

**Measurement of the Higgs-boson CP
properties from decays into WW and ZZ at
the Photon Collider**

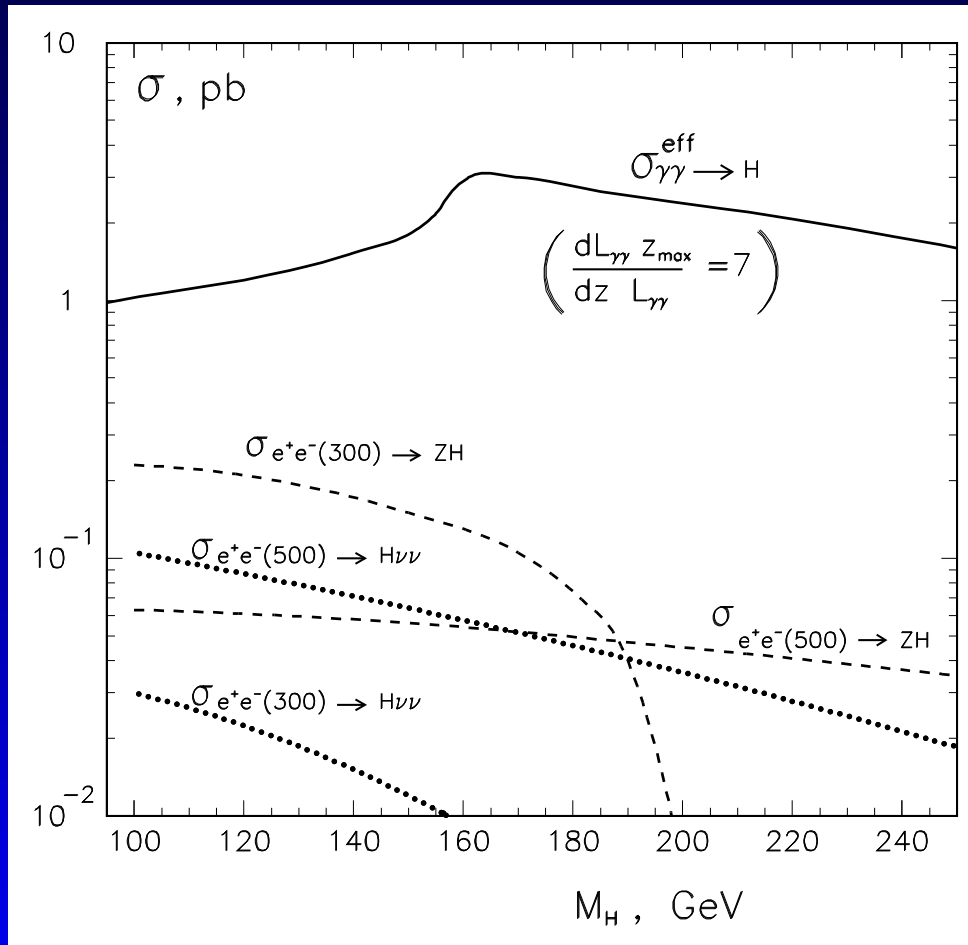
**Higgs Physics at Future Colliders workshop
2004/2005**

**A.F.Żarnecki
09.03.2005**

Introduction

Why do we need Photon Collider ?

Comparison of SM Higgs boson production cross sections:



$\gamma\gamma$ cross section order of magnitude higher

$$\sigma = \frac{1}{\mathcal{L}_{\gamma\gamma}} \frac{d\mathcal{L}_{\gamma\gamma}^{J_z=0}}{dW_{\gamma\gamma}} \cdot \frac{4\pi^2 \Gamma_{\gamma\gamma}}{M_h^2}$$

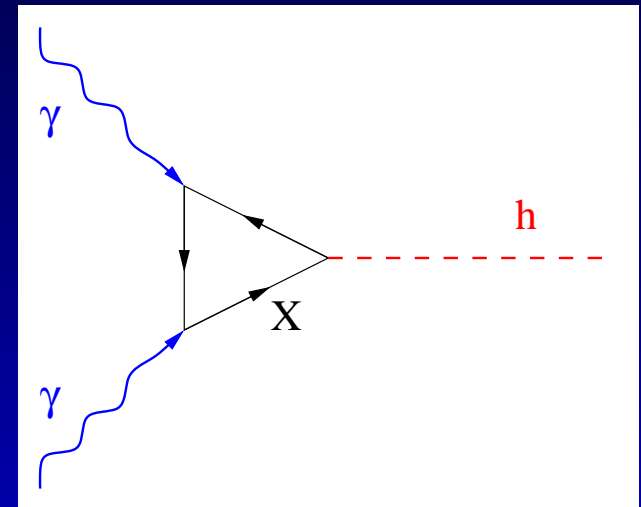
expected $\gamma\gamma$ luminosity similar to e^+e^-



Higgs boson at PC

Two-photon width of the Higgs boson $\Gamma_{\gamma\gamma}$ is sensitive to all massive and charged particles in the loop:

$$\Gamma(h \rightarrow \gamma\gamma) = \frac{G_F \alpha^2 M_h^3}{128 \sqrt{2} \pi^3} \cdot |\mathcal{A}|^2$$



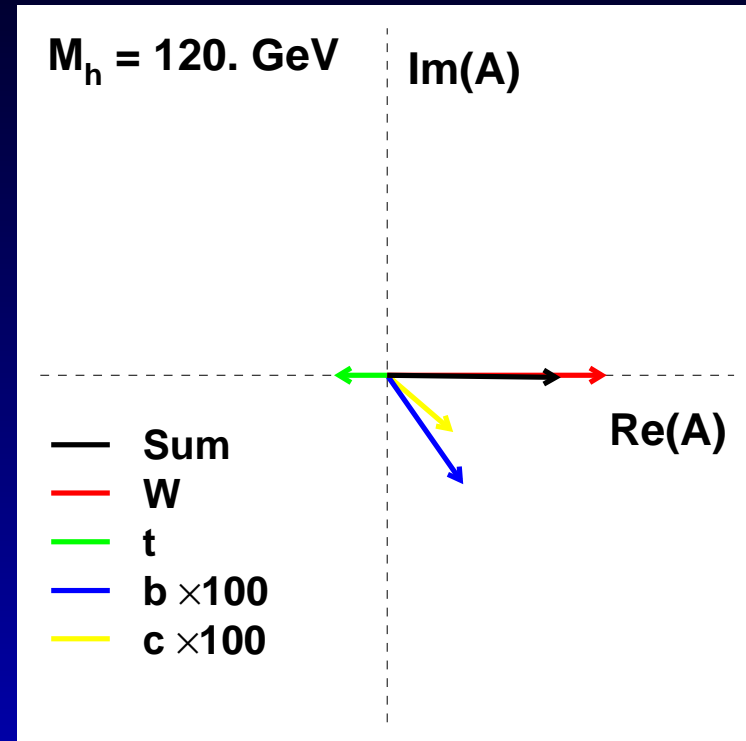
where:

$$\mathcal{A} = A_W(M_W) + \sum_f N_c Q_f^2 A_f(M_f) + \dots$$

two-photon amplitude

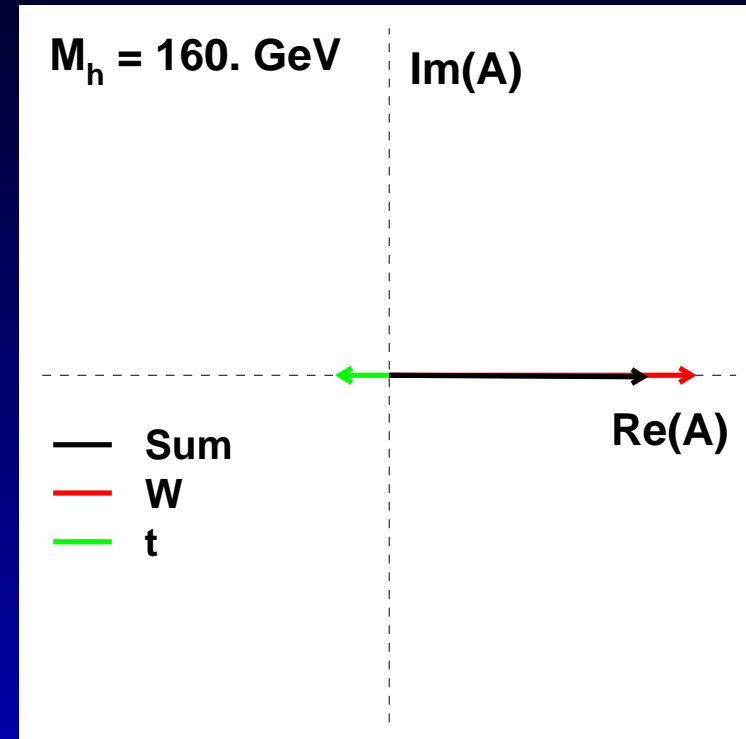
Phase

amplitude \mathcal{A} is **real**
 imaginary contribution from light
 fermions - very tiny



Phase

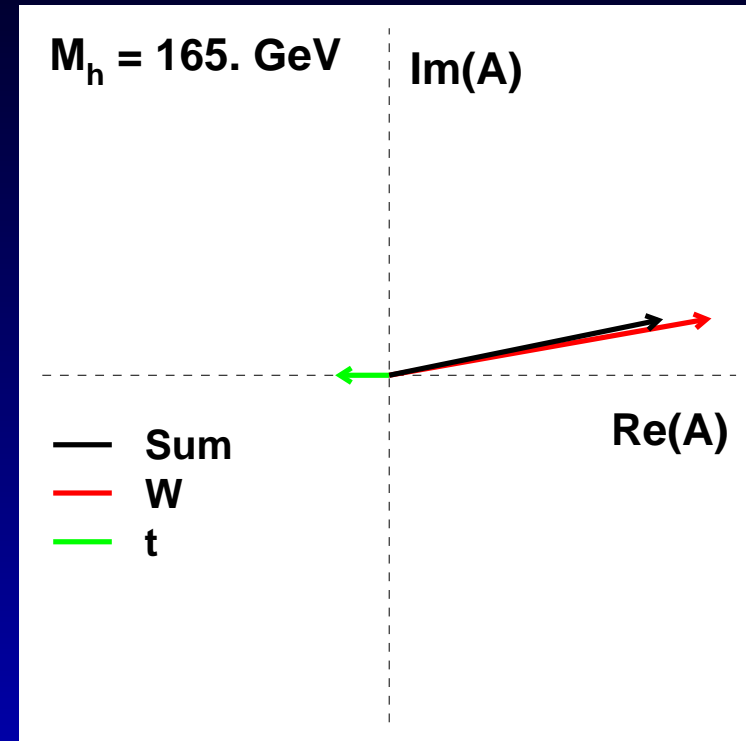
For $m_H \leq 2m_W$
 amplitude \mathcal{A} is real



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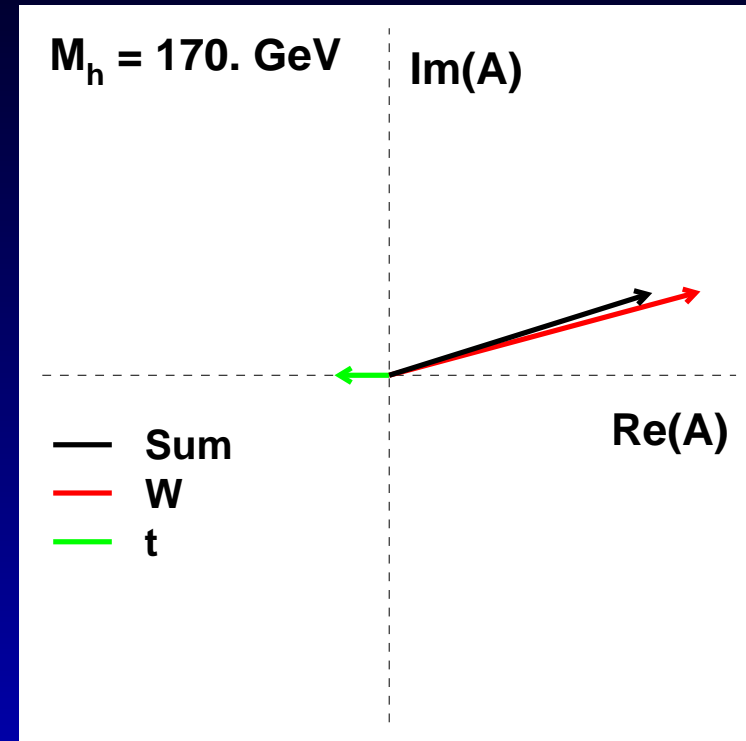
For $m_H > 2m_W$
 W contribution is **complex**



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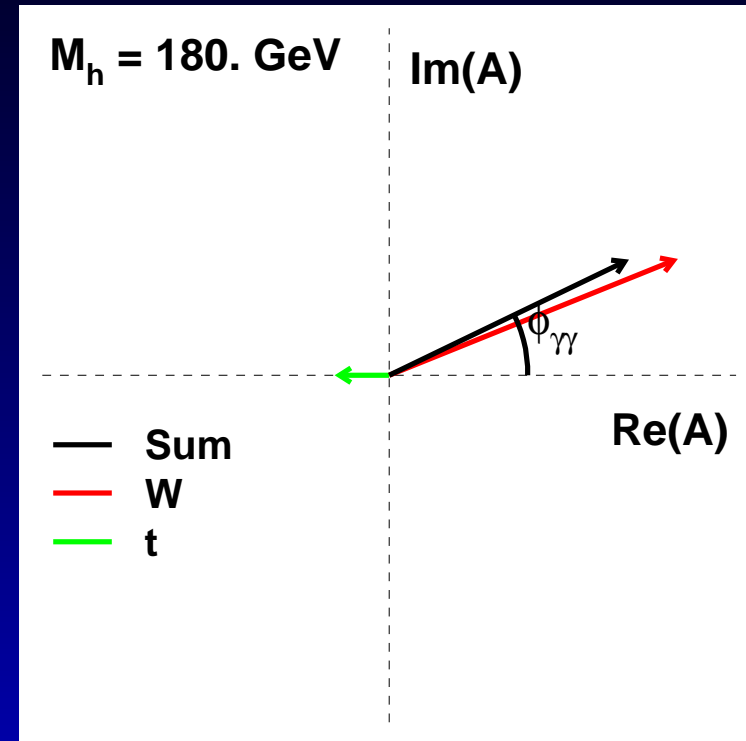
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$$\mathcal{A} = |\mathcal{A}| \cdot e^{i\phi} - \text{phase } \phi_{\gamma\gamma} \neq 0$$

$$\Gamma_{\gamma\gamma} \sim \text{Im}(\mathcal{A})^2 + \text{Re}(\mathcal{A})^2$$



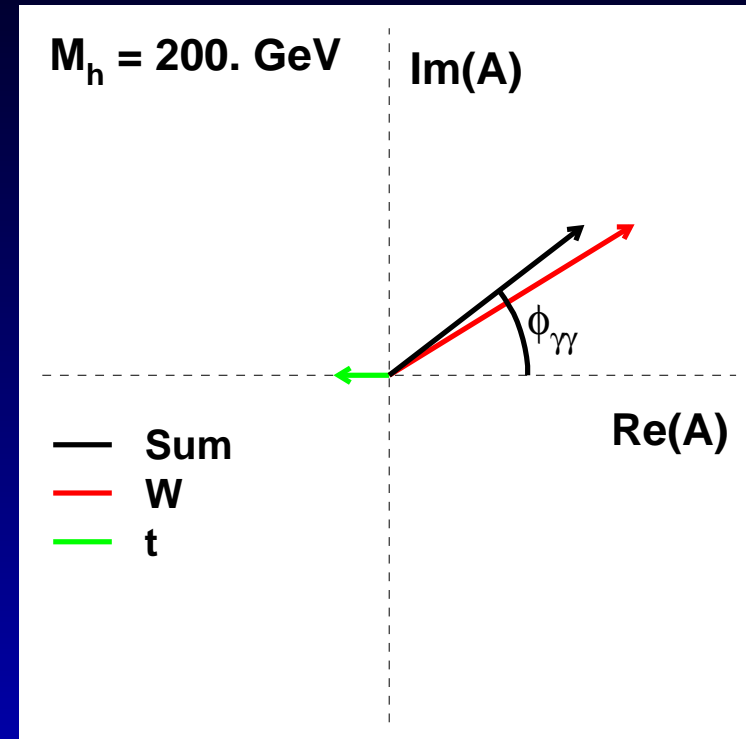
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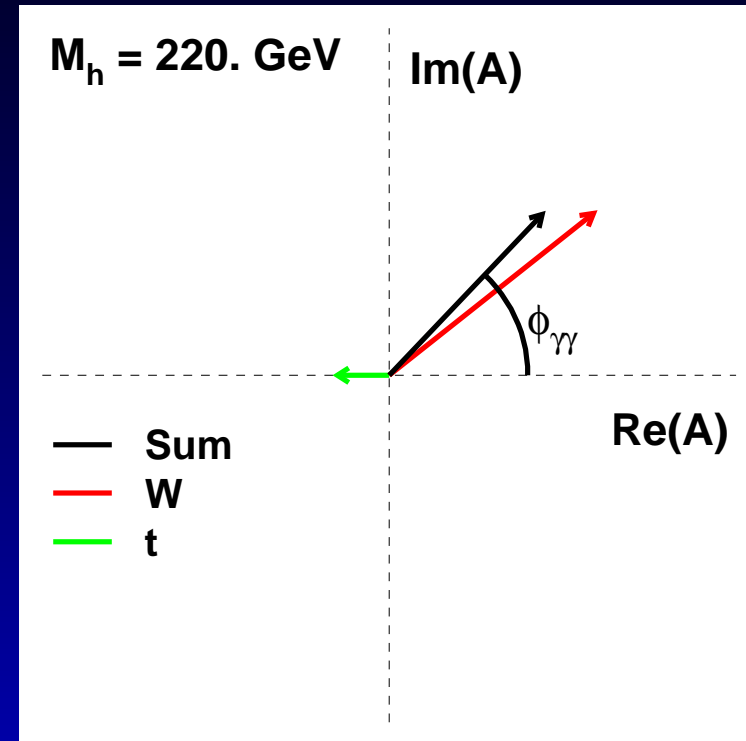
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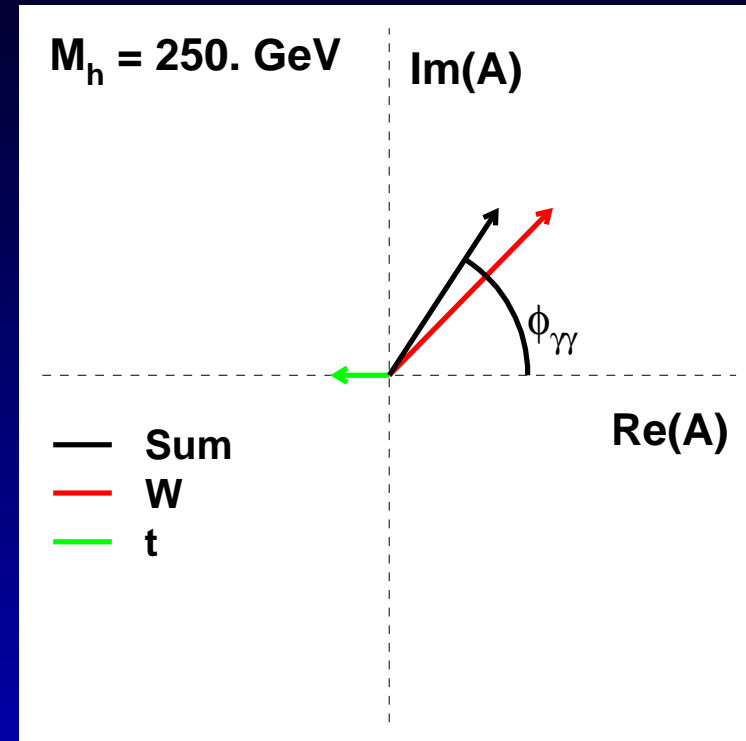
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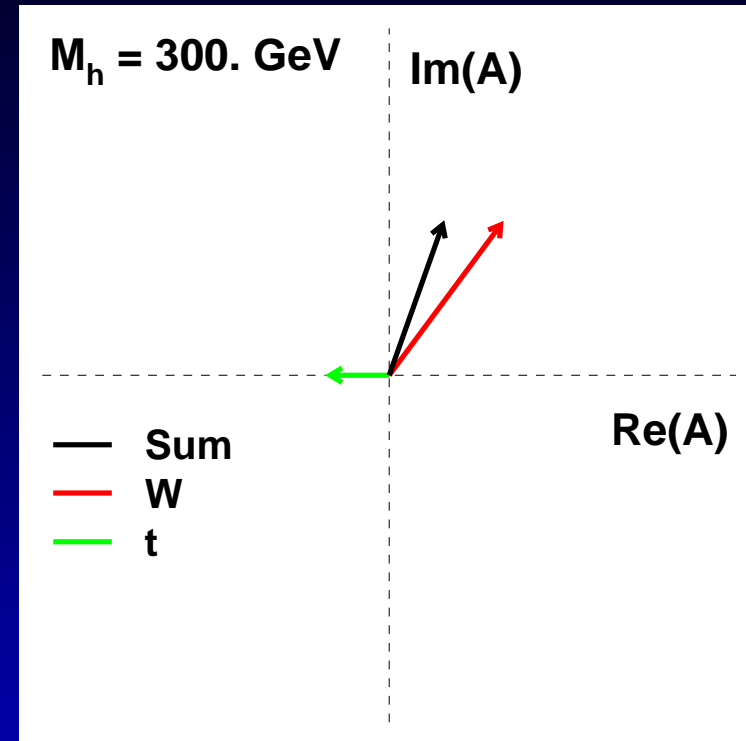
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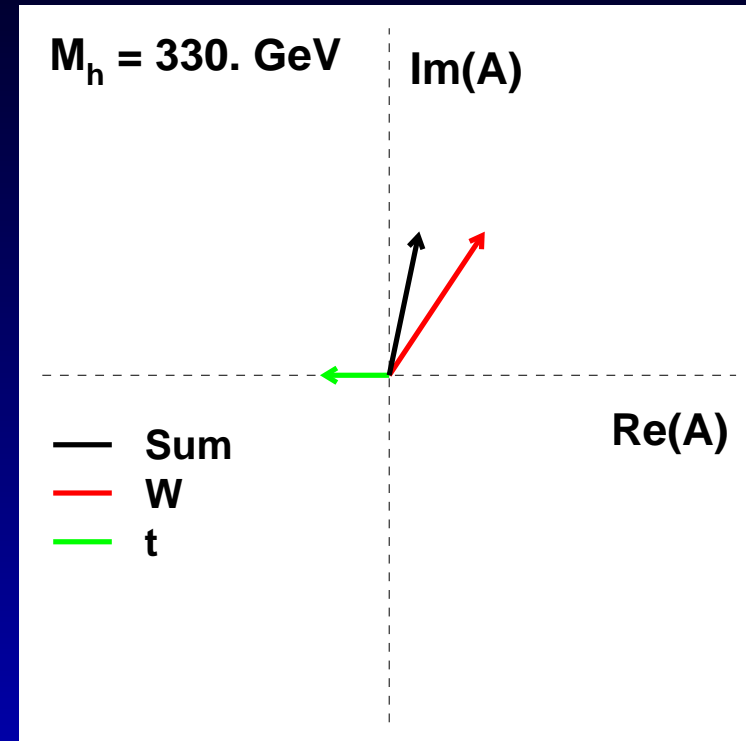
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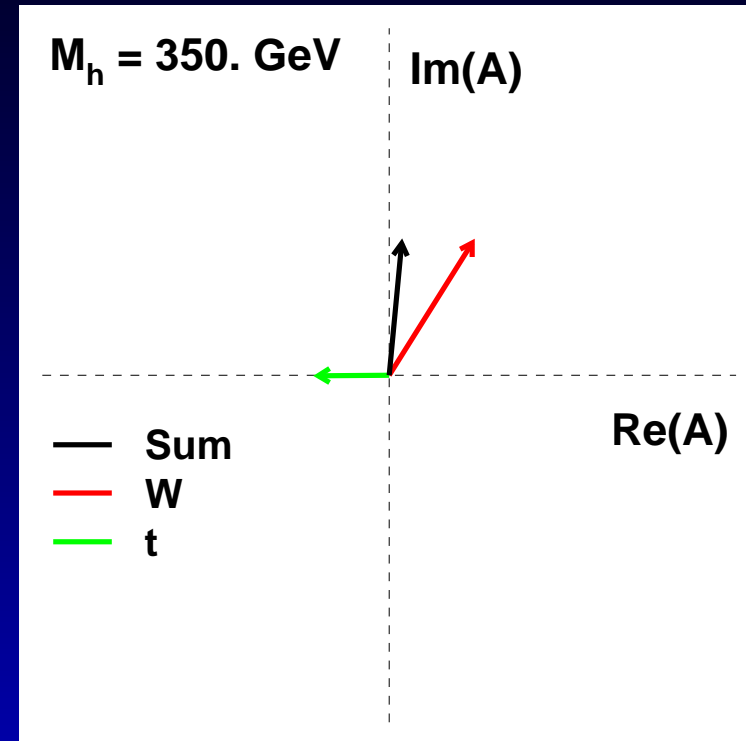
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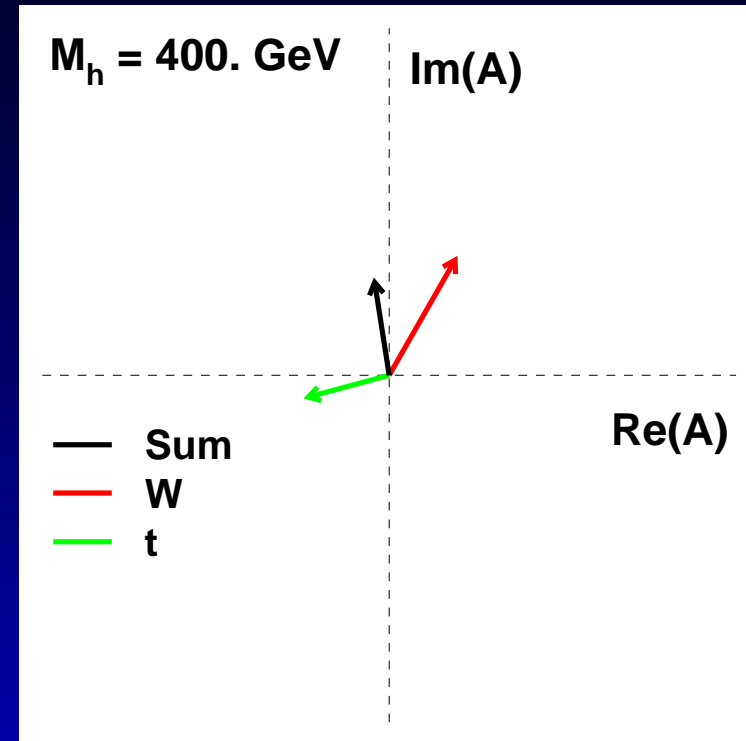
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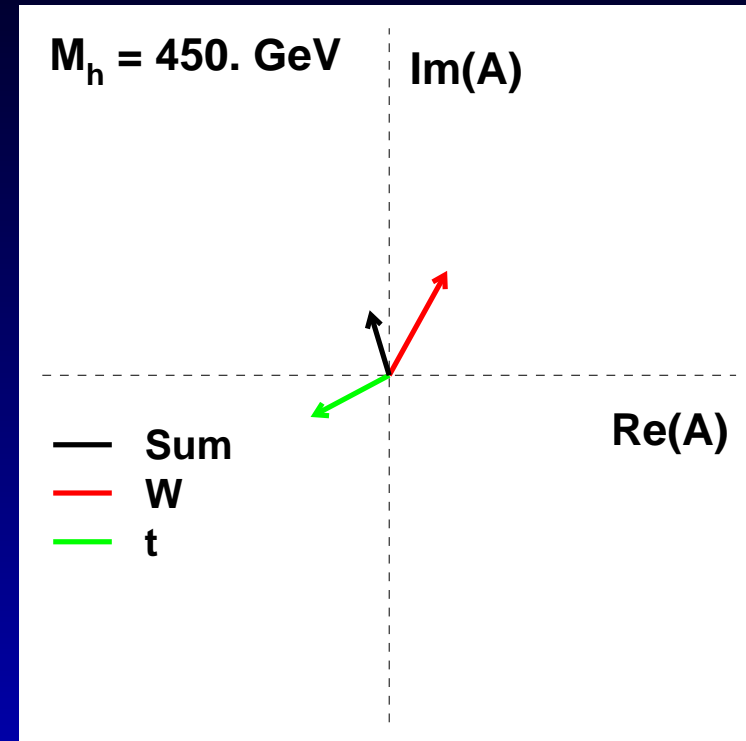
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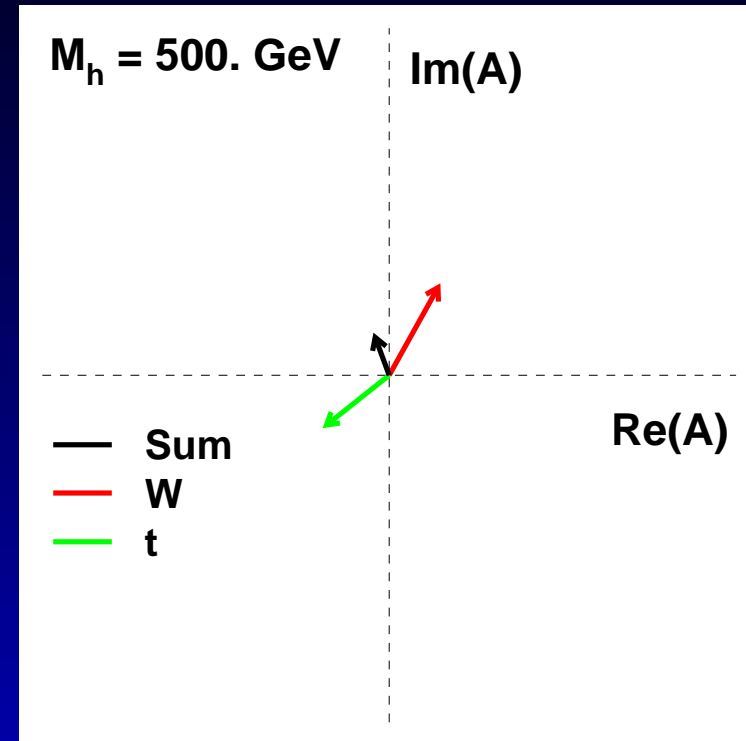
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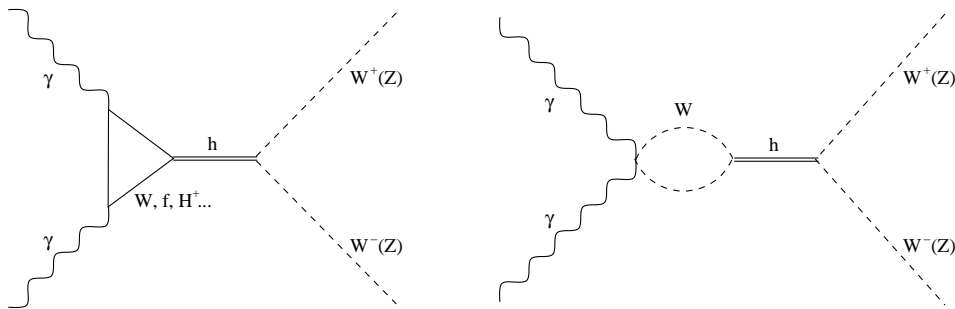
$$\Gamma_{\gamma\gamma} \sim \text{Im}(\mathcal{A})^2 + \text{Re}(\mathcal{A})^2$$



$$\gamma\gamma \rightarrow (h) \rightarrow W^+W^-, ZZ$$

Higgs production and decay

For $M_h > 2M_W$, $h \rightarrow W^+W^-$ dominate:



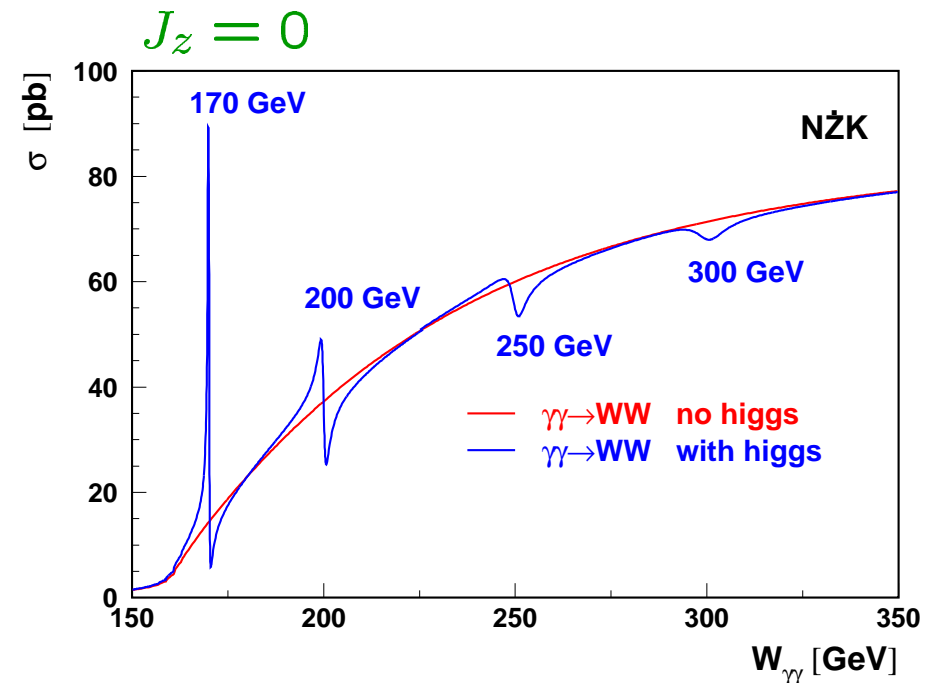
“resonant”

There is a large background from “direct”, non-resonant production $\gamma\gamma \rightarrow W^+W^-$

G.Belanger, F.Boudjema, Phys.Lett.B288(1992)210;
D.A.Morris, et al., Phys. Lett. B323(1994)421;
I.F.Ginzburg, I.P.Ivanov, Phys. Lett. B408(1997)325.

Interference

Resonant and direct amplitudes interfere
Large effects expected:

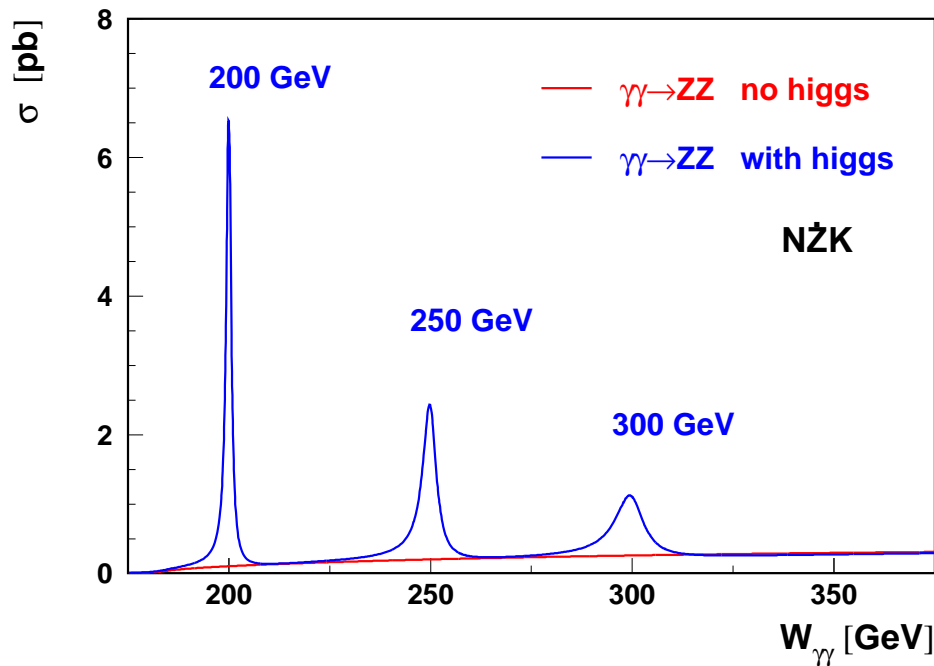


Destructive interference dominates above ~ 200 GeV

$$\gamma\gamma \rightarrow (h) \rightarrow W^+W^-, ZZ$$

$$\gamma\gamma \rightarrow ZZ$$

Non-resonant background only at loop level



⇒ small interference effects

G.J.Gounaris et al., Eur. Phys. J. C13 (2000) 79.

Simulation

$\gamma\gamma$ spectra from **CompAZ** hep-ex/0207021

$\gamma\gamma \rightarrow W^+W^-, ZZ$ events
generated with PYTHIA 6.152

events reweighted to take into account:

- beam polarization
- Higgs production and interference

detector simulation with SIMDET v. 3.01

total $\gamma\gamma$ luminosity: 600 – 1000 fb^{-1}

High $W_{\gamma\gamma}$ peak: 75 – 115 fb^{-1}

for $\sqrt{s_{ee}} = 305 – 500$ GeV

$$\gamma\gamma \rightarrow (h) \rightarrow W^+W^-, ZZ$$

Parametrization

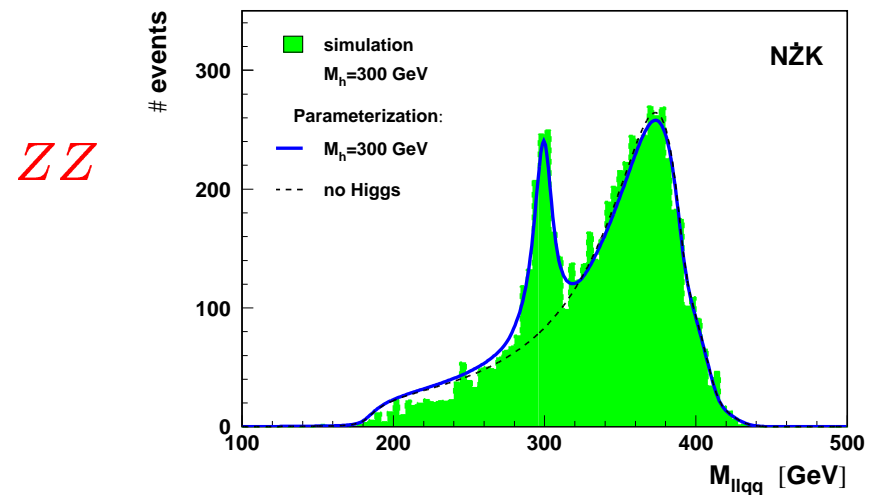
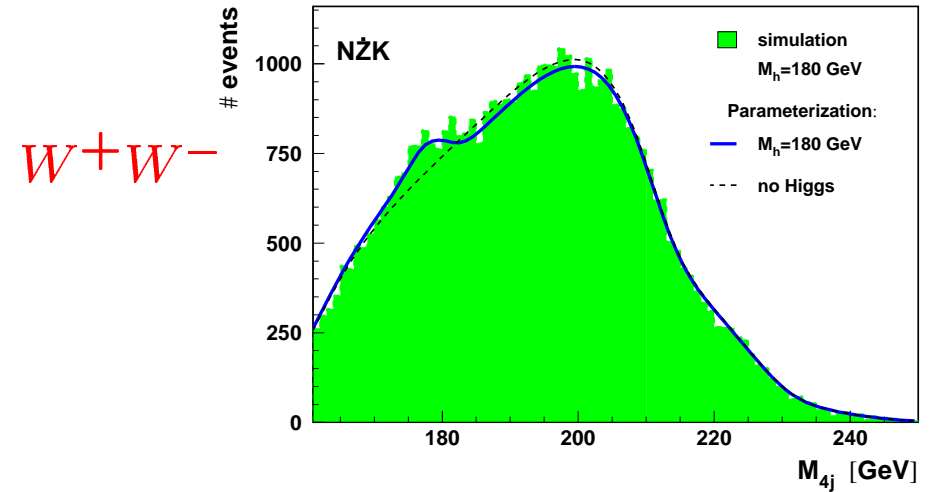
“Measured” invariant mass distribution for selected W^+W^- and ZZ events is described by convolution of:

- Analytical luminosity Spectra **CompAZ**
- Cross section formula for signal + background + **interf.**
- Invariant mass resolution parametrized as a function of $W_{\gamma\gamma}$

⇒ mass spectra can be calculated for any $\sqrt{s_{ee}}$ and m_h without time-consuming MC simulation

⇒ can be used for fast simulation and fitting

Comparison with full simulation:



SM results

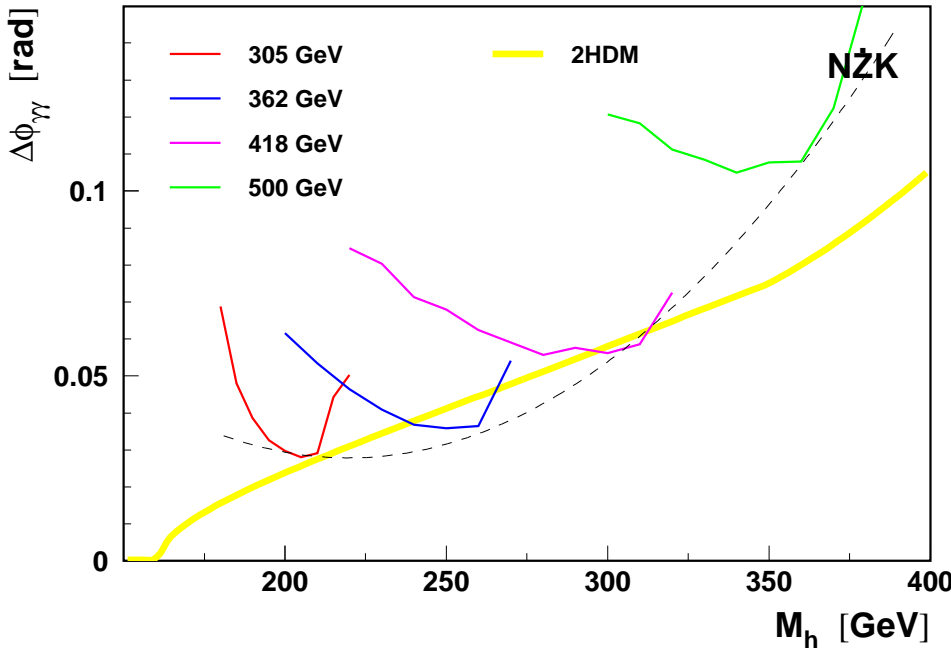
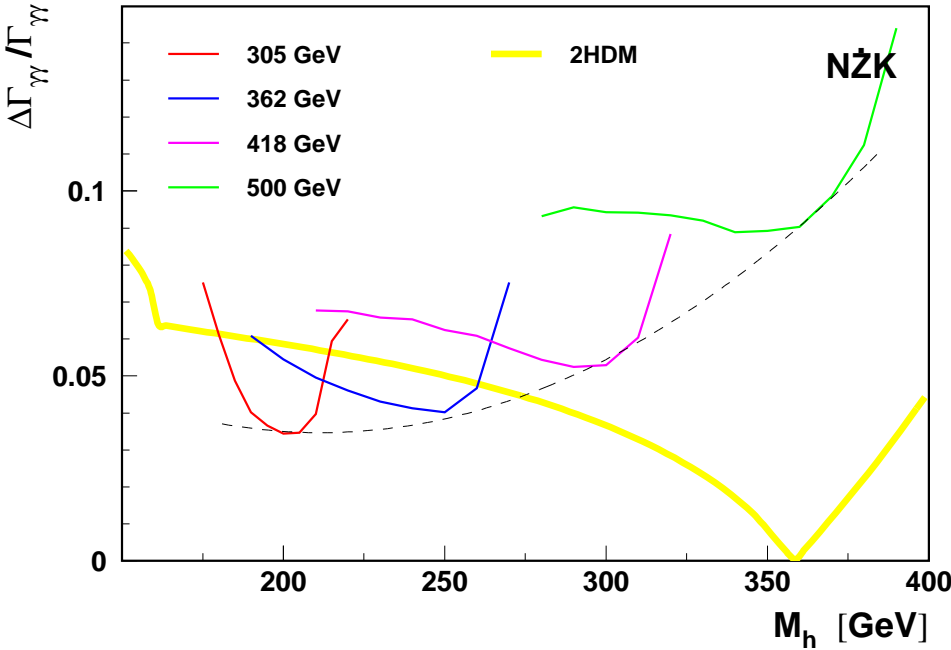
Two parameter fit to W^+W^- and ZZ invariant mass distribution

Expected statistical precision, assuming SM branching ratios (1 PC year):

$\Gamma_{\gamma\gamma}$

hep-ph/0207294

$\phi_{\gamma\gamma}$



Phase measurement significantly improves our sensitivity to new heavy charged particles e.g. heavy charged Higgs boson of the SM-like 2HDM(II) with $M_{H^\pm} = 800$ GeV at large Higgs boson masses

CP conserving 2HDM (II)

Higgs boson couplings

Scalar Higgs bosons h and H
with basic couplings (relative to SM):

$$\chi_x = g_{\mathcal{H}xx} / g_{\mathcal{H}xx}^{SM} \quad \mathcal{H} = h, H, A$$

	h	H	A
χ_u	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$-i \gamma_5 \frac{1}{\tan \beta}$
χ_d	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$-i \gamma_5 \tan \beta$
χ_V	$\sin(\beta - \alpha)$	$\cos(\beta - \alpha)$	0

For charged Higgs boson couplings
(loop contribution to $\Gamma_{\gamma\gamma}$) we set

$$M_{H^\pm} = 800 \text{ GeV} \quad \mu = 0$$

Higgs couplings are related by
“patter relation”

$$(\chi_V - \chi_d)(\chi_u - \chi_V) + \chi_V^2 = 1$$

I. F. Ginzburg, M. Krawczyk and P. Osland,
hep-ph/0101331

Instead of angles α and β use couplings χ_V and χ_u to parametrize cross sections

$$0 \leq \chi_V \leq 1$$

If we neglect H decays to h and A
(small) cross sections and BRs calculated for H are also valid for h

2HDM(II)

SM-like 2HDM(II)

Solution A

For light Higgs boson h :

$$\chi_u = \chi_d = \chi_V = 1$$

χ_i - couplings normalized to SM couplings

All couplings are the same as in SM.

$\Gamma_{\gamma\gamma}$ and $\phi_{\gamma\gamma}$ affected only by the H^+ loop

For heavy Higgs bosons H and A :

$$\chi_V \equiv 0$$

No decays to W^+W^- and ZZ ...

I. F. Ginzburg, M. Krawczyk and P. Osland,
Nucl. Instrum. Meth. A472:149, 2001
hep-ph/0101331; hep-ph/0101208.

Solution B (extended)

	h	H	A
χ_u	-1	$-\frac{1}{\tan\beta}$	$-i \gamma_5 \frac{1}{\tan\beta}$
χ_d	+1	$-\tan\beta$	$-i \gamma_5 \tan\beta$
χ_V	$\cos(2\beta)$	$-\sin(2\beta)$	0

$\tan\beta \rightarrow 0 \Rightarrow \text{sol. } B_u$

$\tan\beta \rightarrow \infty \Rightarrow \text{sol. } B_d$

Higgs production ($\Gamma_{\gamma\gamma}$ and $\phi_{\gamma\gamma}$)
and decays depend on $\tan\beta$.

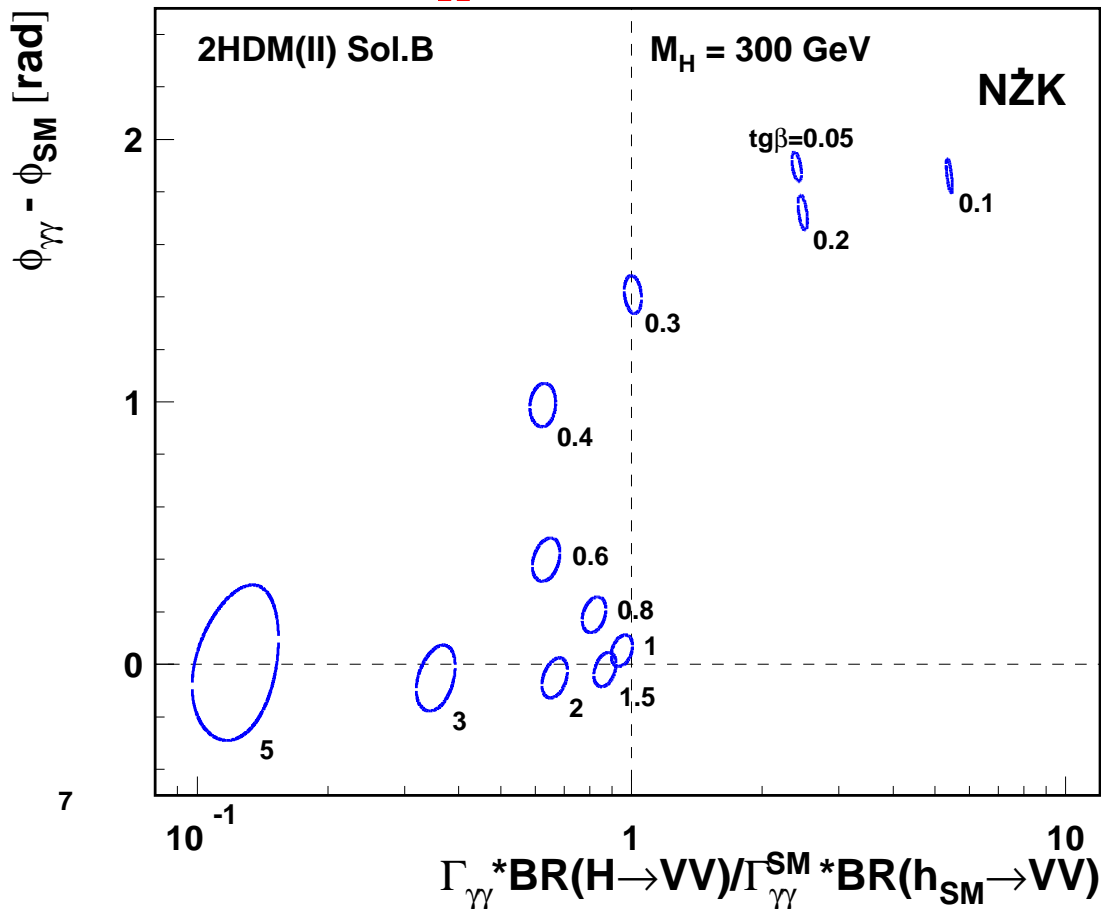
**Can we extract $\tan\beta$ value
from the measured W^+W^- and ZZ
invariant mass distributions ?**

SM-like 2HDM(II)

Heavy Higgs boson H

Two-photon width and phase measurement for different $\tan \beta$ $\chi_V = -\sin 2\beta$

$M_H = 300 \text{ GeV}$



$\Gamma_{\gamma\gamma}$ enhancement for $\tan \beta < 1$ due to top contribution ($\chi_u = -\frac{1}{\tan \beta}$)

1 σ contours for 1 year of PC running
statistical errors only

$M_h = 120 \text{ GeV}, M_{H^\pm} = 800 \text{ GeV}$

SM-like 2HDM(II)

Light Higgs boson

Influence of **systematic uncertainties** on the $\tan \beta$ determination is estimated by adding additional **free parameters** to the fit:

Uncertainties:

- luminosity
- energy scale
- mass resolution
- luminosity spectra

Parameters:

- ⇒ overall normalization
relative normalization of WW and ZZ samples fixed
- ⇒ Higgs boson mass
- ⇒ Higgs boson width
- ⇒ spectra shape variations

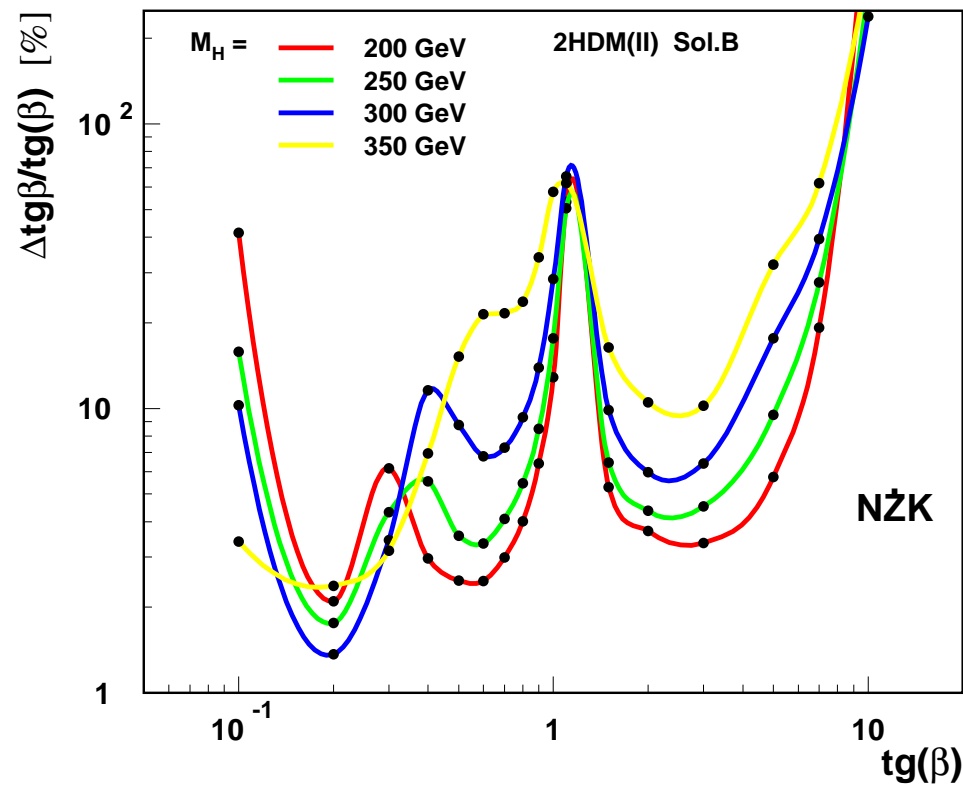
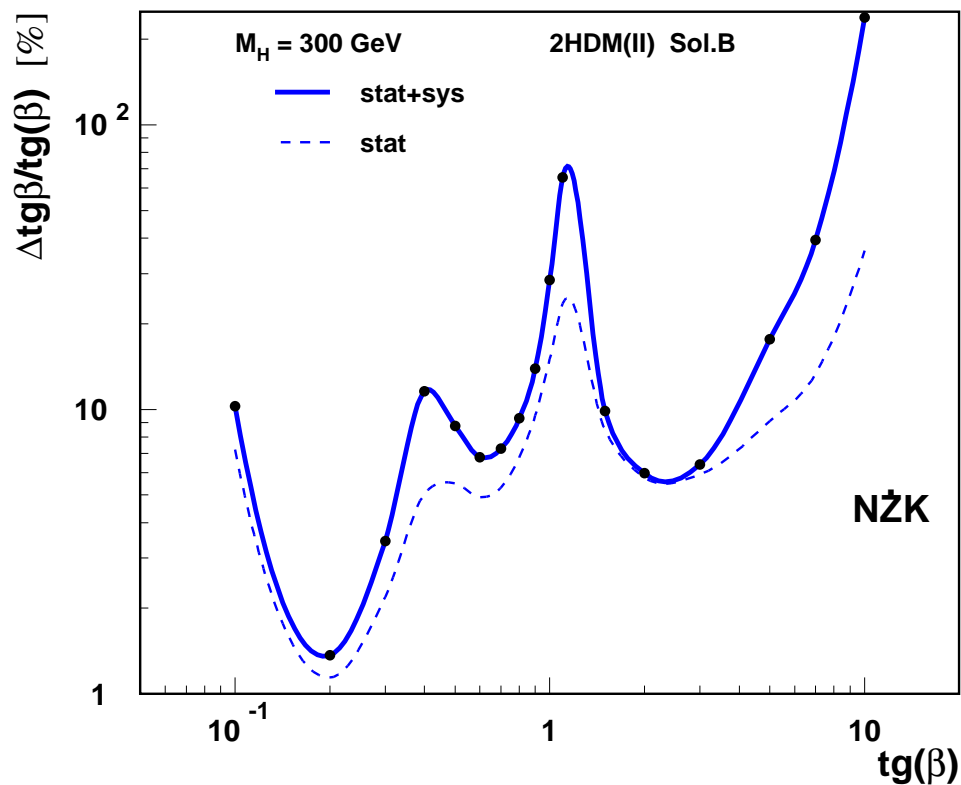
$$\frac{dL}{dW_{\gamma\gamma}} = \frac{dL^{CompAZ}}{dW_{\gamma\gamma}} (1 + A \cdot \sin \pi x + B \cdot \sin 2\pi x)$$
$$x = \frac{W_{\gamma\gamma} - W_{min}}{W_{max} - W_{min}}$$

SM-like 2HDM(II)

Heavy Higgs boson H

Influence of systematic uncertainties
for $M_H = 300$ GeV

Expected precision in $\tan\beta$ determination
stat. + sys. errors



Large effects of systematic uncertainties

2HDM(II) with CP violation

General Two Higgs Doublet Model

Mass eigenstates of the neutral Higgs-bosons h_1 , h_2 and h_3 do not need to match CP eigenstates h , H and A .

We consider SM-like 2HDM(II) with CP violation through a small mixing between H and A states

Couplings relative to SM: (assuming $|\Phi_{HA}| \ll 1$)

$$\begin{aligned}\chi_X^{h_1} &\approx \chi_X^h \\ \chi_X^{h_2} &\approx \chi_X^H \cdot \cos \Phi_{HA} + \chi_X^A \cdot \sin \Phi_{HA} \\ \chi_X^{h_3} &\approx \chi_X^A \cdot \cos \Phi_{HA} - \chi_X^H \cdot \sin \Phi_{HA}\end{aligned}$$

$$X = u, d \text{ or } V; \quad V = W \text{ or } Z$$

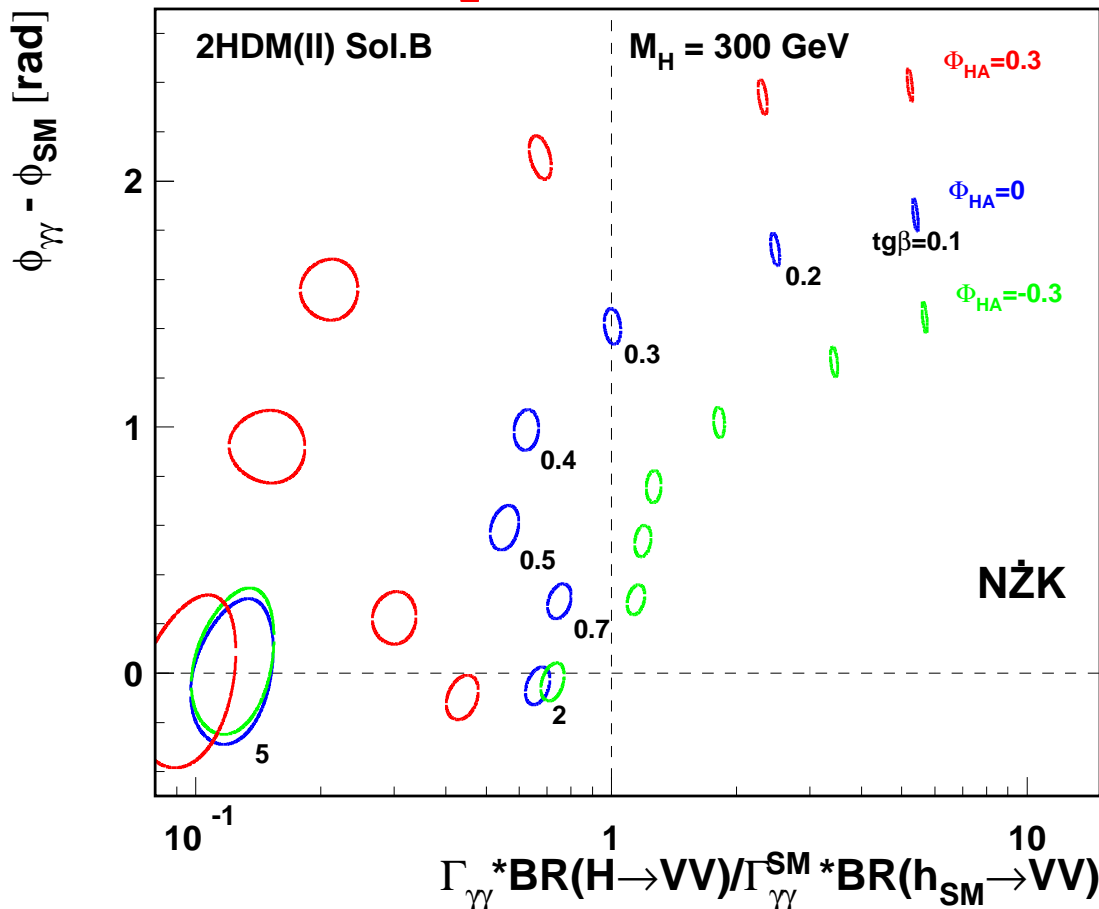
⇒ additional model parameter: **CP-violating mixing phase Φ_{HA}**

2HDM(II) with CP violation

Higgs boson h_2

Two-photon width and phase measurement for different $\tan \beta$ $\Phi_{HA} = 0$

$$M_{h_2} = 300 \text{ GeV}$$



Low $\tan \beta$

\Rightarrow large effects due to H-A mixing

Large $\tan \beta$

\Rightarrow little sensitivity to Φ_{HA}

1σ contours for 1 year of PC running
statistical errors only

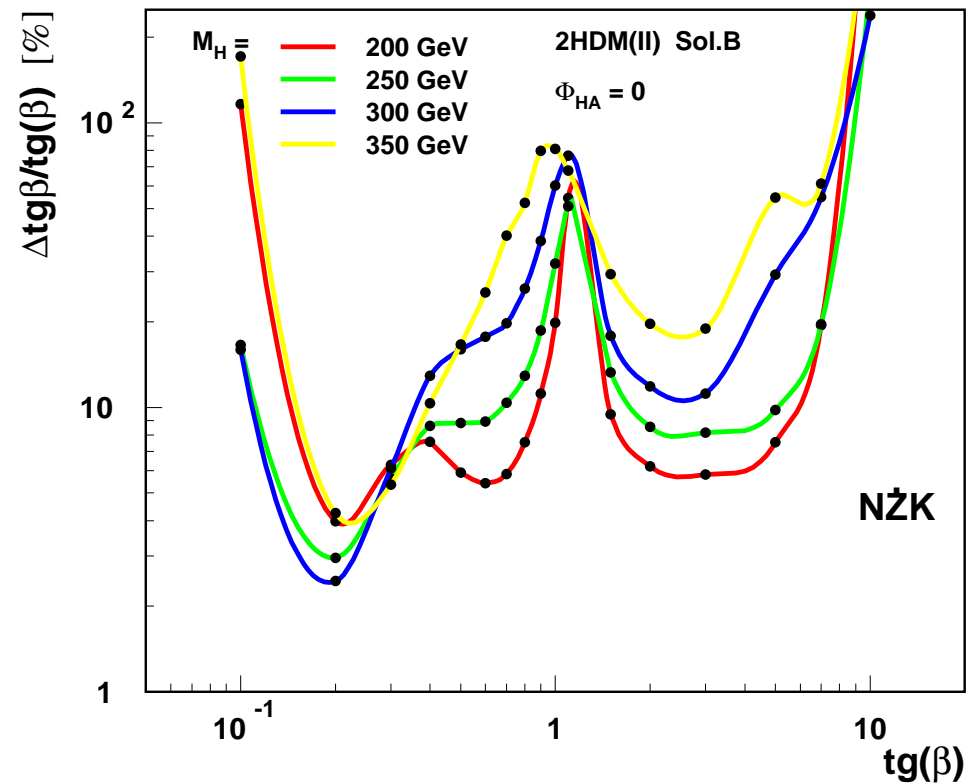
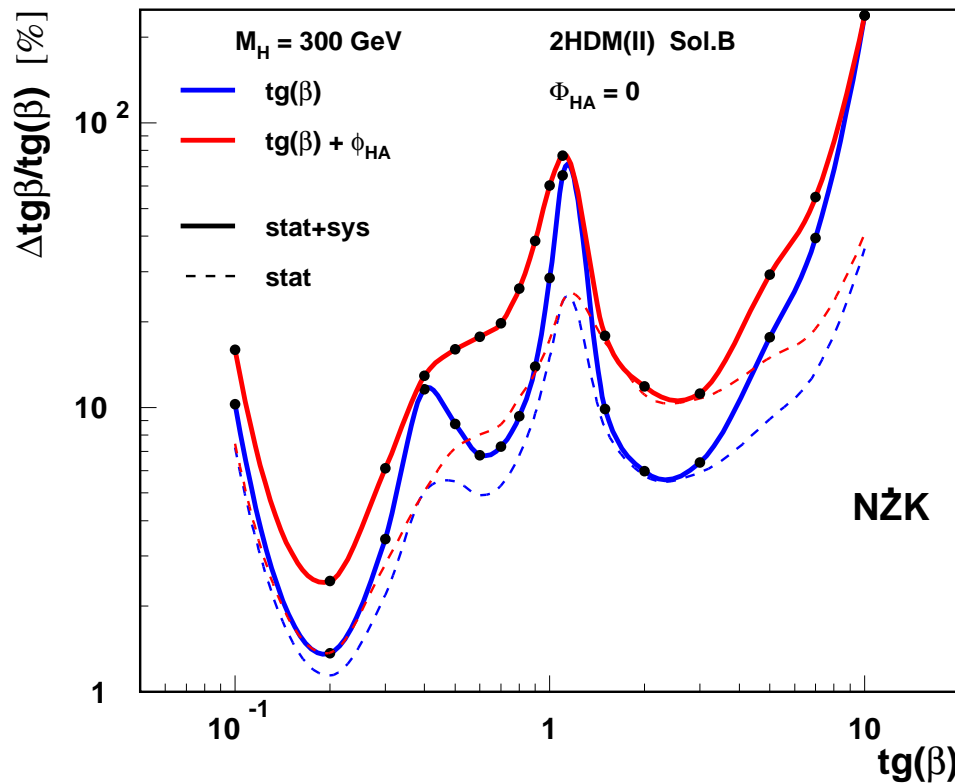
$$M_h = 120 \text{ GeV}, M_{H^\pm} = 800 \text{ GeV}$$

2HDM(II) with CP violation

Higgs boson h_2

Influence of phase and systematics in $\tan \beta$ determination ($M_H = 300$ GeV)

Expected precision in $\tan \beta$ determination stat. + sys. errors from $\tan \beta$ and Φ_{HA} fit



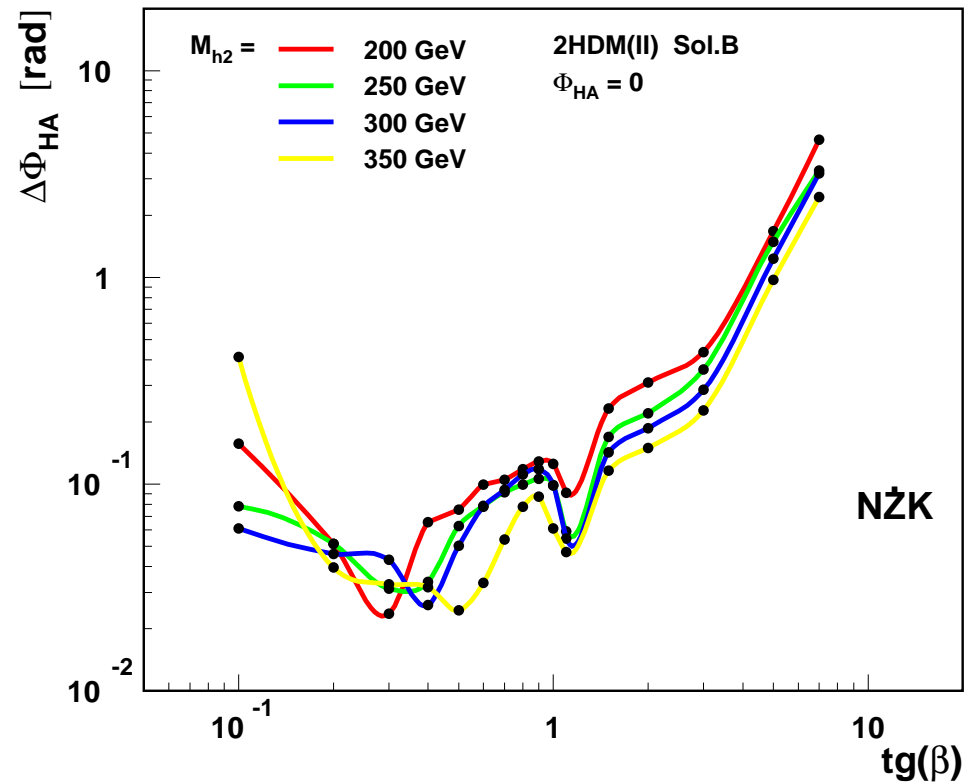
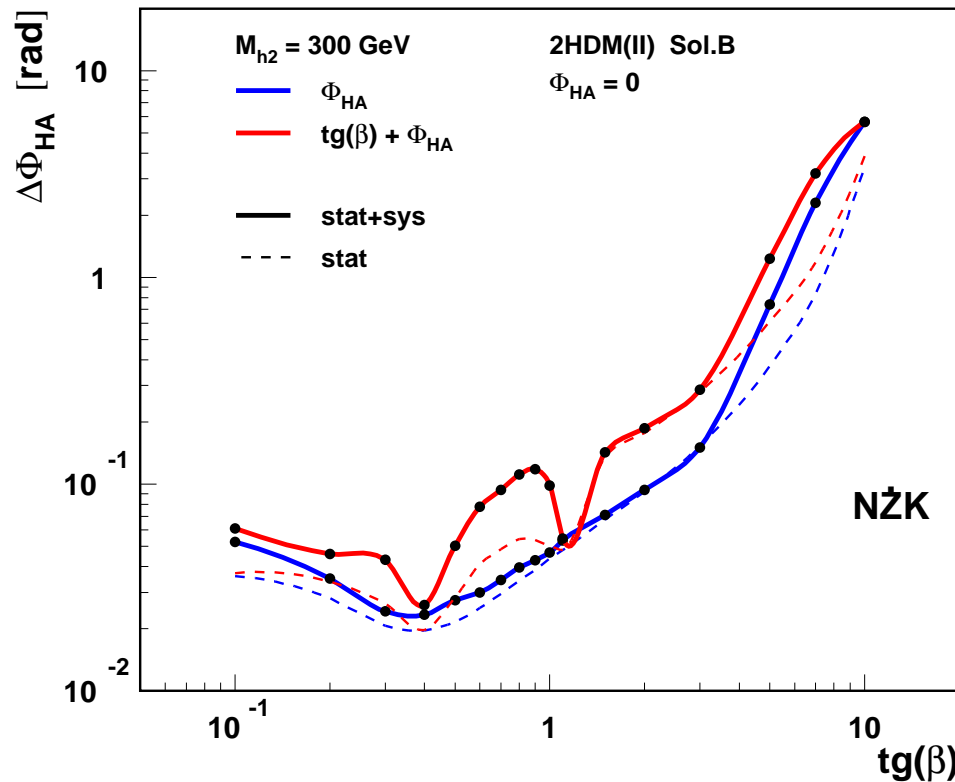
Possible CP violation increases expected $\tan \beta$ measurement errors

2HDM(II) with CP violation

Higgs boson h_2

Influence of $\tan\beta$ and systematics in Φ_{HA} measurement ($M_{H_2} = 300$ GeV, $\Phi_{HA} = 0$)

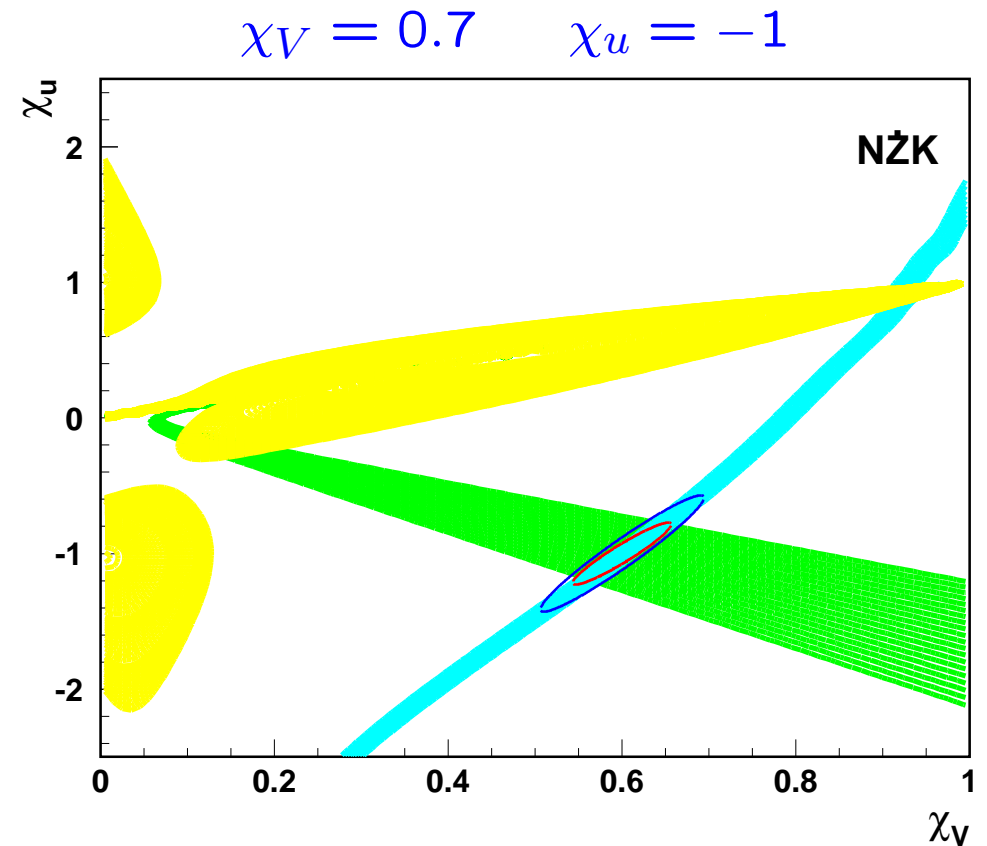
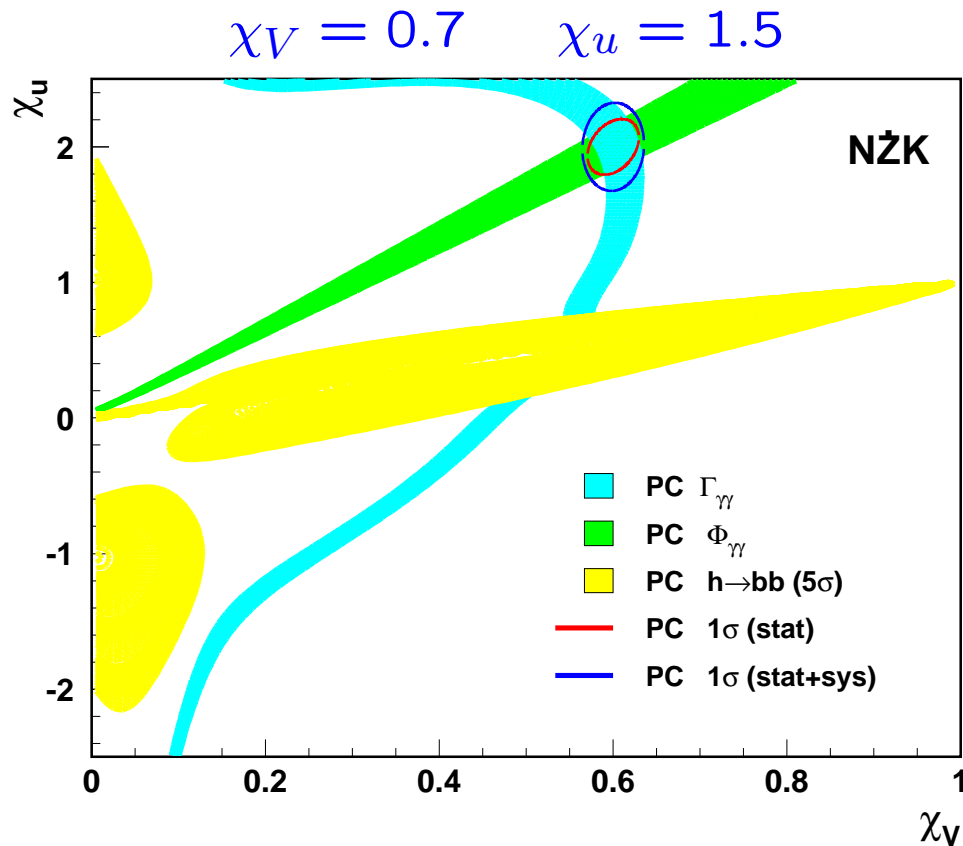
Expected precision in Φ_{HA} determination stat. + sys. errors from $\tan\beta$ and Φ_{HA} fit



CP violating H–A mixing can be precisely measured if $\tan\beta$ is not too large

Photon Collider

Combined fit to W^+W^- and ZZ invariant mass distributions $\Rightarrow \Gamma_{\gamma\gamma}$ and $\phi_{\gamma\gamma}$
 \Rightarrow couplings to both vector bosons (χ_V) and up fermions (χ_u) can be determined
 1σ contours for 1 year of PC running, $M_H = 250$ GeV



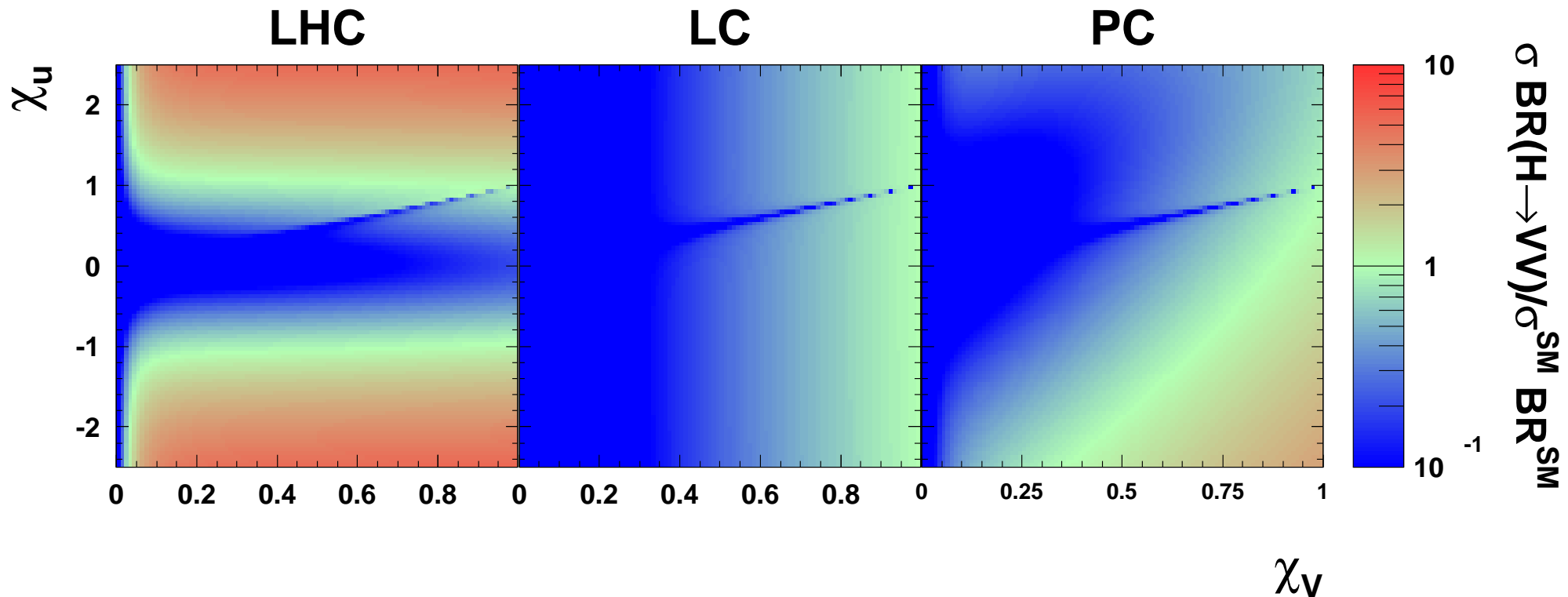
Systematic uncertainties affect mainly $\phi_{\gamma\gamma}$ measurement !

LHC ⊕ LC ⊕ PC

Measurements at LHC, LC and Photon Collider are complementary, being sensitive to different combinations of Higgs-boson couplings

Cross sections × BR relative to SM

$M_H = 250 GeV$



LHC ⊕ LC ⊕ PC

Allowed coupling values from **cross section** measurements at **LHC**, **LC** and **PC**, and the phase measurement at **PC**.

Inconsistency would indicate “**new physics**”:

- different **coupling structure** or
- existence of **new heavy particles** contributing to Γ_{gg} and $\Gamma_{\gamma\gamma}$

Results for 2HDM (II) with **weak CP violation**: **NŻK**

