\mu^2/v^2 + i\delta]2v_1v_2e^{-i\xi},$$

$$\text{so } \mu = \text{Re}(m_{12}^2)v^2/2v_1v_2$$

$$\text{Im}(m_{12}^2e^{i\xi}) = \text{Im}(\lambda_5e^{2i\xi})v_1v_2$$

Naive conclusion: phase ξ violates CP ("complex" fermion masses)

However (eg. Branco), phase ξ can be removed by suitable redefinitions of phases of Higgs fields $\phi_{1,2}$, λ_5 and m_{12}^2 :

$$\phi_{1,2} \rightarrow \phi_{1,2} e^{-ip_{1,2}}, \lambda_5 \rightarrow \lambda_5 e^{2i(p_2-p_1)}, m_{12}^2 \rightarrow m_{12}^2 e^{i(p_2-p_1)}$$

and the same for fermion fields. So, the ξ disappears, we can put 0 (rephasing invariance). **CPV if $\text{Im} \lambda_5 \neq 0$.**

Unitarity constraints- upper limits of heavy Higgs bosons 600 GeV
 There are non-decoupling effects
 large $\lambda_{4,5}$ (small μ)

OR

large μ (leading to decoupling)
 The lightest Higgs h has all properties as the SM Higgs boson all
 heavier Higgs bosons decouple...

To get large masses we need:

$$M_{A^0}^2 = \mu^2 - \lambda_5 v^2, \quad M_{H^\pm}^2 = \mu^2 - \frac{1}{2}(\lambda_4 + \lambda_5)v^2$$

Masses of pseudoscalar and charged Higgs bosons:

Mass terms and decoupling (CP consv.)

λ_i in terms of masses, μ^2 etc.

Solving:

$$\lambda_1 v^2 = \frac{1}{\cos^2 \beta} \{ M_H^2 \cos^2 \alpha + M_h^2 \sin^2 \alpha \} - \mu^2 \tan^2 \beta$$

$$\lambda_2 v^2 = \frac{1}{\sin^2 \beta} \{ M_H^2 \sin^2 \alpha + M_h^2 \cos^2 \alpha \} - \mu^2 \cot^2 \beta$$

Remaining λ_i :

$$\lambda_5 = \frac{1}{v^2} [-M_{A_0}^2 + \mu^2]$$

$$\lambda_4 = \frac{1}{v^2} [M_{A_0}^2 - 2M_{H^\pm}^2 + \mu^2]$$

$$\lambda_3 = \frac{1}{v^2} \left[2M_{H^\pm}^2 + \frac{\sin 2\alpha}{\sin 2\beta} (M_H^2 - M_h^2) - \mu^2 \right]$$

$$g_{hhh} = -3v \left[-\cos\beta \sin^3\alpha \lambda_1 + \sin\beta \cos^3\alpha \lambda_2 - \frac{1}{2} \sin 2\alpha \cos(\beta + \alpha) \lambda_{345} \right] = \frac{-3g}{\sin 2\beta M_W^2} \left[(\cos\beta \cos^3\alpha - \sin\beta \sin^3\alpha) M_h^2 - \cos^2(\beta - \alpha) \cos(\beta + \alpha) m_{12}^2 \right],$$

Note, if selfcouplings are expressed in terms of masses, also m enters!

- Higgs quartic couplings
- Higgs trilinear couplings
- Higgs masses (quadratic couplings)

Physical content of potential

CP conservation: Higgs masses and couplings

$$\chi_{\phi}^i = \frac{g_{SM}^i}{g_{\phi}^i}, \phi = h, H, A$$

with $i = V, u, d$

couplings":

It is useful to express all couplings in terms of the relative "basic

e.g. Model II:

- couplings to fermions (Yukawa)

$$\text{for eg. } Z: g_h^2 + g_{H/2}^2 = g_{H/2}^{SM}$$

- couplings to gauge bosons: hWW, HWW , while $AWW = AZZ = 0$

Independent of potential are:

Basic couplings to gauge bosons $V = W/Z$ and fermions u, d -types

α – parameterizes mixing among the two neutral CP-even Higgs fields [eq. (– π , 0)]

$\tan \beta$ – the ratio of the vacuum expectation values of the two basic Higgs doublets [(0, $\pi/2$)]

$$\begin{aligned} \chi_H^p &= \cos(\beta - \alpha) + \tan \beta \sin(\beta - \alpha) \\ \chi_H^n &= \cos(\beta - \alpha) - \cot \beta \sin(\beta - \alpha) \\ \chi_H^A &= \cos(\beta - \alpha) \\ \chi_y^p &= \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) \\ \chi_y^n &= \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha) \\ \chi_y^A &= \sin(\beta - \alpha) \end{aligned}$$

DIRECT COUPLINGS in 2HDM

Pattern relation

We found that for both h and H :

$$(X_u - X_V)(X_V - X_D) + X_V^2 = 1$$

or

$$(X_u + X_D)X_V = 1 + X_u X_D.$$

Also,

$$\tan^2 \beta = \frac{X_V - X_D}{X_V - X_U} = \frac{1 - X_D^2}{1 - X_U^2}$$

The pattern relation was obtained here in the tree approximation. Radiative corrections will modify it at the level of *few percents*.

“Finite” for “large” $M_{H^\pm}^2$ (non-decoupling for small μ)
 important for $\gamma\gamma\phi$ loop-coupling.

$$\chi_{\phi}^{H^\pm} \equiv -\frac{2g_{\phi H^+ H^-} M_{H^\pm}^2}{M_\phi^2} \left(1 - \frac{M_{H^\pm}^2}{M_\phi^2} \right) + \chi_\phi^V + \frac{2M_{H^\pm}^2}{M_\phi^2 - \mu^2} (\chi_\phi^u + \chi_\phi^p)$$

One can introduce a relative coupling for $\phi H^+ H^-$, $\phi = h, H$:

Selfcouplings in terms of observables

Existing constraints for 2HDM (II)

CP conserv. 2HDM(II) with soft violation of Z_2 symmetry (μ^2 term):
 \Rightarrow five Higgs bosons: h, H, A, H^\pm
 \Rightarrow 7 parameters: $M_h, M_H, M_A, M_{H^\pm}, \alpha, \beta,$ and μ^2

MODEL II (as in MSSM)

Couplings (relative to SM):

	h	A	
to W/Z:	$\chi_V = \sin(\beta - \alpha)$	0	
to down quarks/leptons:	$\chi_d = \chi_V - \sqrt{1 - \chi_V^2} \tan \beta$	$-i\gamma_5 \tan \beta$	
to up quarks:	$\chi_u = \chi_V + \sqrt{1 - \chi_V^2} / \tan \beta$	$-i\gamma_5 / \tan \beta$	

For couplings like for h with:

$$\sin(\beta - \alpha) \leftrightarrow \cos(\beta - \alpha) \text{ and } \tan \beta \leftrightarrow -\tan \beta.$$

Pattern relation holds: $(\chi_u + \chi_d)\chi_V = 1 + \chi_u\chi_d$

I. Ginzburg, MK, P. Osland, hep-ph/0101208

DATA

LEP • direct: (h) Bjorken process $Z \rightarrow Zh,$

(hA) pair prod. $e^+e^- \rightarrow hA,$

(h/A) Yukawa pro. $e^+e^- \rightarrow bbh/A$

(H^\pm) $e^+e^- \rightarrow H^+H^-$

via loop: $(h/A, \text{ and } H^\pm) Z \rightarrow h/A\gamma$

Others exp. • via loop: (h/A) Wilczek process $\tau \rightarrow h/A\gamma$

loop: $(H^\pm) b \rightarrow s\gamma M^{H^\pm} > 500\text{GeV}$ (Misiak, Gambino 2001)

leptonic tau decay (MK, Temes - hep-ph/0410248)

g-2 data (Hocker SM - hep-ph/0410081)

Global fit • (all Higgses)

Chanowski at al., EPJC 11,661:PL B496,195

Cheung and Kong - hep-ph/0302111

b to s gamma

Strong constraints on new physics from $B \rightarrow X_s \gamma$ crucially depend on theoretical uncertainties in the Standard Model prediction for this decay

$$\text{BR}[B \rightarrow X_s \gamma] = \left[3.21 \pm 0.43_{\text{stat}} \pm 0.27_{\text{sys}} \begin{pmatrix} +0.18 \\ -0.10 \end{pmatrix}_{\text{theory}} \right] \times 10^{-4} \quad (\text{CLEO}),$$

$$\text{BR}[B \rightarrow X_s \gamma] = \left[3.36 \pm 0.53_{\text{stat}} \pm 0.42_{\text{sys}} \pm 0.54_{\text{theory}} \right] \times 10^{-4} \quad (\text{BELLE}),$$

$$\text{BR}[b \rightarrow s \gamma] = (3.11 \pm 0.80_{\text{stat}} \pm 0.72_{\text{sys}}) \times 10^{-4} \quad (\text{ALEPH}).$$

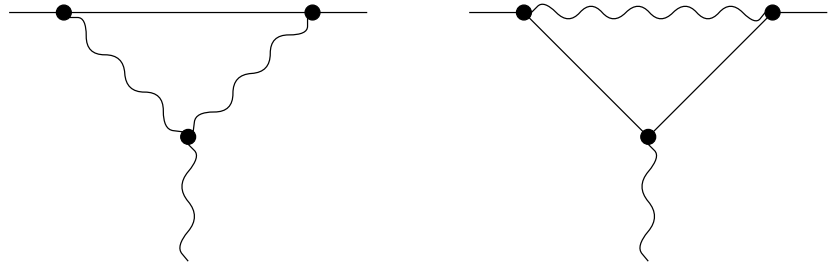
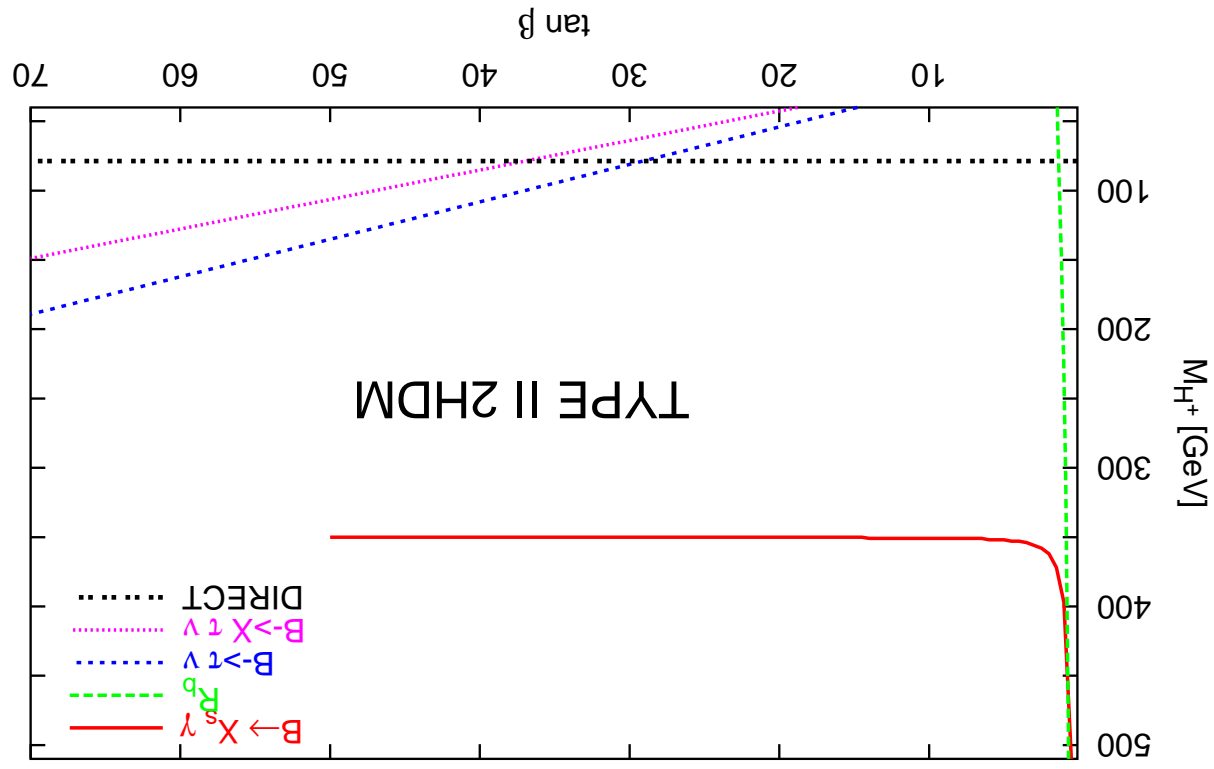
The weighted average for $\text{BR}_\gamma \equiv \text{BR}[B \rightarrow X_s \gamma]$

$$\text{BR}_{\text{exp}}^\gamma = (3.23 \pm 0.42) \times 10^{-4}$$

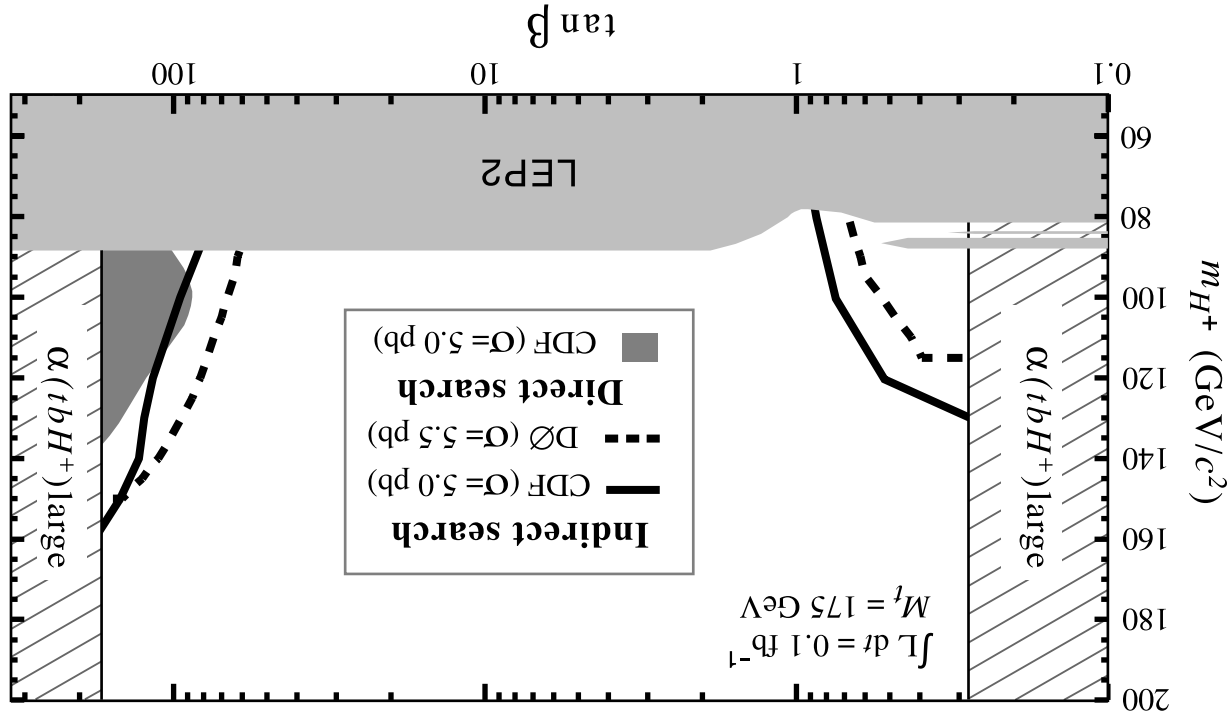
with an error of around 13%. Improved experimental results coming-
reduce the theor. uncertainty significantly below 10% needed

Sources of uncertainties in the theoretical prediction:
parametric, non-perturbative and perturbative

Limits: at 95 % CL - MH+ above 500 GeV



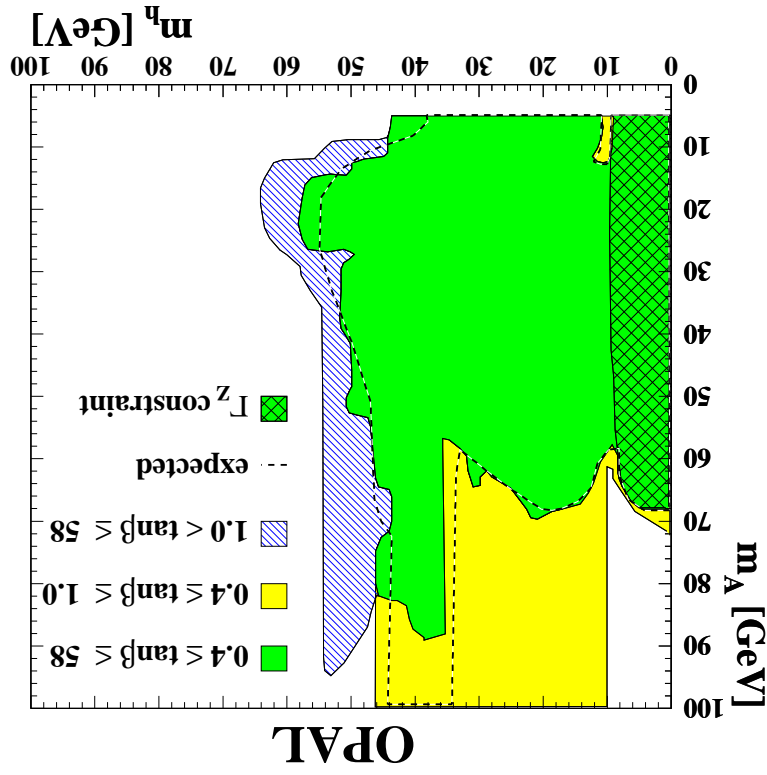
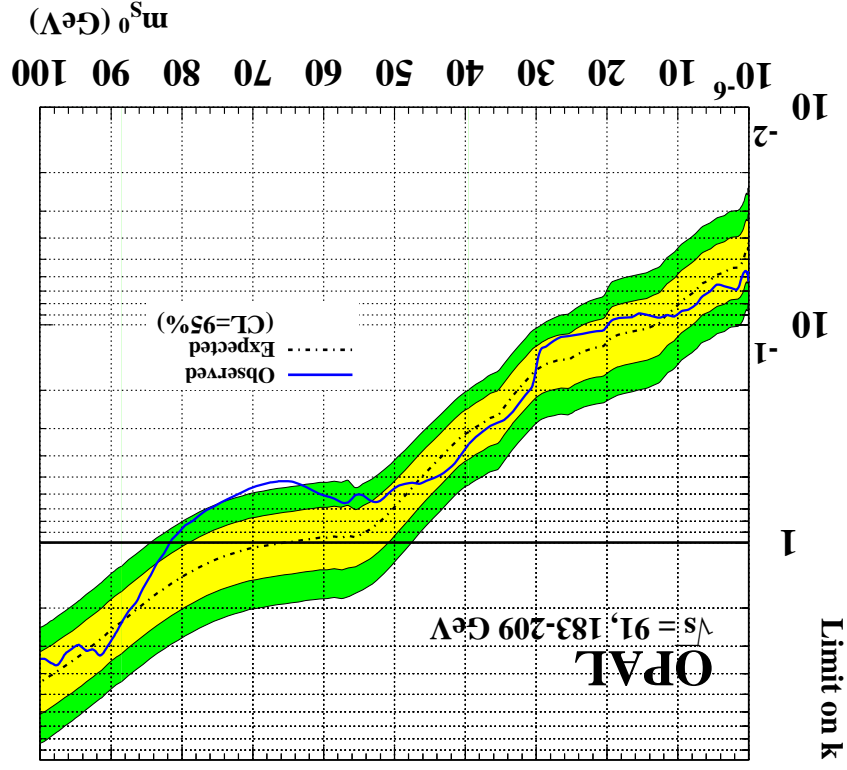
Limits for charged Higgs boson



Tevatron, LEP data

h, A - coupling to gauge boson, and mass plot

Light h OR light A in agreement with current data
 hZZ: $\sin(\beta - \alpha)$ and hAZ: $\cos(\beta - \alpha)$
 $k = \sin^2(\beta - \alpha)$



hep-ph/0103223v3
hep-ph/0112112 Snowmass proc
Acta Phys. Pol. B 33 (2002) 2621
(hep-ph/020807)

the lightest Higgs boson in 2HDM(II)

and

Precision results for $(g-2)$ for muon

DATA and SM prediction for $g - 2$ for muon $a_\mu \equiv \frac{g-2}{2}$

A significant revision due to change in sign of the light by light hadronic contribution to a_μ light-by-light (lbl):
 previous av: $-8.5(2.5)10^{-10}$
 recent:

Knecht, Nyfeler $+8.3(1.2)$
 Hayakawa, Kinoshita $+8.9(1.5)$
 Bijnens, et al $+8.3(3.2)$
 Blokland, et al. $+5.6$

$$a_{exp}^\mu = 11659203(8) \cdot 10^{-10}$$

$$a_{SM}^\mu = a_{QED}^\mu + a_{EW}^\mu + a_{had}^\mu$$

101804 [Erratum-ibid. 89 (2002)
 E821, Phys. Rev. Lett. 89 (2002)
 129903 [arXiv:hep-ex/0208001]

$$had=vac.pol.1+vac.pol.2+lbl$$

$$\Delta a_\mu = a_{exp}^\mu - a_{SM}^\mu$$

SM contributions

Hadronic contribution		[in 10^{-11}]
ho (Krause)	-100	(6)
hbl (Nyffeler)	80	(40)
vp1 (Jegou2)	6889	(58)
had [FJ02]	6869	(71)

SM and data

SM contribution	[in 10^{-11}]
QED	116 584 705.7 (2.9)
had[FJ02]	6 869.0 (70.7)
EW	152.0 (4.0)
tot	116 591 726.7 (70.9)
$\Delta a_\mu(\sigma)$	303.3 (106.9)
lim(95%)	93.8 $\leq \delta a_\mu \leq$ 512.8

[HMNT (ex)]: $\Delta a_\mu(\sigma) = 297.0 (107.2)$ $87.2 \leq \delta a_\mu \leq 507.4$,
 [HMNT(in)]: $\Delta a_\mu(\sigma) = 357.2 (106.4)$ $148.7 \leq \delta a_\mu \leq 565.7$
 [DEHZ (e+e-)]: $\Delta a_\mu(\sigma) = 339.0 (112)$

Jegerlehner, Talk at Marseille, March 2002
 Hagiwara et al (hep-ph/0209187v2)
 Davier et al (hep-ph/0208177)

19.09.03
 BNL 10.01.2004
 Hocker (10.2004)
 $\Delta a_\mu(\sigma) = 234 (119)$ $0.076 \leq \delta a_\mu \leq 467$
 $\Delta a_\mu(\sigma) = 301 (104.1)$ $96.96 \leq \delta a_\mu \leq 505$
 $\Delta a_\mu(\sigma) = 252(92)$

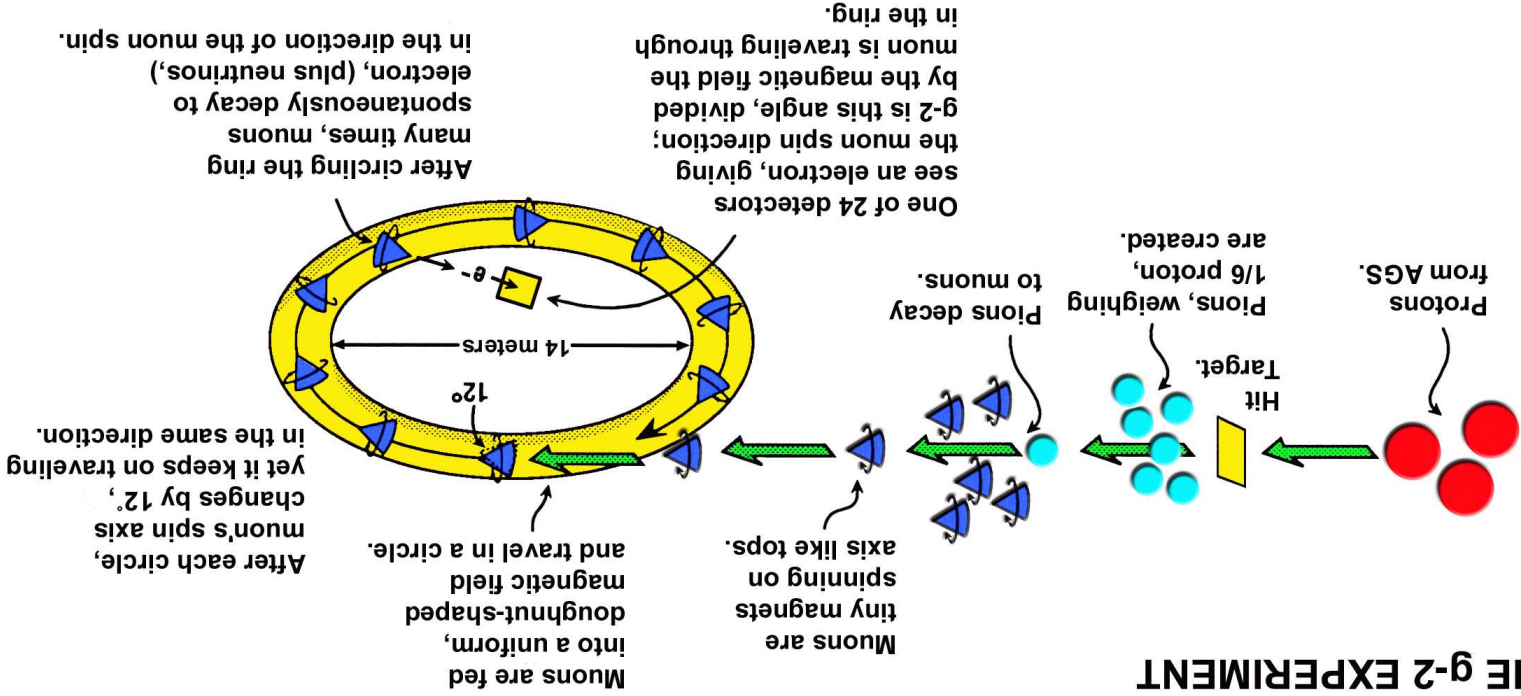
δa_μ region can be used to constrain parameters of new models

Hot News: BNL hep-ex/0401008

Measurement of the Negative Muon Anomalous Magnetic Moment to 0.7 ppm muon spin precession in a magnetic storage ring with electrostatic focusing. The same experimental technique as in $a^{\mu+}$, and a similar precision of 0.7 ppm was achieved.

Overview of the experiment

LIFE OF A MUON: THE g-2 EXPERIMENT



The anomalous magnetic moments of the muon and the electron \Rightarrow an important role in the development of the SM. Compared to the electron, the muon anomaly has a relative sensitivity to heavier mass scales proportional to $(m_\mu/m_e)^2$.

The negative muon anomalous magnetic moment from data collected in early 2001.

$$a_{\mu^-} = 11\,659\,214(8)(3) \times 10^{-10} (0.7 \text{ ppm})$$

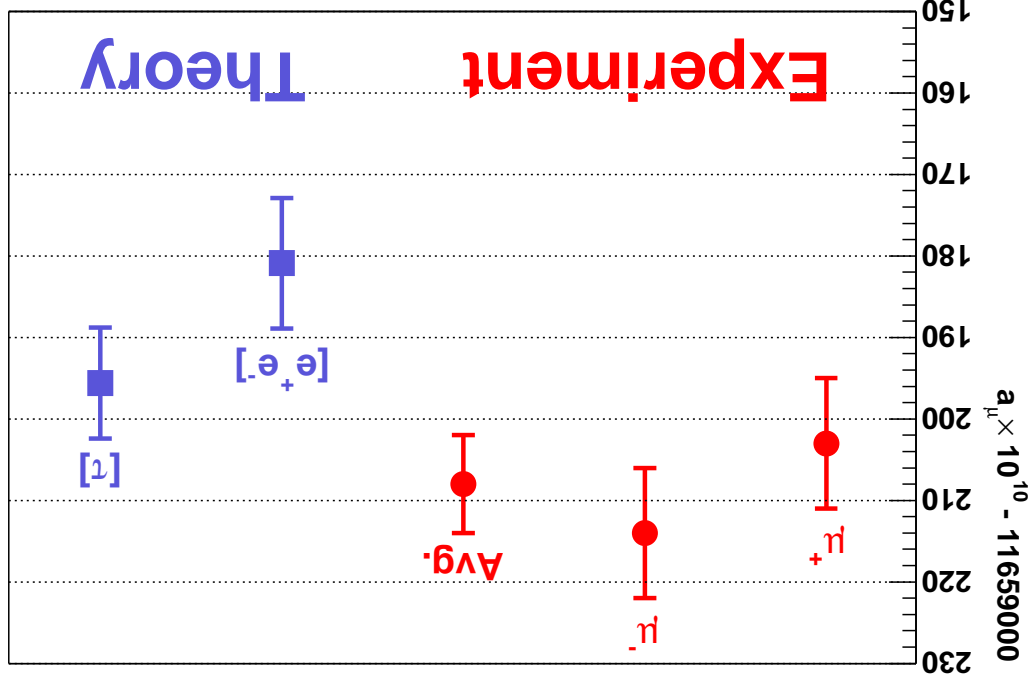
(statistical + systematic)

consistent with previous measurements of the anomaly for the positive and negative muon $a_\mu(\text{exp}) = 11\,659\,203(8) \times 10^{-10}$.

The average for the muon anomaly is

$$a_\mu(\text{exp}) = 11\,659\,208(6) \times 10^{-10} (0.5 \text{ ppm})$$

(correlated systematic errors between the data sets)



Two data sets do not give consistent results for the pion form factor. e^+e^- annihilation gives $a_\mu(\text{SM}) = 11\,659\,181(8) \times 10^{-10}$ (0.6 ppm). τ decay gives result 15×10^{-10} larger.

So, The difference of a_μ^{exp} and the SM the e^+e^- or τ data for the calculation of the hadronic vacuum polarization is 2.7σ and 1.4σ

Hadronic contr. - this summer summary

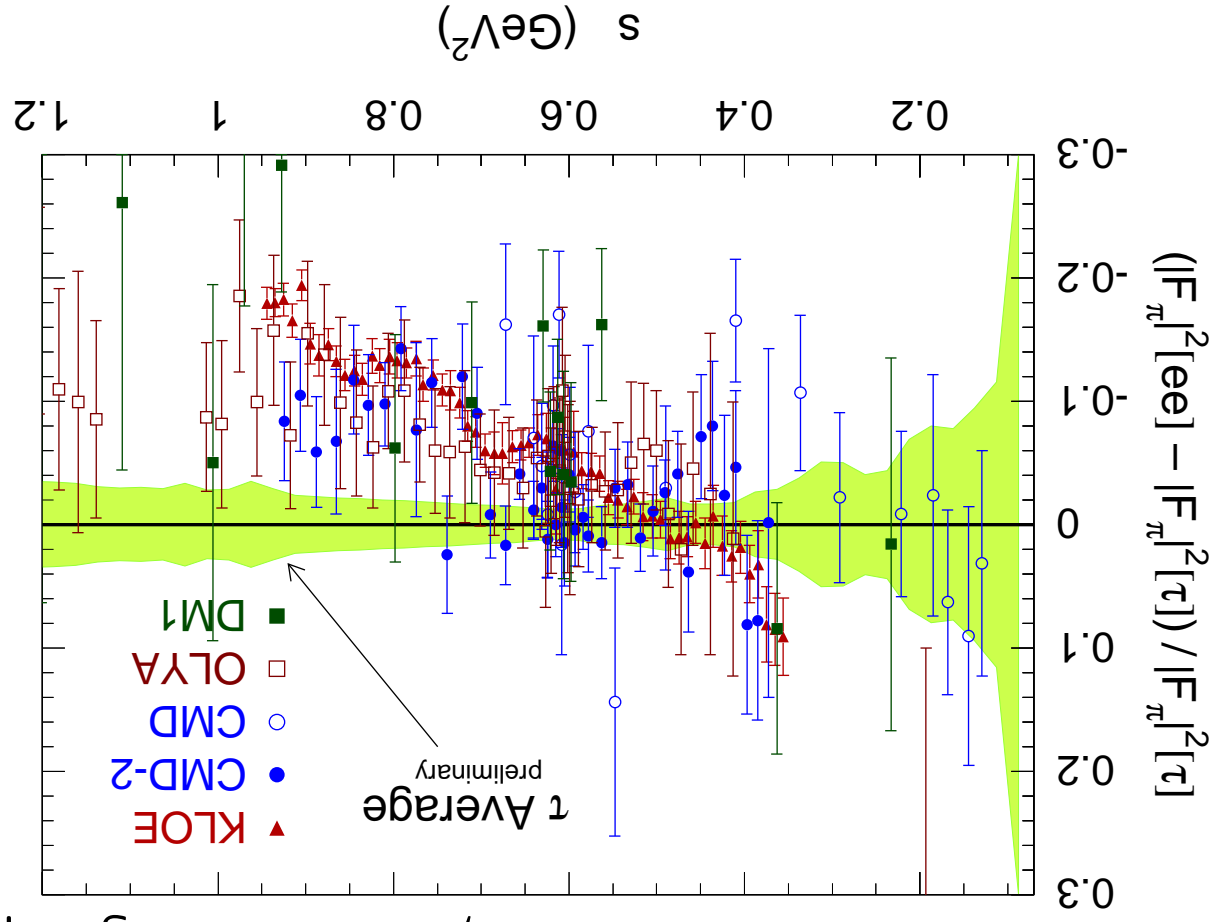
Hadronic contribution to the muon magnetic anomaly - a new estimate using precise results on the $\pi^+ \pi^-$ spectral function from the KLOE Confirmation of the previous $e^+ e^-$ annihilation data in this channel, Disagreement with the isospin-breaking-corrected spectral function from $\tau \rightarrow \pi \pi^0 \nu$ decays.

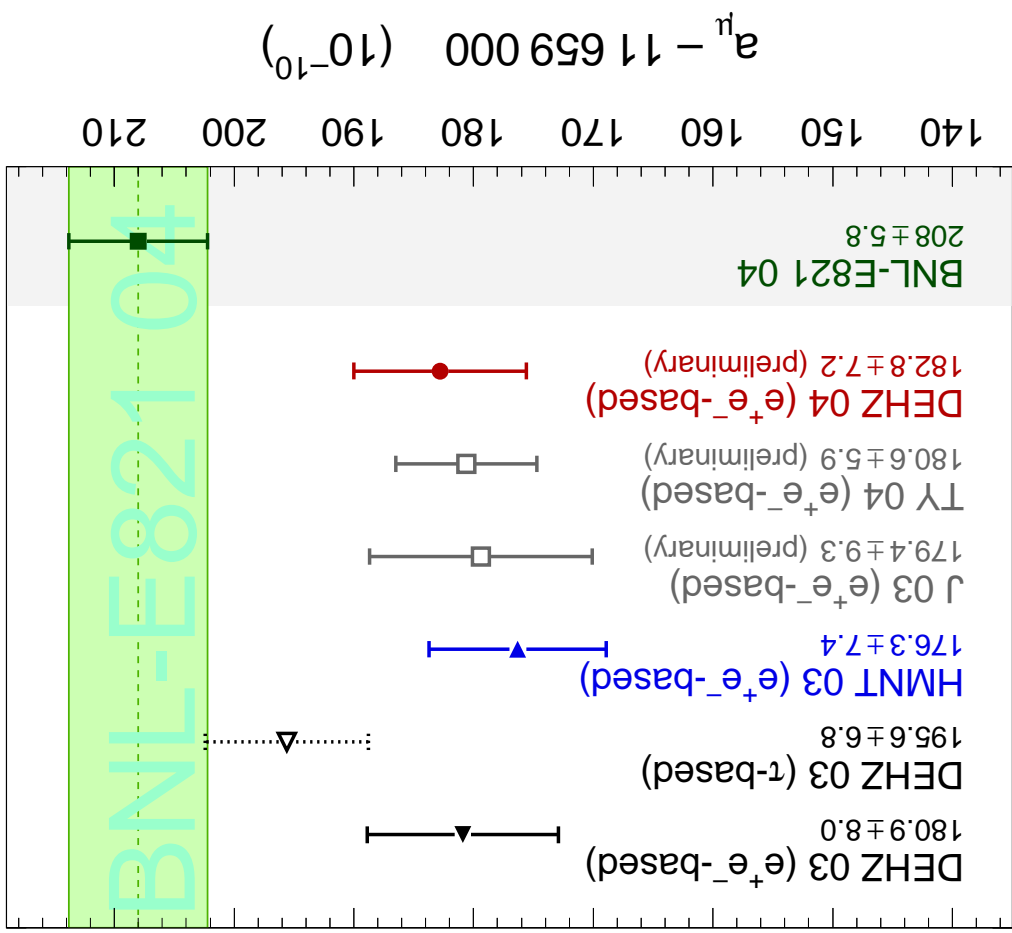
2.7 standard deviations from the BNL measurement !

When compared to the world average of the muon magnetic anomaly measurements, dominated by the results from the BNL experiment,

$$a_\mu = (11\,659\,208.0 \pm 5.8) 10^{-10},$$

Respective e^+e^- and τ -based predictions disagreed at the level of 2.5 and 1.3 standard deviations, when adding exp. and th. errors in quadrat

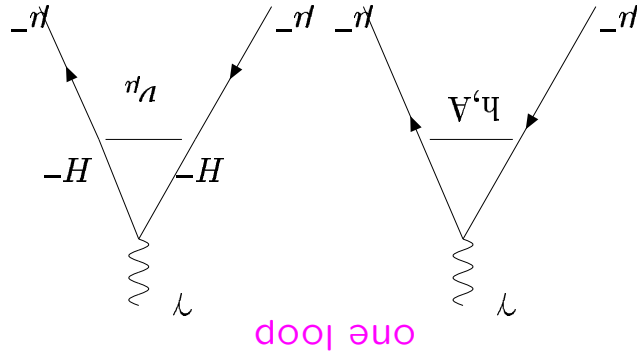
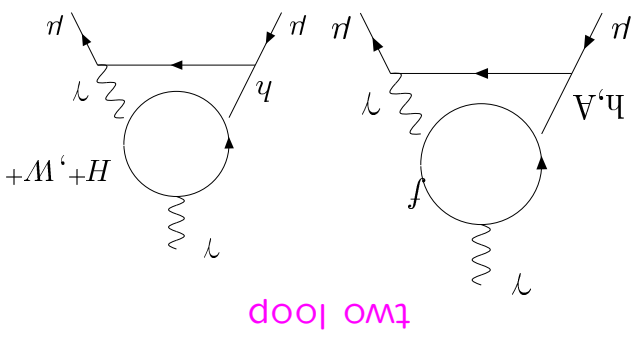




Summary

Two loop contributions larger than one-loop for mass \sim few GeV!

Zochowski, MK'96, MK'01; Dedes, Haber'01
Chang et al., Cheung et al., Wu, Zhou, MK'01, '02..

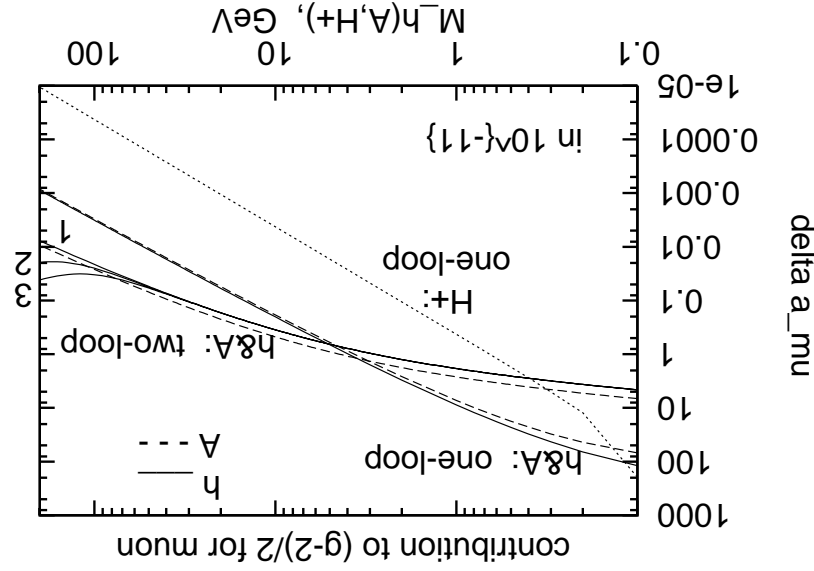


2HDM contribution to a_μ : $a_\mu^{2\text{HDM}} = a_\mu^h + a_\mu^A + a_\mu^H + a_\mu^{H^\pm}$

- light h scenario: $a_\mu^{2\text{HDM}} \approx a_\mu^h$
- light A scenario: $a_\mu^{2\text{HDM}} \approx a_\mu^A$

Various contributions for couplings = 1

- 1- no H^\pm
- 2- $M_{H^\pm} = 800 \text{ GeV}$
- 3- $M_{H^\pm} = 400 \text{ GeV}$



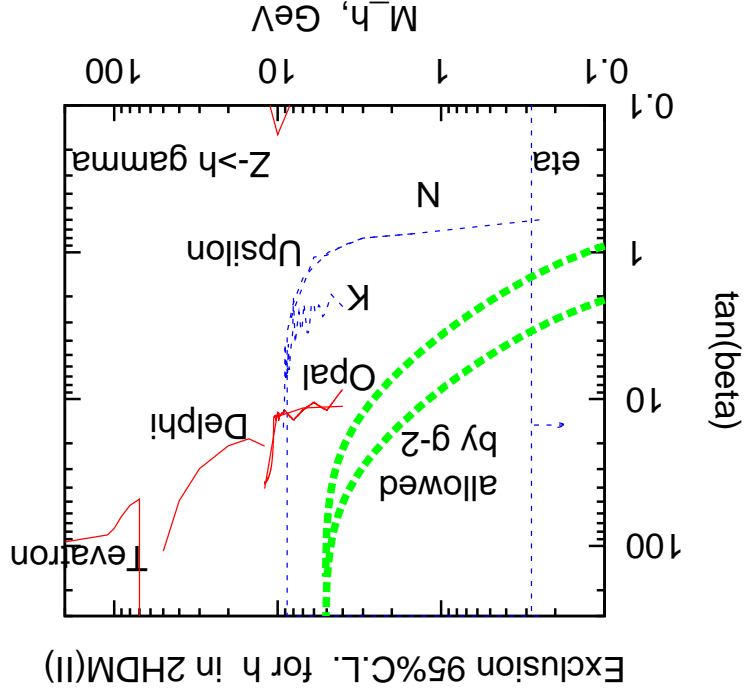
light A

contr. positive
for mass above 5 GeV

light h
contr. positive
for mass below 3 GeV
 $\beta - \alpha = 0, \mu^2 = 0$

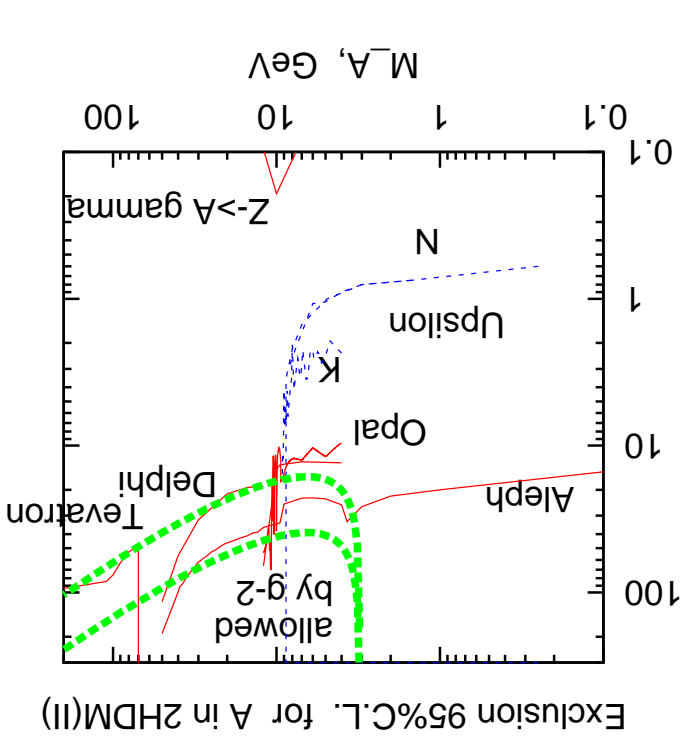
Combined 95% CL constraints for h and A in 2HDM(II) '2004

scalar h for $\beta - \alpha = 0, \mu^2 = 0$



Exclusion 95% C.L. for h in 2HDM(II)

pseudoscalar A



Exclusion 95% C.L. for A in 2HDM(II)

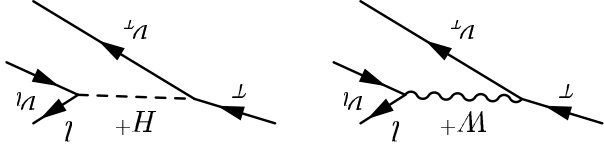
thick lines : upper & lower limits from g-2 plus LEP data, etc

New estimations \Rightarrow allowed regions for A only if all existing data are taken into account

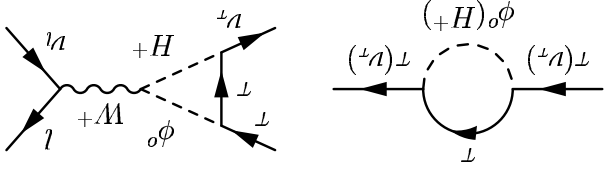
A with mass 25-70 GeV and $25 < \tan \beta < 115$ in agreement with all data

Leptonic tau decays

In SM - tree W exchange, tree level in 2HDM: Charged Higgs bosons



Loop corrections involve neutral Higgs bosons dominant contributions at large tan beta



The partial decay widths and branching ratios:

$$\tau \rightarrow e\bar{\nu}_e\nu_\tau \text{ and } \tau \rightarrow \mu\bar{\nu}_\mu\nu_\tau.$$

The '04 world averaged data for the leptonic τ decay modes and τ lifetime:

$$Br_e^{exp} = (17.84 \pm 0.06)\%, \quad Br_\mu^{exp} = (17.37 \pm 0.06)\%$$

$$\tau_\tau = (290.6 \pm 1.1) \times 10^{-15} \text{s}.$$

Note that the relative errors of the above measured quantities are of the order 0.34-0.38 %, the biggest being for the lifetime.

The SM prediction for these branching ratios can be defined as the ratios of the SM predicted decay widths to the total width as measured in the lifetime experiments, namely $Br_l^{SM} = \Gamma_l^{SM} / \Gamma_{tot}^{exp} = \Gamma_l^{SM\tau}$. Therefore, one can parametrise a possible beyond the SM contribution by a quantity Δ_l , defined as

$$Br_l = Br_l^{SM} (1 + \Delta_l). \quad (1)$$

In the lowest order of SM

$$Br_e^{SM} = (17.80 \pm 0.07)\%, \quad Br_\mu^{SM} = (17.32 \pm 0.07)\%. \quad (2)$$

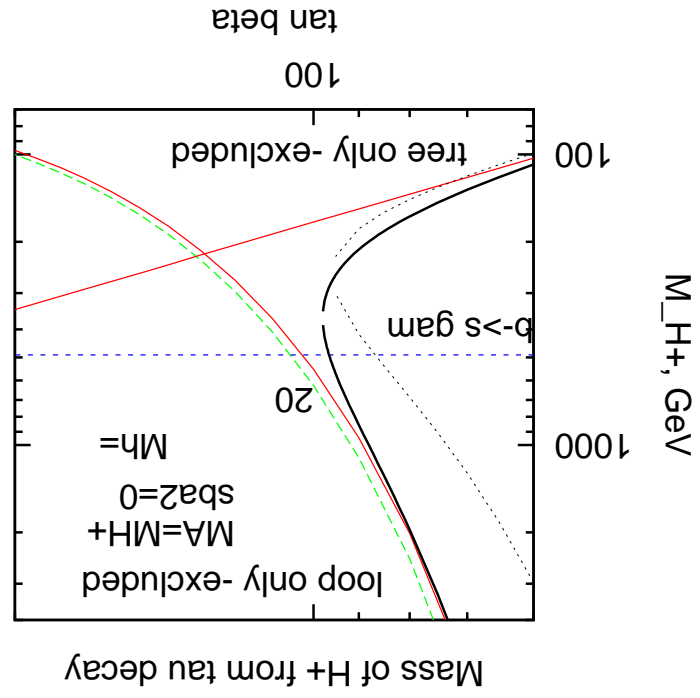
Together with the experimental data this leads to the following estimations for the possible beyond SM contributions to the considered branching ratios,

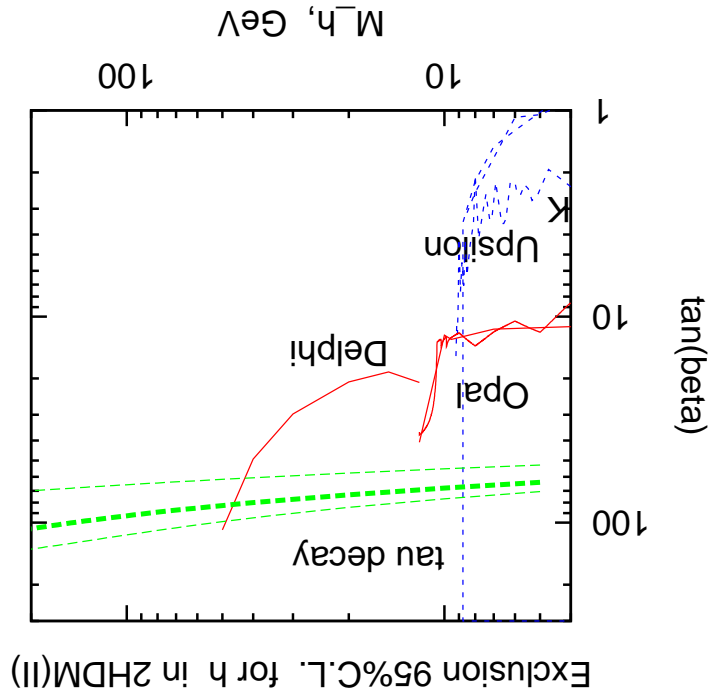
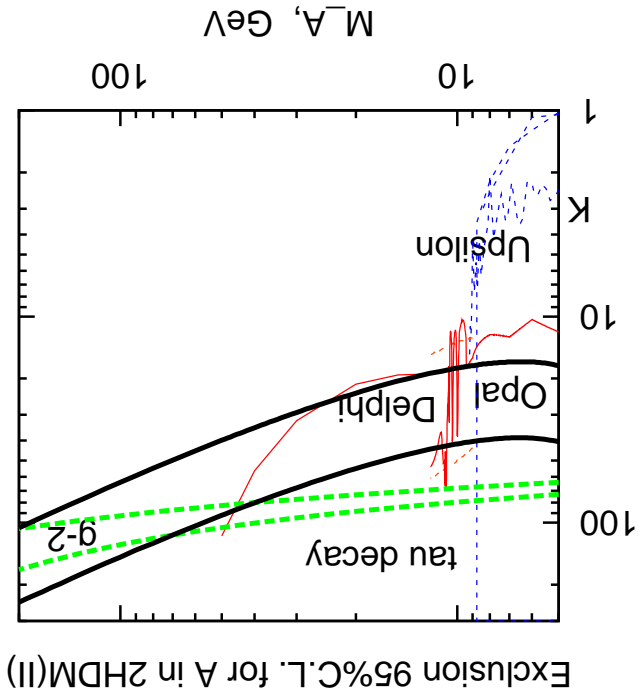
$$\Delta_e = (0.20 \pm 0.51)\%, \quad \Delta_\mu = (0.26 \pm 0.52)\%.$$

Using them we derive the 95% C.L. bounds on Δ_l , for the electron and muon decay mode, respectively:

$$(-0.80 \leq \Delta_e \leq 1.21)\%, \quad (-0.76 \leq \Delta_\mu \leq 1.27)\%.$$

One can see that the negative contributions are constrained more strongly than the positive ones.





- In 2HDM - various potentials possible
- Large masses of Higgs particle can be obtained in two different ways:
 - by large μ parameter related to the soft term in the potential
 - by large (but not too large) couplings λ_i
- The selfcoupling of Higgs particles, like $g_{hH^+H^-}$, if expressed in terms of masses, depends on μ
- The $H \rightarrow \gamma\gamma$ process, due to loop with H^\pm , is sensitive to this coupling. It can be used to distinguish between SM and SM-like 2HDM(II)
- Light h of Δ even with mass ~ 10 GeV in agreement with data

Conclusions

Challenge → SM-like scenarios in the extensions of the SM

- SM-like, with mass eg. 115 GeV, couplings as for H^{SM} (relative couplings $\chi_V, \chi_u, \chi_d = 1$)

- very light, with mass eg. few GeV, and with very weak (or no) coupling to Z/W

with the lightest Higgs boson

2HDM (II) - in agreement with data even in such extreme cases:

What that means: SM in agreement with data?

Light or Little Higgs?