

Metody eksperymentalne w fizyce wysokich energii

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Zakład Cząstek i Oddziaływań Fundamentalnych IFD

Wykład XIV

- Pomiar przekroju czynnego
- ⇒ przekrój całkowity
- ⇒ przekrój różniczkowy

Cross Section: Experimentally

Number of observed events: counted

Background:
Measured from data /
calculated from theory

$$\sigma = \frac{N_{\text{obs}} - N_{\text{BG}}}{\int L dt \cdot \epsilon}$$

Cross section σ

Luminosity:
Determined by accelerator,
trigger prescale, ...

Efficiency:
optimized by
experimentalist

Includes acceptance due to kinematics, geometry, cuts etc.

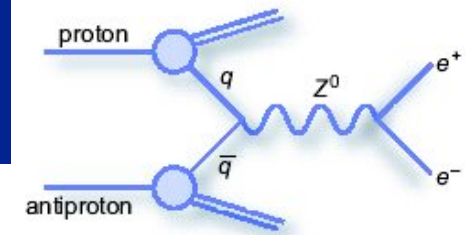
Acceptance / Efficiency

- Actually rather complex:
 - Many ingredients enter here
 - You need to know:

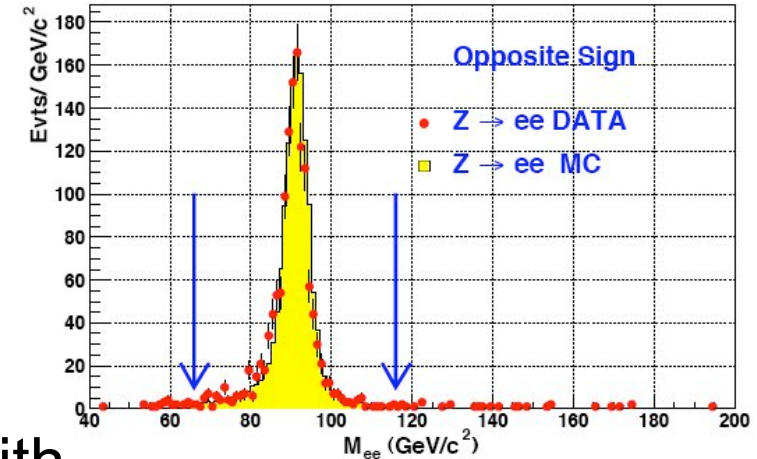
$$\epsilon_{\text{total}} = \frac{\text{Number of Events used in Analysis}}{\text{Number of Events Produced}}$$

- Ingredients:
 - Trigger efficiency
 - Identification efficiency
 - Kinematic acceptance
 - Cut efficiencies
- Using three example measurements for illustration:
 - Z boson, top quark and jet cross sections

Z Boson Cross Section



- Trigger requires one electron with $E_T > 20$ GeV
 - Criteria at L1, L2 and L3/EventFilter
- You select two electrons in the analysis
 - With certain quality criteria
 - With an isolation requirement
 - With $E_T > 25$ GeV and $|\eta| < 2.5$
 - With oppositely charged tracks with $p_T > 10$ GeV
- You require the di-electron mass to be near the Z:
 - $66 < M(\text{ll}) < 116$ GeV



$$\Rightarrow \epsilon_{\text{total}} = \epsilon_{\text{trig}} \epsilon_{\text{rec}} \epsilon_{\text{ID}} \epsilon_{\text{kin}} \epsilon_{\text{track}}$$

Uncertainty on Cross Section

- You will want to minimize the uncertainty:

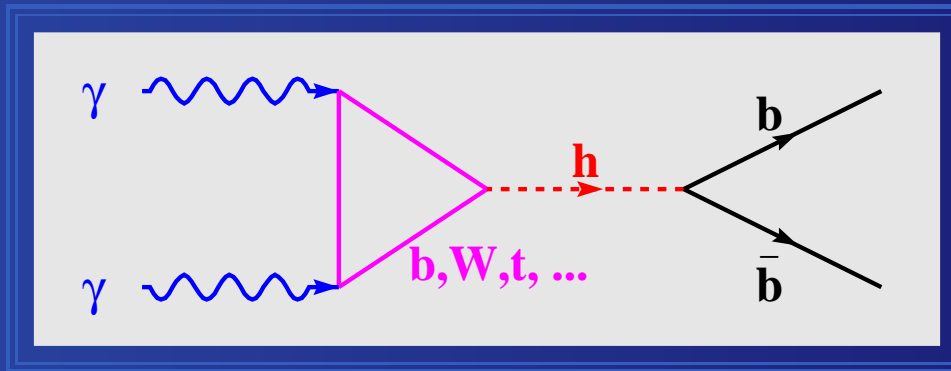
$$\frac{\delta\sigma}{\sigma} = \sqrt{\frac{\delta N_{obs}^2 + \delta N_{BG}^2}{(N_{obs} - N_{BG})^2} + \left(\frac{\delta\mathcal{L}}{\mathcal{L}}\right)^2 + \left(\frac{\delta\epsilon}{\epsilon}\right)^2}$$

- Thus you need:
 - $N_{obs} - N_{BG}$ small (i.e. N_{signal} large)
 - Optimize selection for large acceptance and small background
 - Uncertainties on efficiency and background small
 - Hard work you have to do
 - Uncertainty on luminosity small
 - Usually not directly in your power

$$m_h \approx 120 \text{ GeV}$$

Process: $\gamma + \gamma \rightarrow h \rightarrow b + \bar{b}$

$$J_z = 0$$



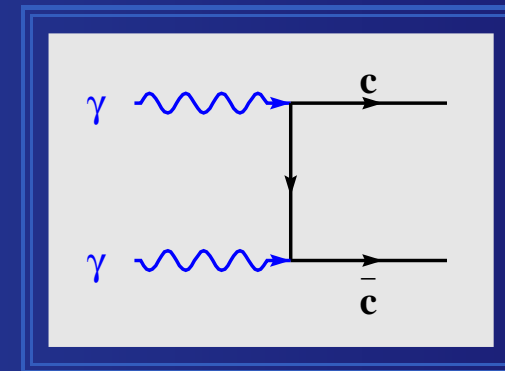
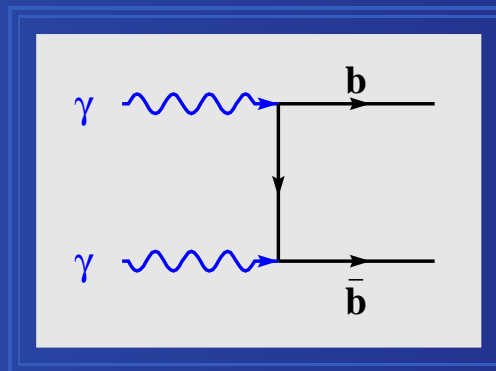
“Hard” background:

- $\gamma + \gamma \rightarrow b + \bar{b}$

- $\gamma + \gamma \rightarrow c + \bar{c}$

$$\sigma \propto Q_q^4$$

$$\sigma^{LO}(|J_z| = 2) \gg \sigma^{LO}(J_z = 0)$$



Other background:

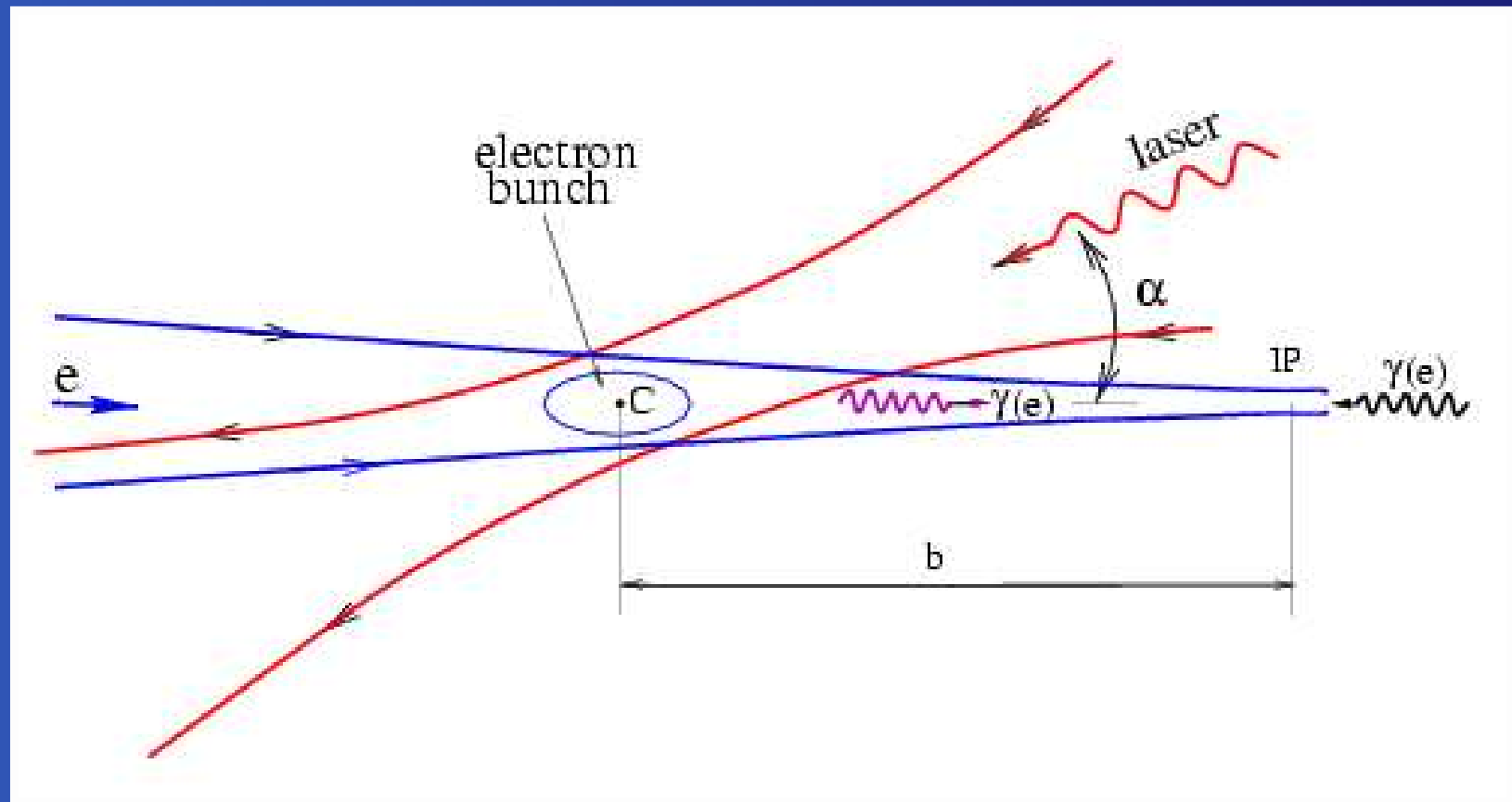
- Resolved photon(s) interactions $\gamma + \gamma \rightarrow X + Q + \bar{Q}$

- Overlaying events

(high intensity of photon-beams in the low-energy part of the spectrum)

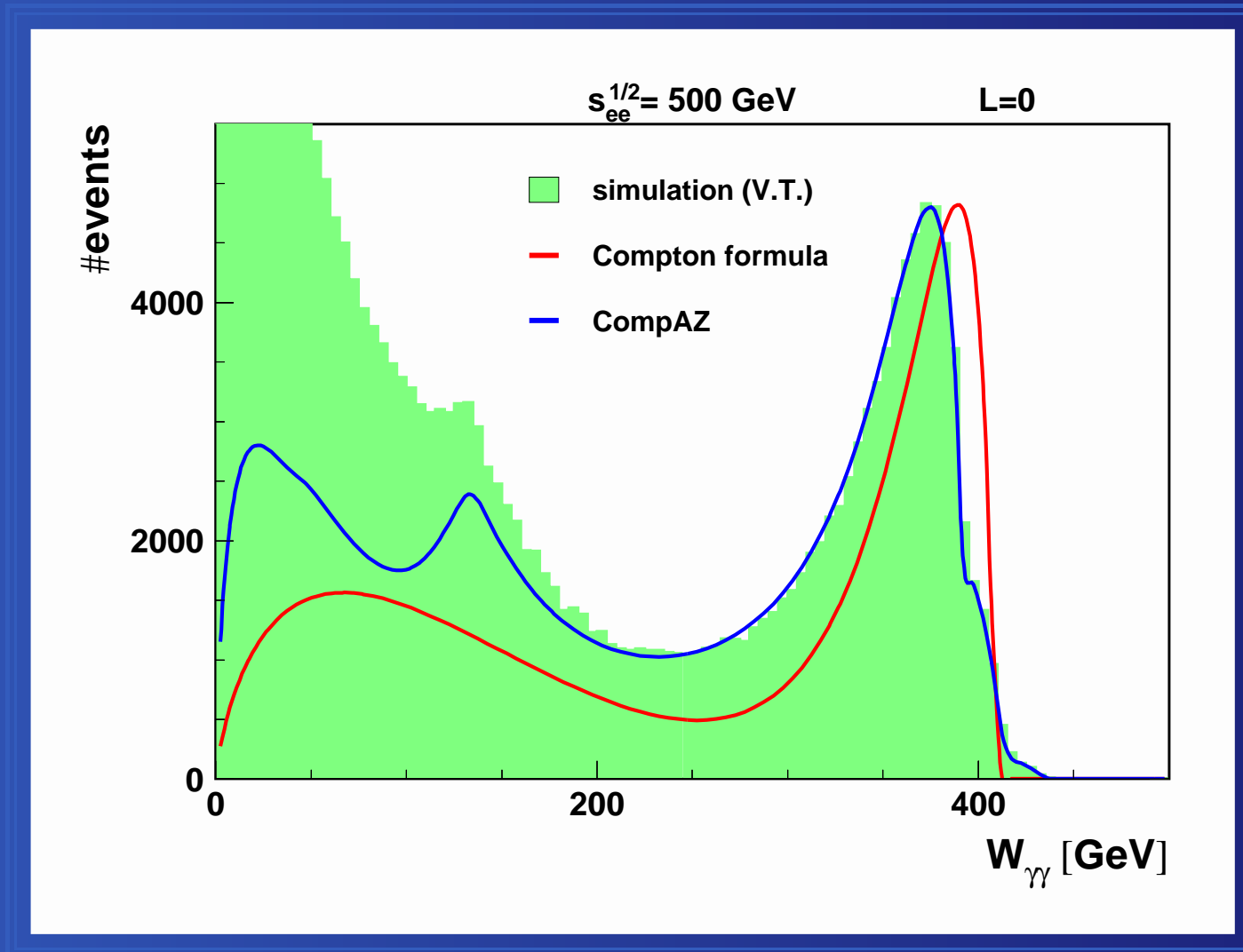
Photon Collider

High-energy photons obtained in the Compton back-scattering



Photon Collider

$\gamma\gamma$ -luminosity spectrum



Generation & Simulation. Selection.

Photon-photon spectrum: CompAZ

Signal: HDECAY, PYTHIA

Background: program by G. Jikia

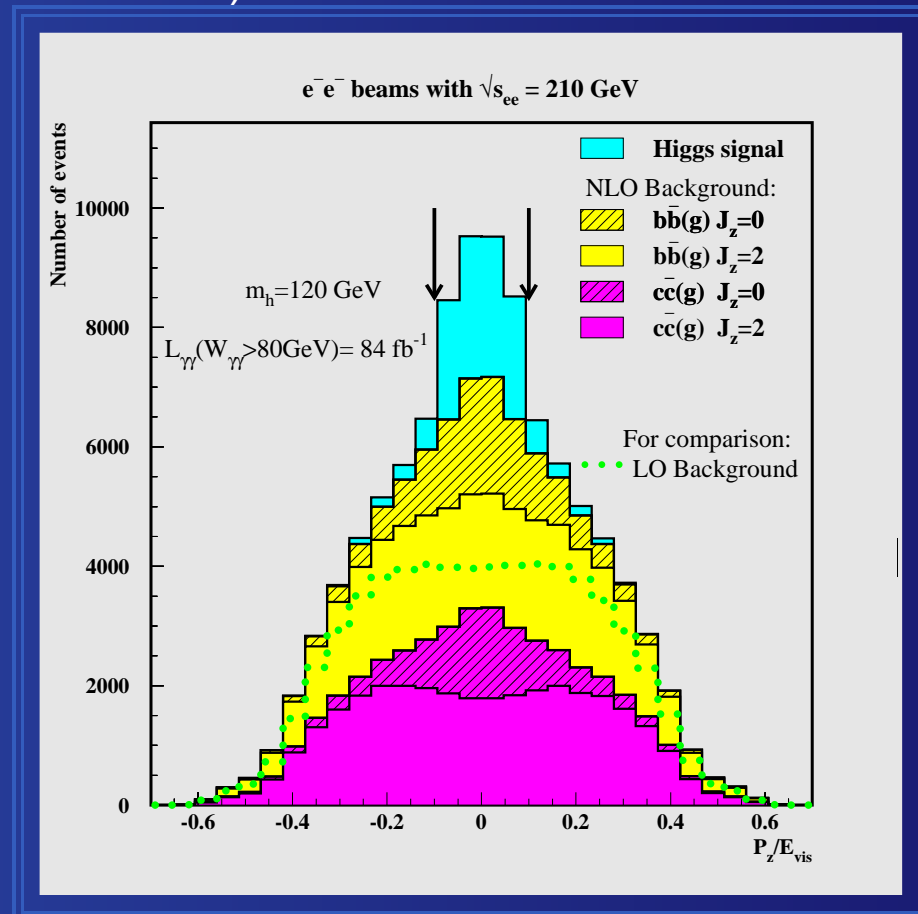
Fragmentation: Lund in PYTHIA

Detector performance: SIMDET (parametric simulation)

Jets: Durham algorithm with $y_{cut} = 0.02$

Selection of $b\bar{b}$ events:

- 1) Assumed bb-tagging and mistagging
- 2) Using ZVTOP-B-Hadron-Tagger
- $E_{vis} > 90$ GeV
- $N_{jets} = 2, 3$
- $|P_z|/E_{vis} < 0.1$

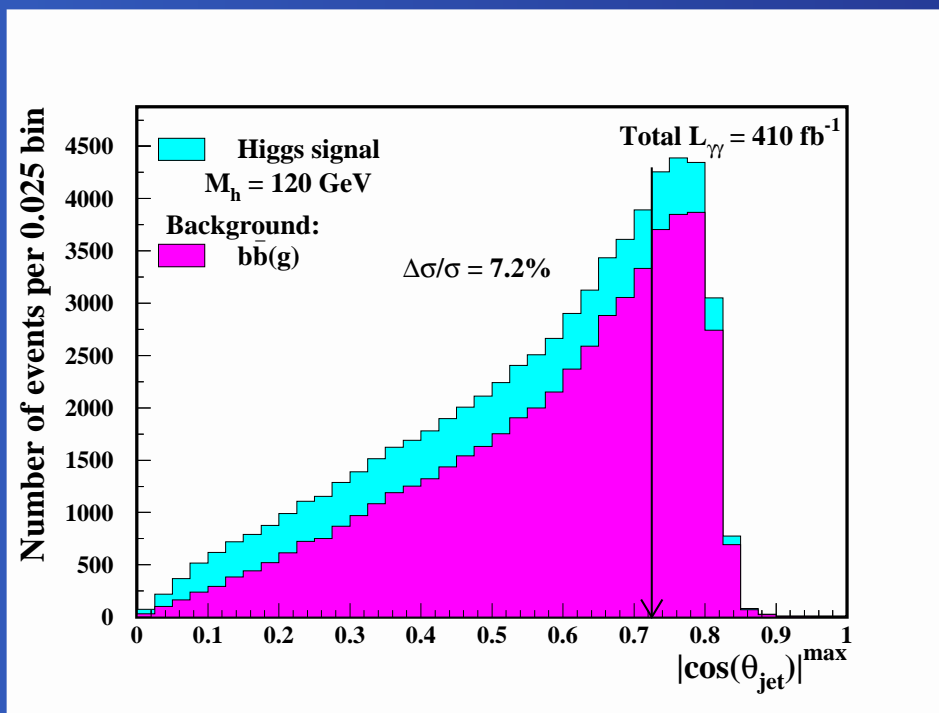


Cuts

Cuts optimized by minimizing:

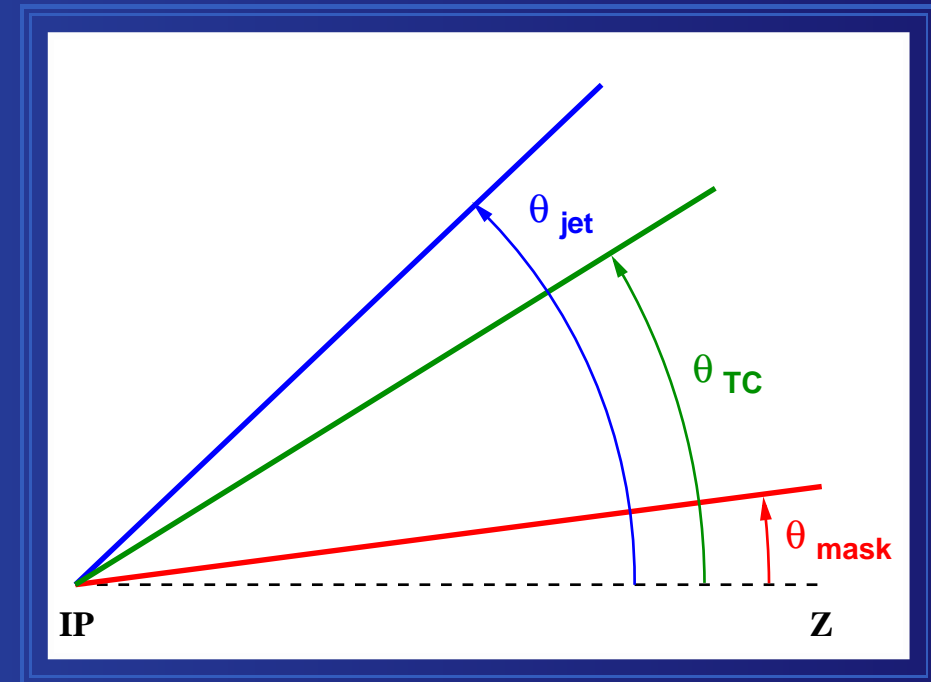
$$\frac{\Delta\sigma(\gamma\gamma \rightarrow h \rightarrow b\bar{b})}{\sigma(\gamma\gamma \rightarrow h \rightarrow b\bar{b})} = \frac{\sqrt{\mu_S + \mu_B}}{\mu_S},$$

For example:



Maximal value of $|\cos \theta_{jet}|$
over all jets in the event

All angular cuts



Detector mask

Particles on Pythia level: $\cos \theta_{mask} \approx 0.99$

OE suppression

Tracks & clusters: $\cos \theta_{TC} = 0.85$

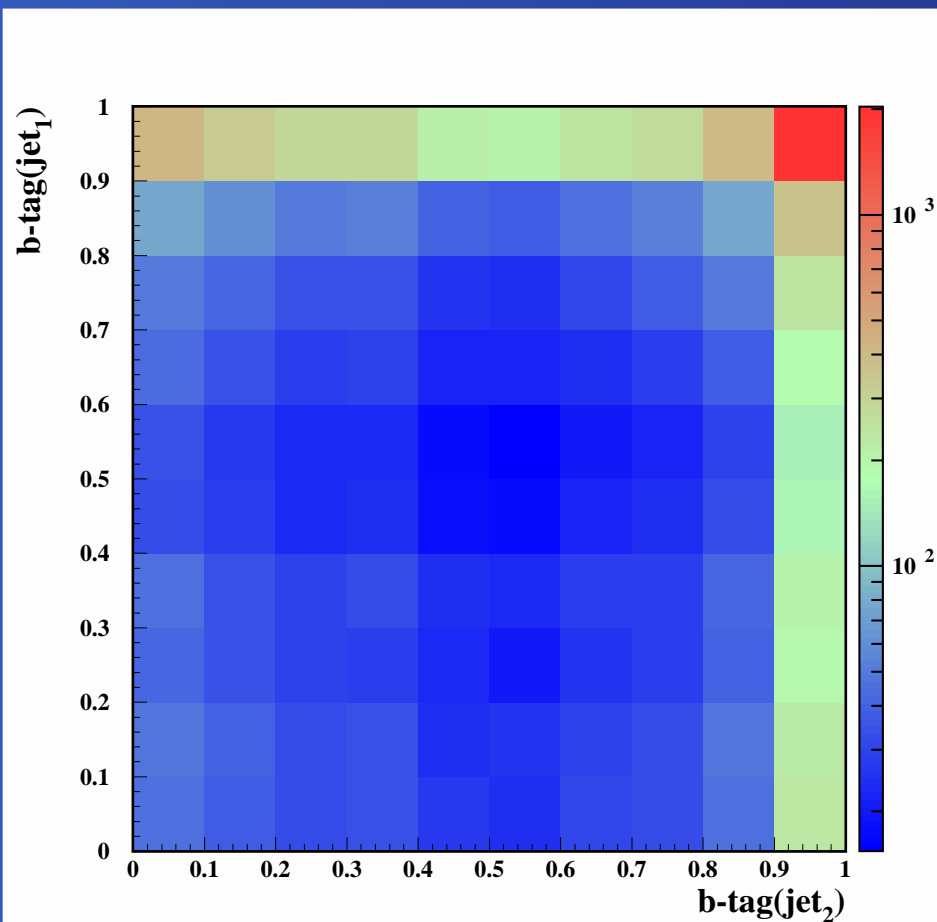
$\gamma\gamma \rightarrow Q\bar{Q}(g)$ suppression

Jets: $|\cos \theta_{jet}|^{\max} = 0.725$

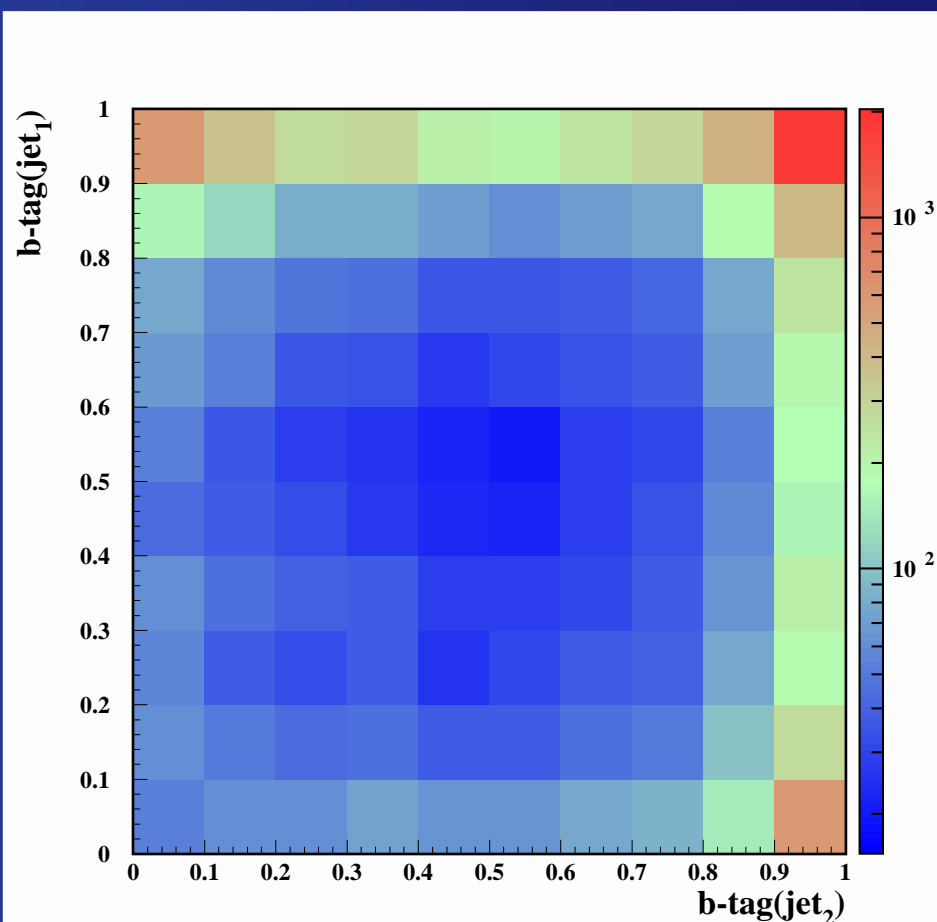


$b\bar{b}$ -tagging

$$\gamma\gamma \rightarrow h \rightarrow b\bar{b}$$



$$\gamma\gamma \rightarrow b\bar{b}(g)$$

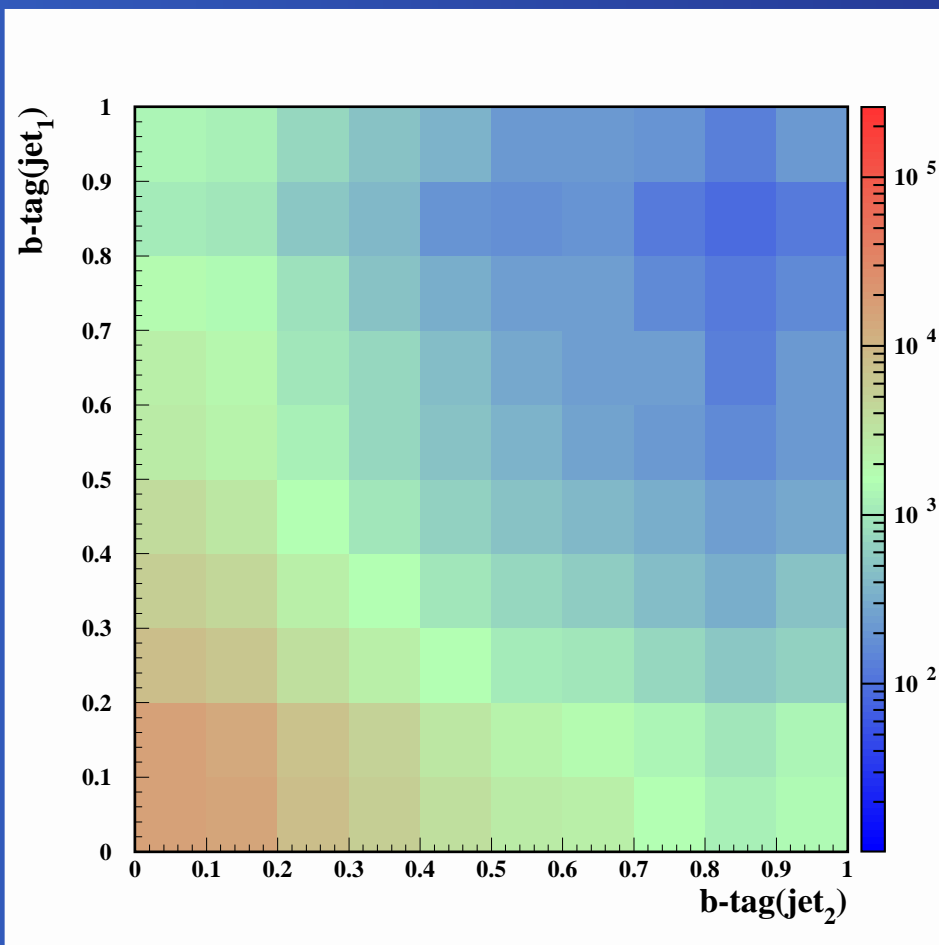


$J_z = 0$ suppressed for $b\bar{b}$
 \Rightarrow hard g -jet with low b -tag

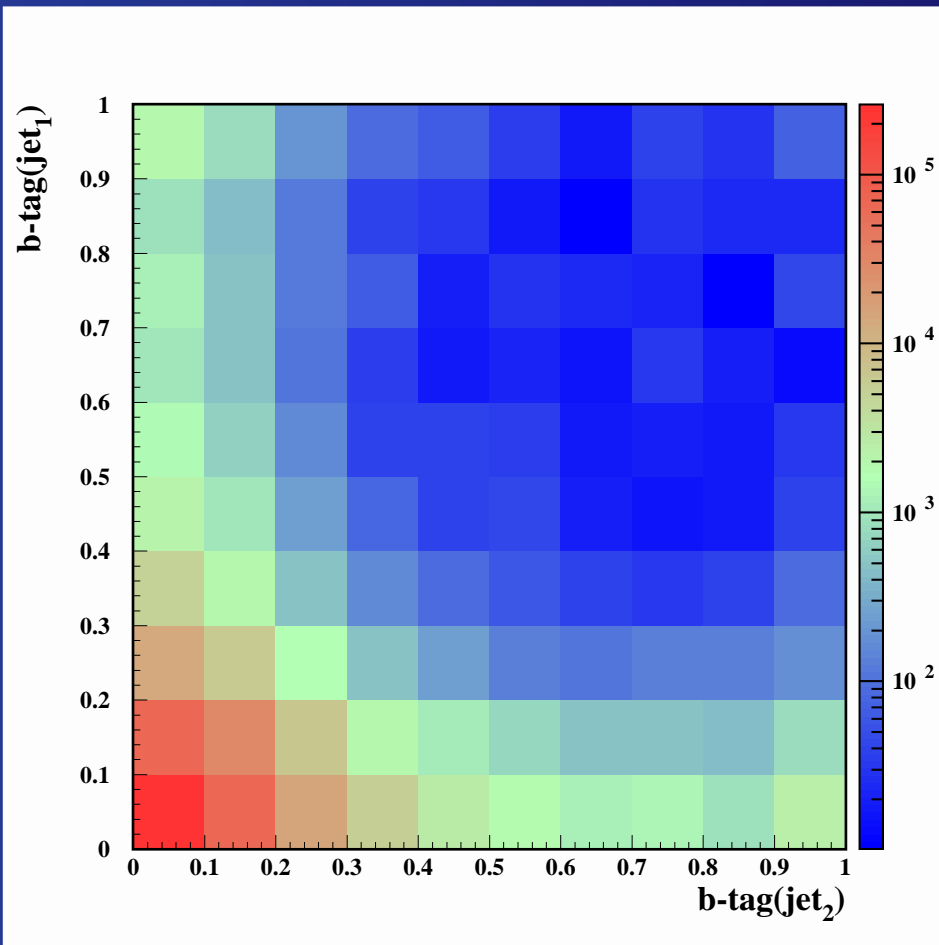


$b\bar{b}$ -tagging

$$\gamma\gamma \rightarrow c\bar{c}(g)$$



$$\gamma\gamma \rightarrow q\bar{q} \quad (q = u, d, s)$$

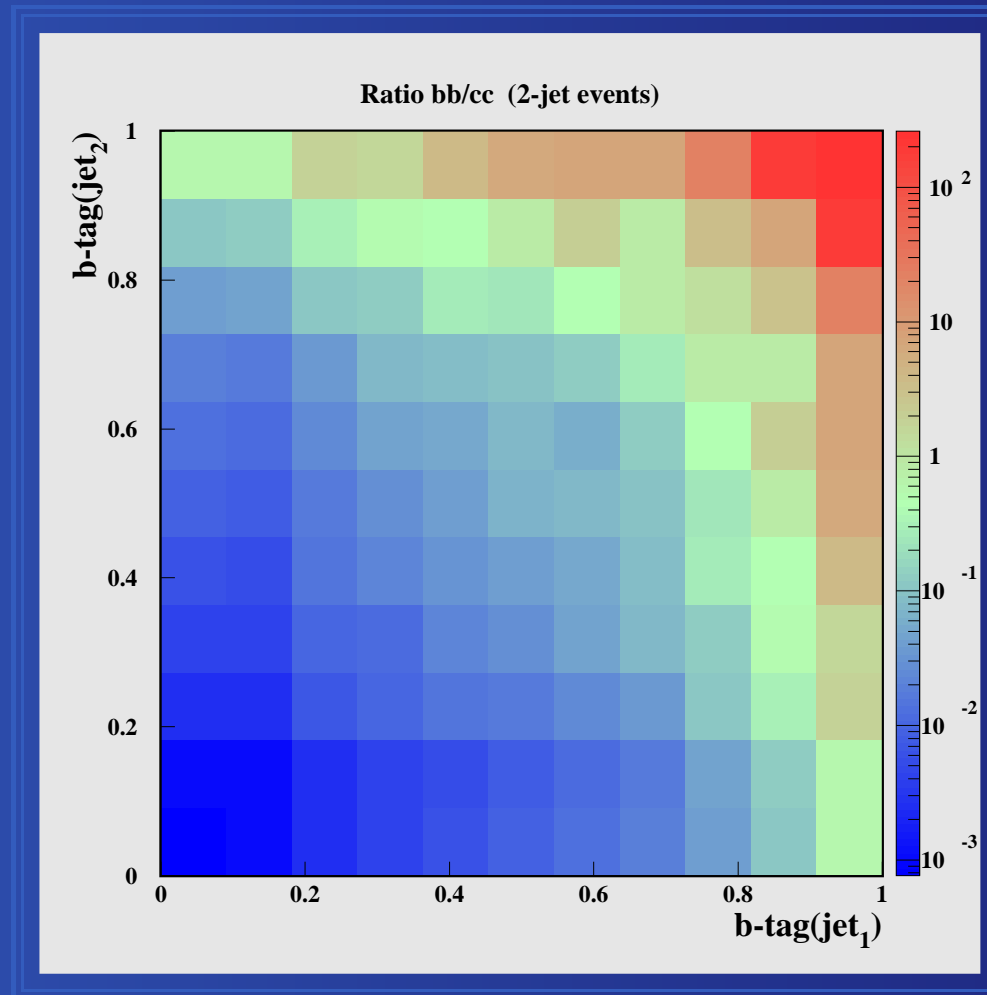


Significant fraction mistagged
 \Rightarrow double b -tag



B-tagging

ZVTOP-B-Hadron-Tagger



$$\frac{S}{B} = \frac{\#(\gamma\gamma \rightarrow b\bar{b})}{\#(\gamma\gamma \rightarrow c\bar{c})}$$



higgs-tagging at $M_h = 120 \text{ GeV}$

higgs-tagging: a cut on the ratio
of $\gamma\gamma \rightarrow h \rightarrow b\bar{b}$

to $\gamma\gamma \rightarrow b\bar{b}(g), c\bar{c}(g)$ events

$\Rightarrow \varepsilon_{higgs} = 70 \%$

$\varepsilon_{bb} = 66\%, \varepsilon_{cc} = 4\%$

Earlier we used *b*-tagging:

a cut on the ratio

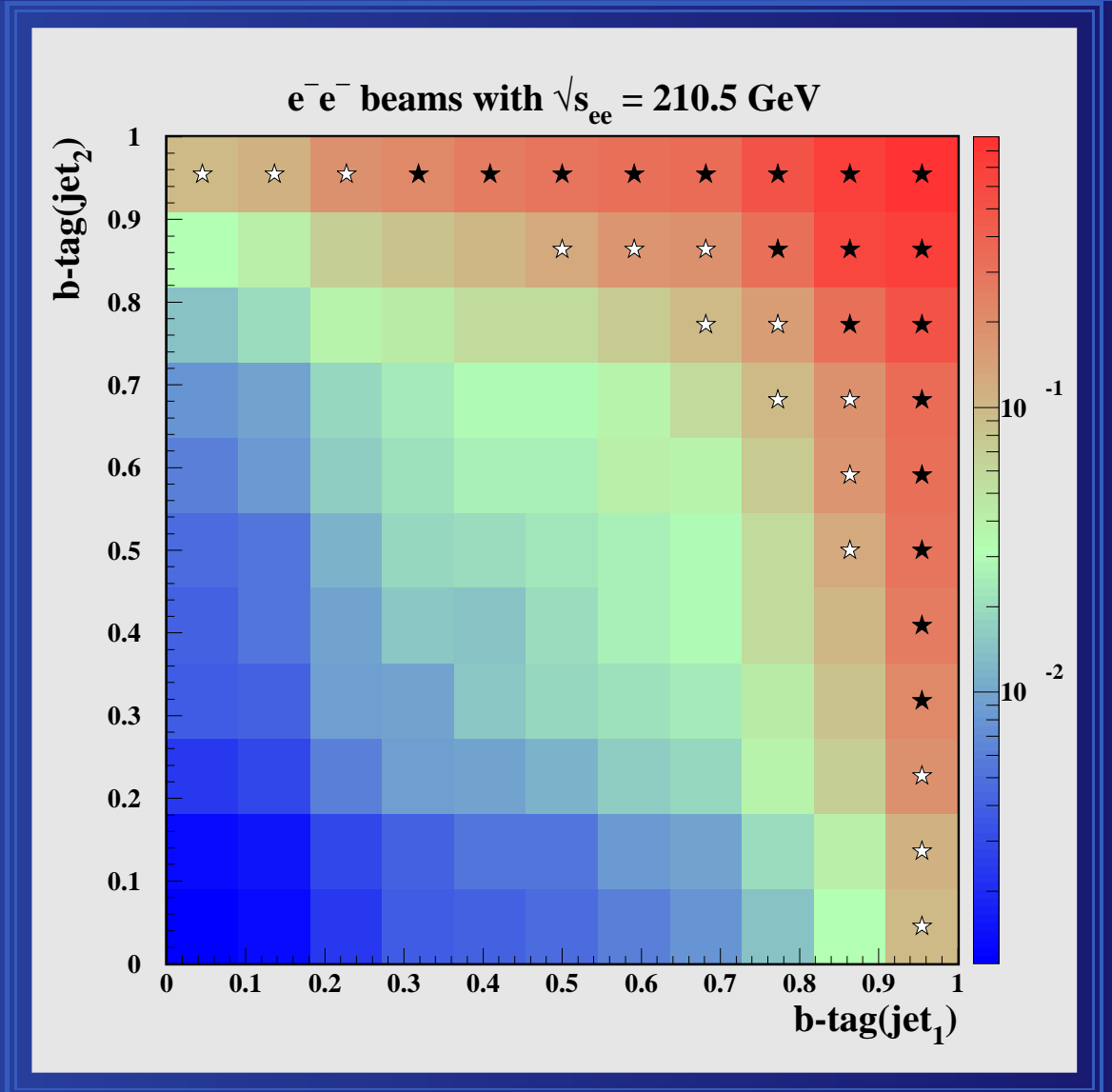
of $\gamma\gamma \rightarrow b\bar{b}(g)$

to $\gamma\gamma \rightarrow c\bar{c}(g)$ events

$\Rightarrow \varepsilon_{higgs} = 85 \%$

$\varepsilon_{bb} = 82\%, \varepsilon_{cc} = 2\%$

Tighter cuts are needed
due to OE contribution

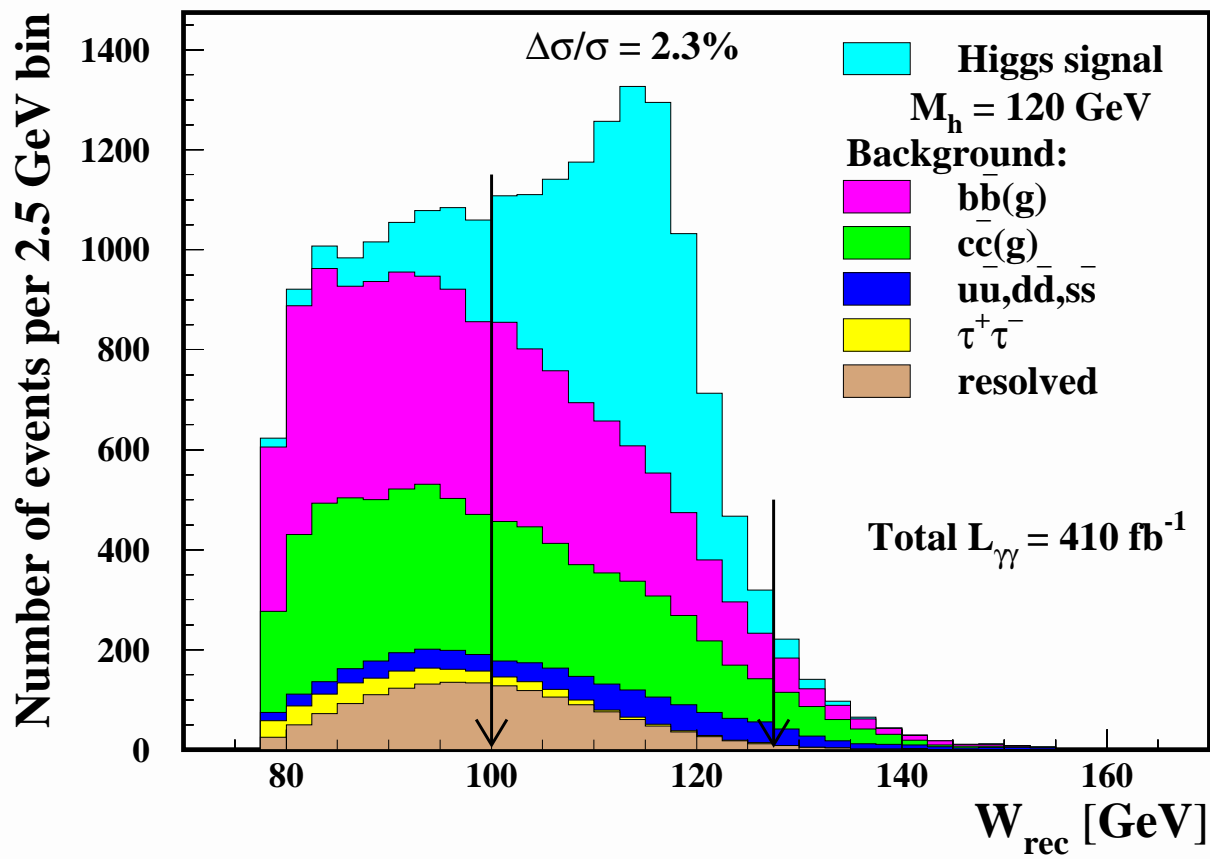


Black stars – optimized selection

Black+white stars – analysis without OE

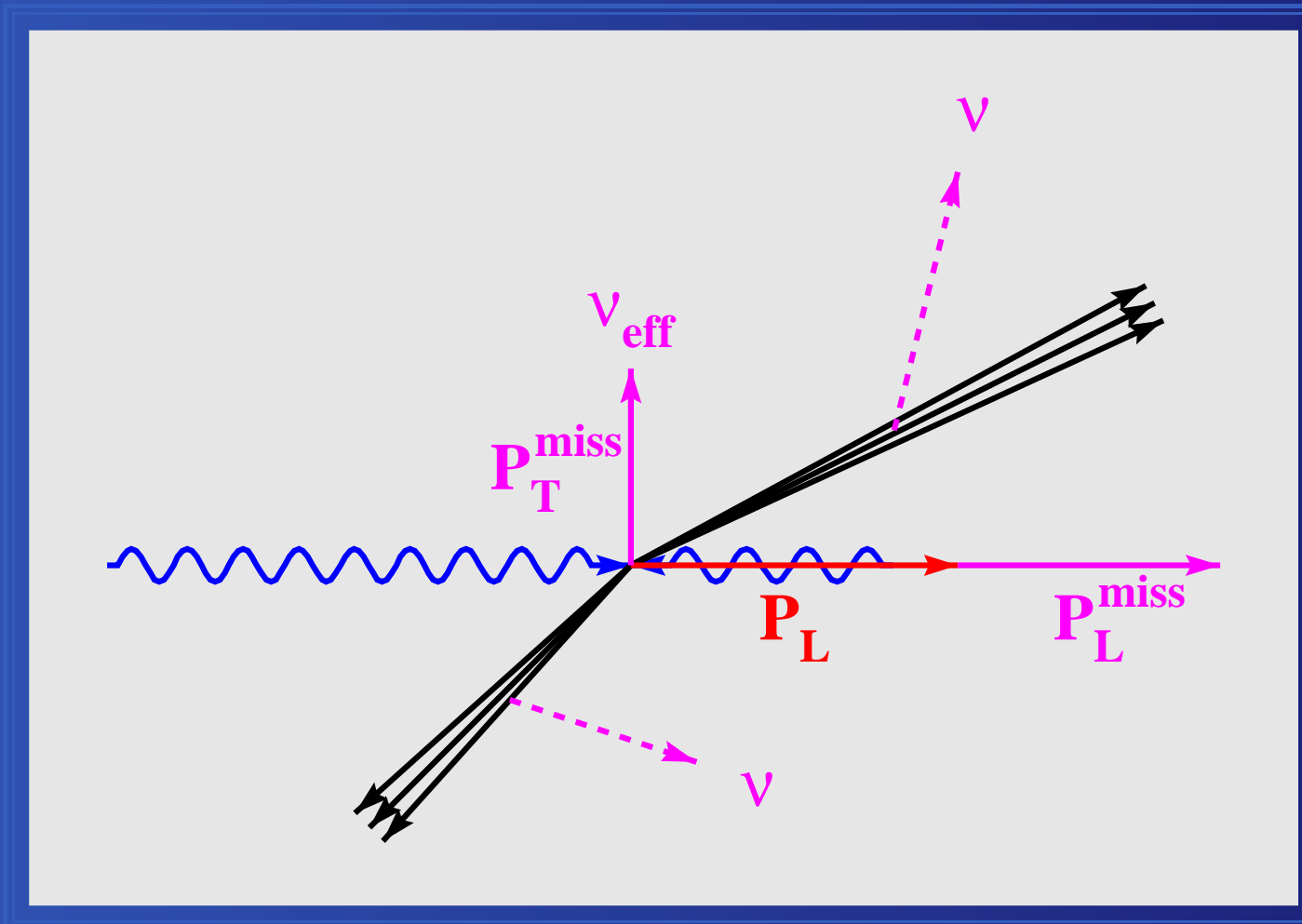
SM, $M_h = 120 \text{ GeV}$

Final results



Missing P_T

Neutrinos from semileptonic decays of D - and B -mesons.

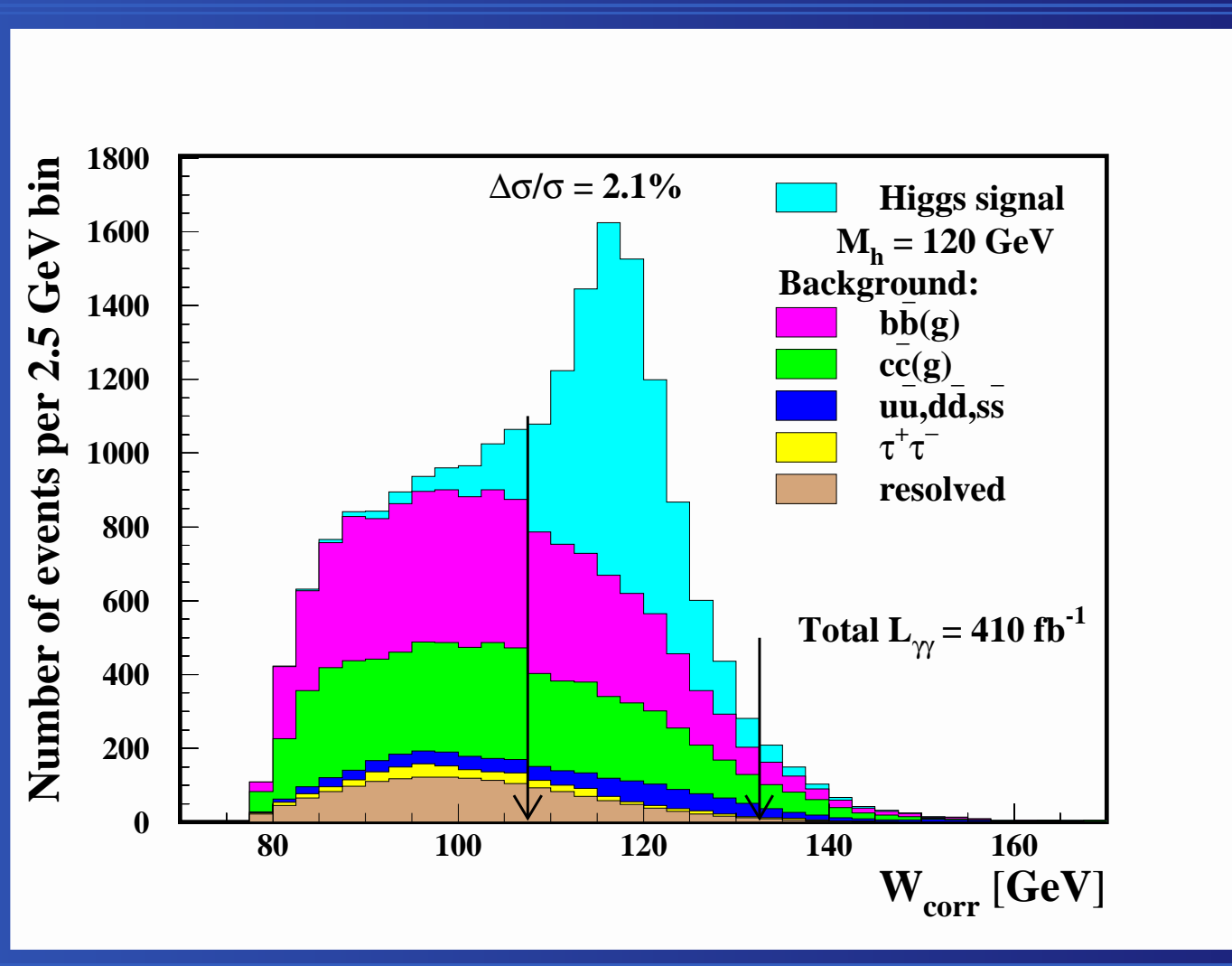


$$W_{\text{corr}} \equiv \sqrt{W_{\text{rec}}^2 + 2P_T(E_{\text{vis}} + P_T)}$$



SM, $M_h = 120 \text{ GeV}$

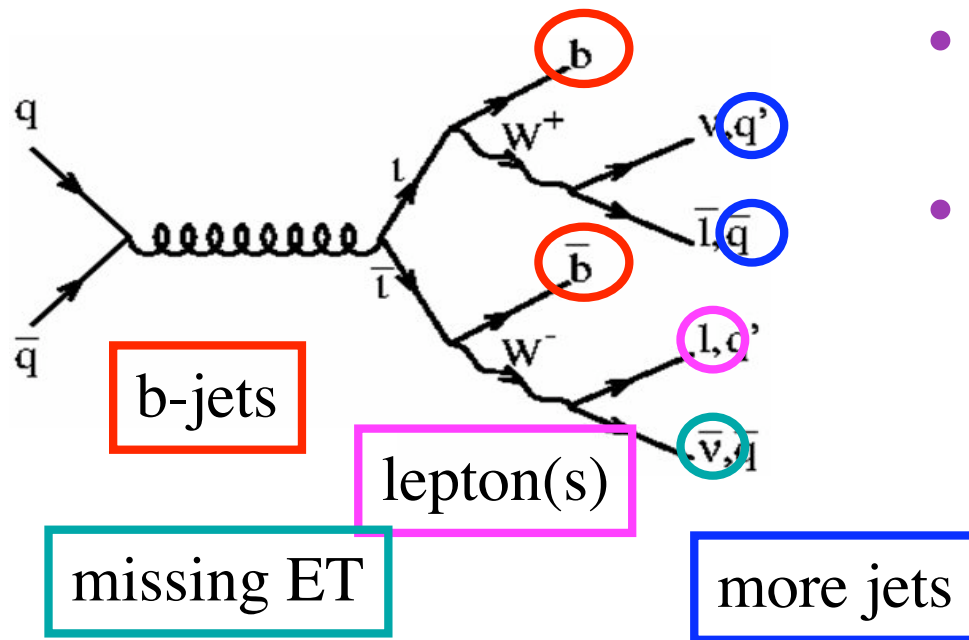
Final results



Top Quark Cross Section

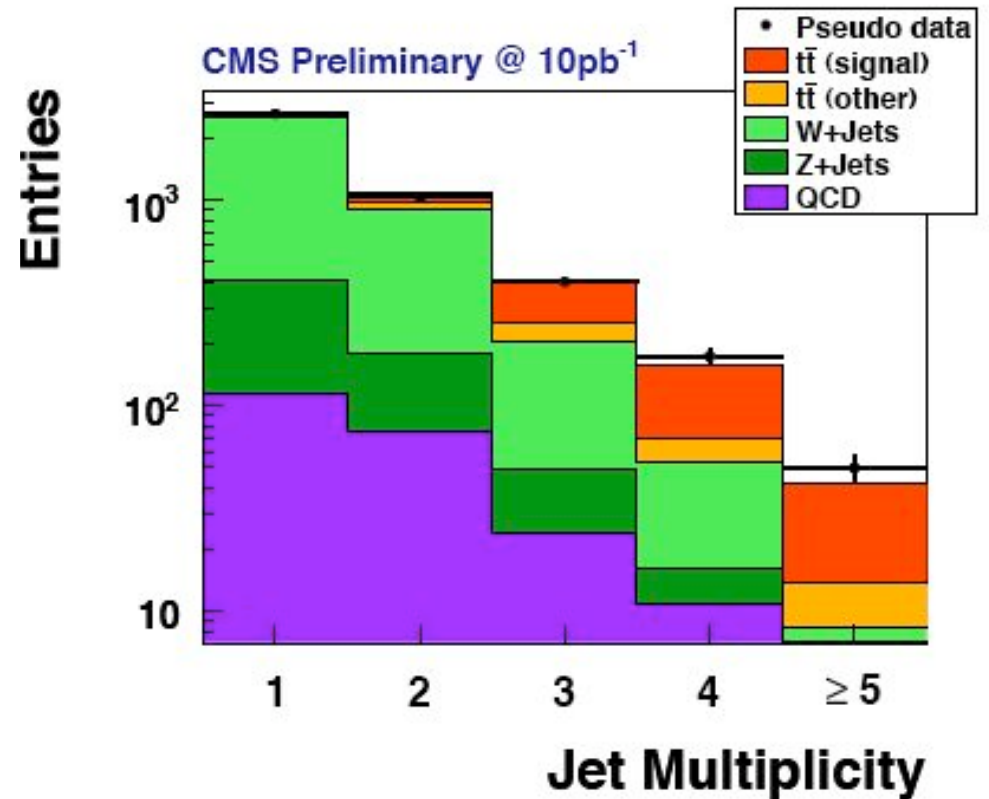
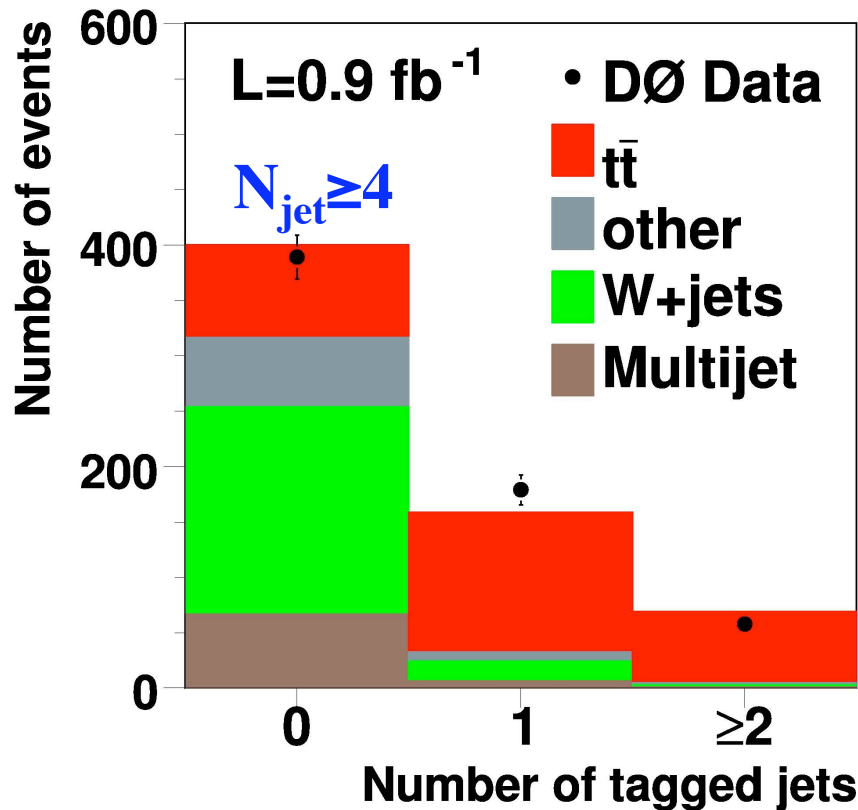
SM: $t\bar{t}$ pair production, $\text{Br}(t \rightarrow bW) = 100\%$, $\text{Br}(W \rightarrow l\nu) = 1/9 = 11\%$

dilepton	(4/81)	2 leptons + 2 jets + missing E_T
lepton+jets	(24/81)	1 lepton + 4 jets + missing E_T
fully hadronic	(36/81)	6 jets



- Trigger on electron/muon
 - Like for Z's
- Analysis cuts:
 - Electron/muon $p_T > 25$ GeV
 - Missing $E_T > 25$ GeV
 - 3 or 4 jets with $E_T > 20-40$ GeV

Finding the Top Quark



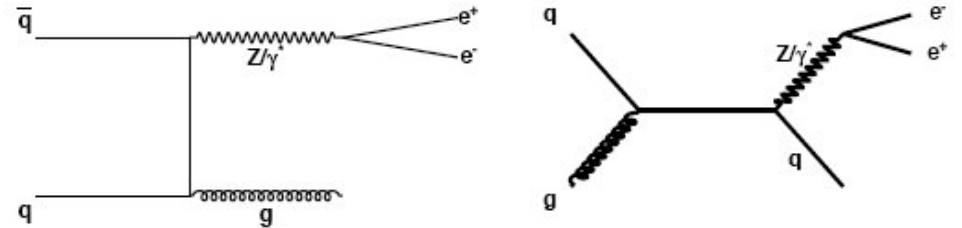
- **Tevatron**
 - Top is overwhelmed by backgrounds:
 - Top fraction is only 10% (≥ 3 jets) or 40% (≥ 4 jets)
 - Use b-jets to purify sample => purity 50% (≥ 3 jets) or 80% (≥ 4 jets)
- **LHC**
 - Purity $\sim 70\%$ w/o b-tagging (90% w b-tagging)

Systematic uncertainties

- This will likely be $>90\%$ of the work
- **Systematic errors cover our lack of knowledge**
 - need to be determined on every aspect of measurement by varying assumptions *within sensible reasoning*
 - Thus there is no “correct way”:
 - But there are good ways and bad ways
 - You will need to develop a feeling and discuss with colleagues / conveners / theorists
 - There is a lot of room for creativity here!
- What’s better? Overestimate or underestimate
 - Find New Physics:
 - it’s fine to be generous with the systematics
 - You want to be really sure you found new physics and not that “Pythia doesn’t work”
 - Precision measurement
 - Need to make best effort to neither overestimate nor underestimate!

QCD Modeling of Process

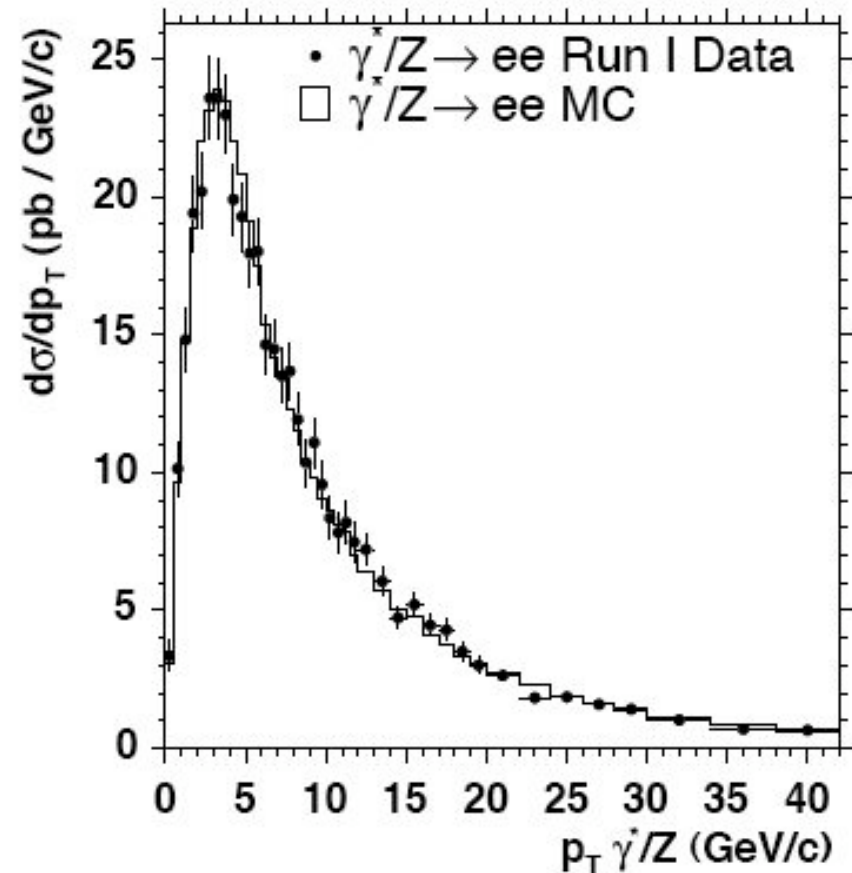
- Kinematics affected by p_T of Z boson
 - Determined by soft and hard QCD radiation
 - tune MC to describe data
- Limitations of Leading Order Monte Carlo
 - Compare to NNLO calculation



CDF

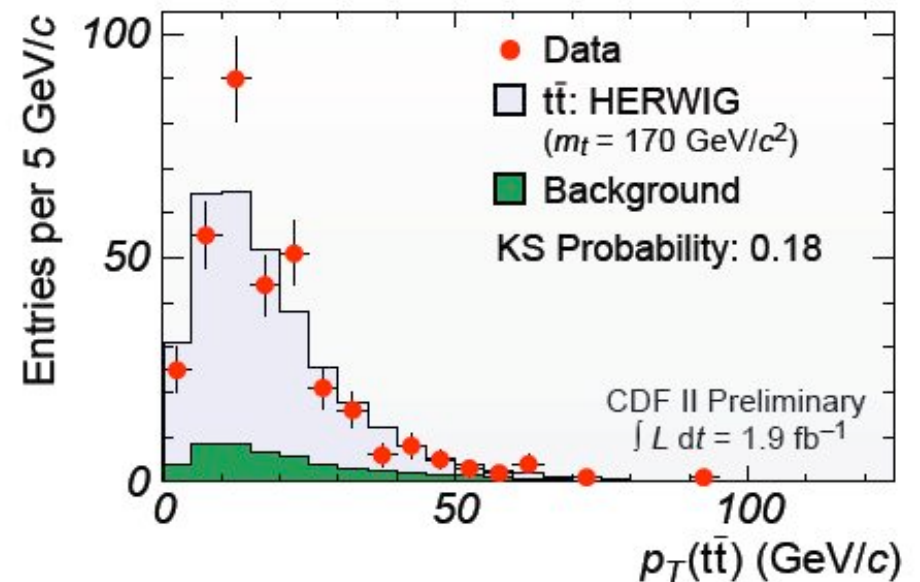
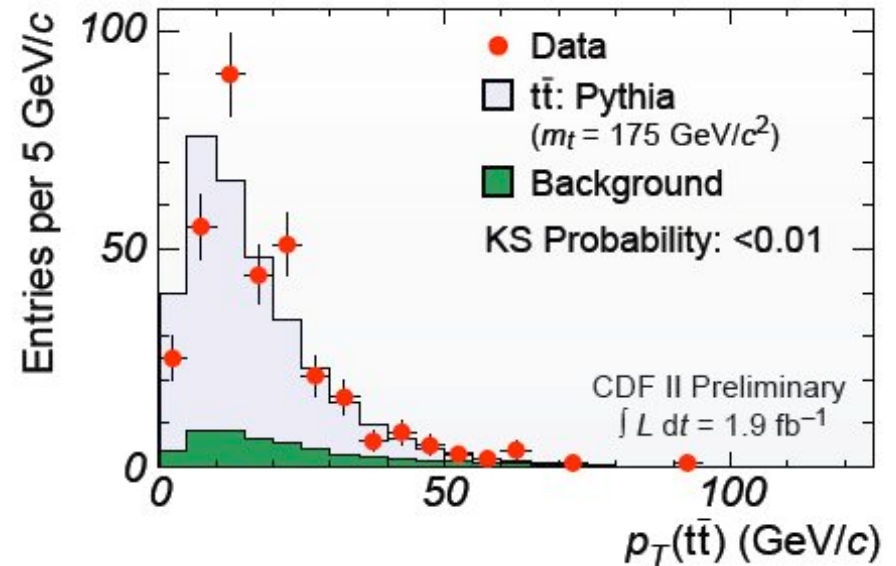
TABLE XII: Central acceptance values for our candidate samples based on $d\sigma/dy$ distributions obtained from both NNLO and PYTHIA simulation.

Acceptance	NNLO Calc.	PYTHIA	Difference (%)
$A_{W \rightarrow \mu\nu}$	0.1970	0.1967	+0.15
$A_{W \rightarrow e\nu}$	0.2397	0.2395	+0.08
$A_{Z \rightarrow \mu\mu}$	0.1392	0.1387	+0.36
$A_{Z \rightarrow ee}$	0.3182	0.3185	-0.09
$A_{Z \rightarrow \mu\mu} / A_{W \rightarrow \mu\nu}$	0.7066	0.7054	+0.17
$A_{Z \rightarrow ee} / A_{W \rightarrow e\nu}$	1.3272	1.3299	-0.20

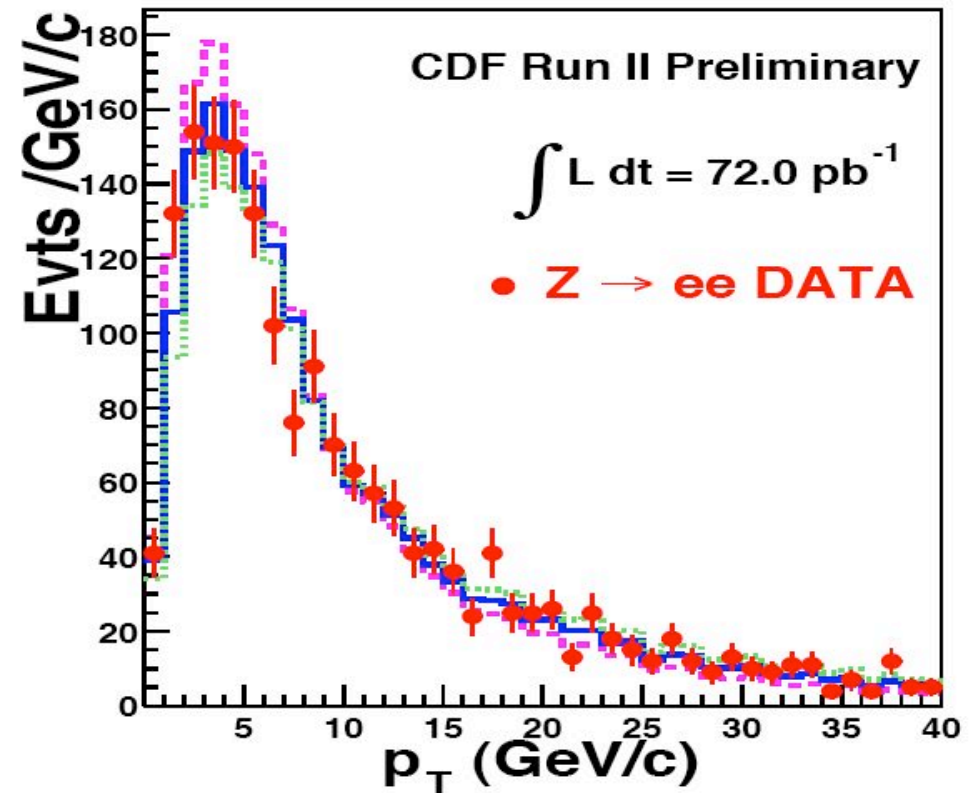
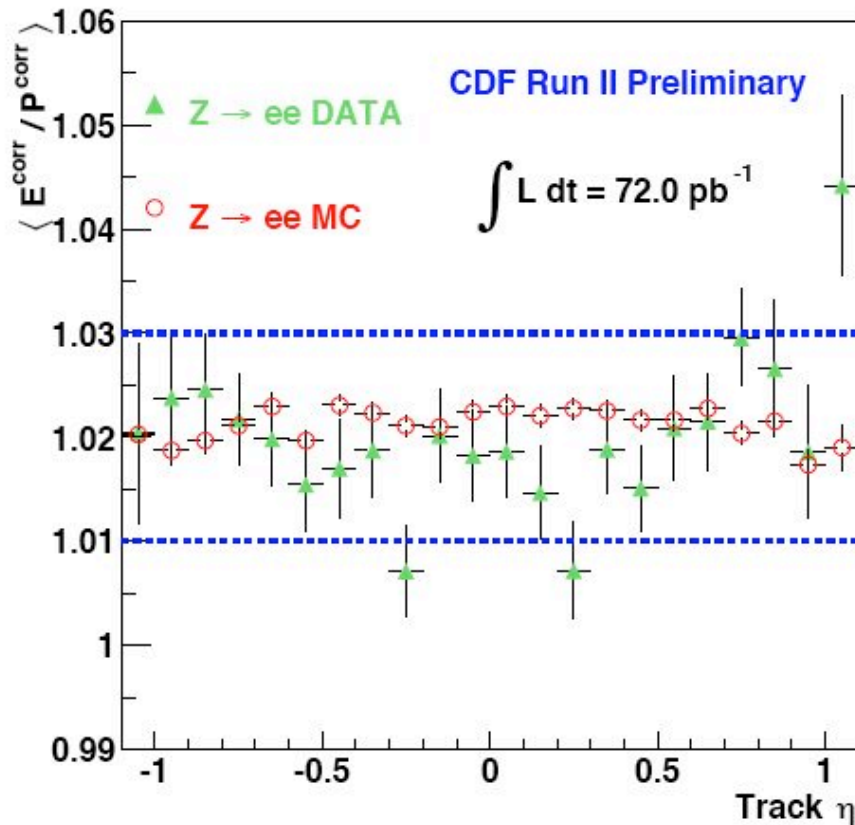


MC Modeling of top

- Use different MC generators
 - Pythia
 - Herwig
 - Alpgen
 - MC @ NLO
 - ...
- Different tunes
 - Underlying event
 - Initial/final state QCD radiation
 - ...
- Make many plots
 - Check if data are modelled well



Examples for Systematic Errors



- Mostly driven by comparison of data and MC
 - Systematic uncertainty determined by (dis)agreement and statistical uncertainties on data

Systematic Uncertainties: Z and top

Z cross section (not all systematics)

source	variation	ΔA_Z	$\Delta A_Z / A_Z$
E_T^e scale	1% variation	0.03%	0.3%
E_T^e resolution	2% extra smearing	0.02%	0.2%
p_T^e scale	1% variation	0.01%	0.1%
p_T modelling		0.01%	0.1%
Material	5.5 % X_0	0.54%	4.7%
PDFs	reweighting of y	0.34%	2.9%
overall		0.64%	5.5%

top cross section

Systematic	Inclusive (Tight)	Double (Loose)
Lepton ID	1.8	
ISR	0.5	0.2
FSR	0.6	0.6
PDFs	0.9	
Pythia vs. Herwig	2.2	1.1
Luminosity	6.2	
JES	6.1	4.1
<i>b</i> -Tagging	5.8	12.1
<i>c</i> -Tagging	1.1	2.1
<i>l</i> -Tagging	0.3	0.7
Non- <i>W</i>	1.7	1.3
<i>W</i> +HF Fractions	3.3	2.0
Mistag Matrix	1.0	0.3
Total	11.5	14.8

- Relative importance and evaluation methods of systematic uncertainties are very, very analysis dependent

Final Result: Z cross section

- Now we have everything to calculate the final cross section

TABLE XXXVII: Summary of the input parameters to the $\gamma^*/Z \rightarrow \ell\ell$ cross section calculations for the electron and muon candidate samples.

	$\gamma^*/Z \rightarrow ee$	$\gamma^*/Z \rightarrow \mu\mu$
N_Z^{obs}	4242	1785
N_Z^{bck}	62 ± 18	13 ± 13
A_Z	$0.3182^{+0.0039}_{-0.0041}$	$0.1392^{+0.0027}_{-0.0033}$
ϵ_Z	0.713 ± 0.012	0.713 ± 0.015
$\int \mathcal{L} dt \text{ (pb}^{-1}\text{)}$	72.0 ± 4.3	72.0 ± 4.3

$$\sigma_{\gamma^*/Z} \cdot Br(\gamma^*/Z \rightarrow ee) = 255.8 \pm 3.9(\text{stat.})$$

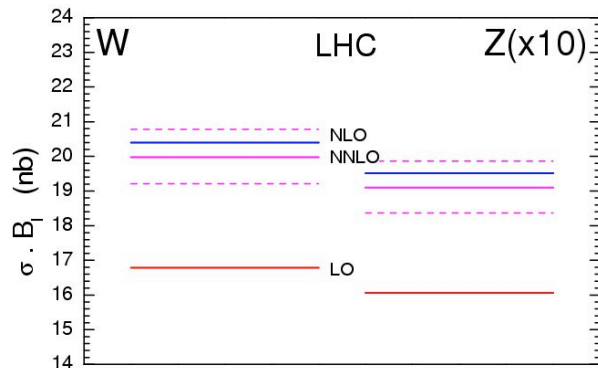
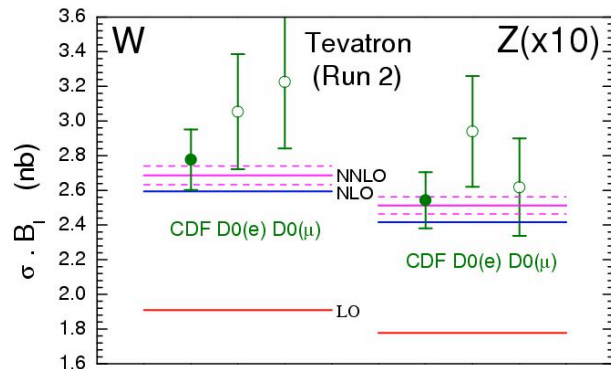
$$\pm 5.5(\text{syst.})$$

$$\pm 15.3(\text{lum.}) \text{ pb}$$

Measurement gets quickly systematically limited

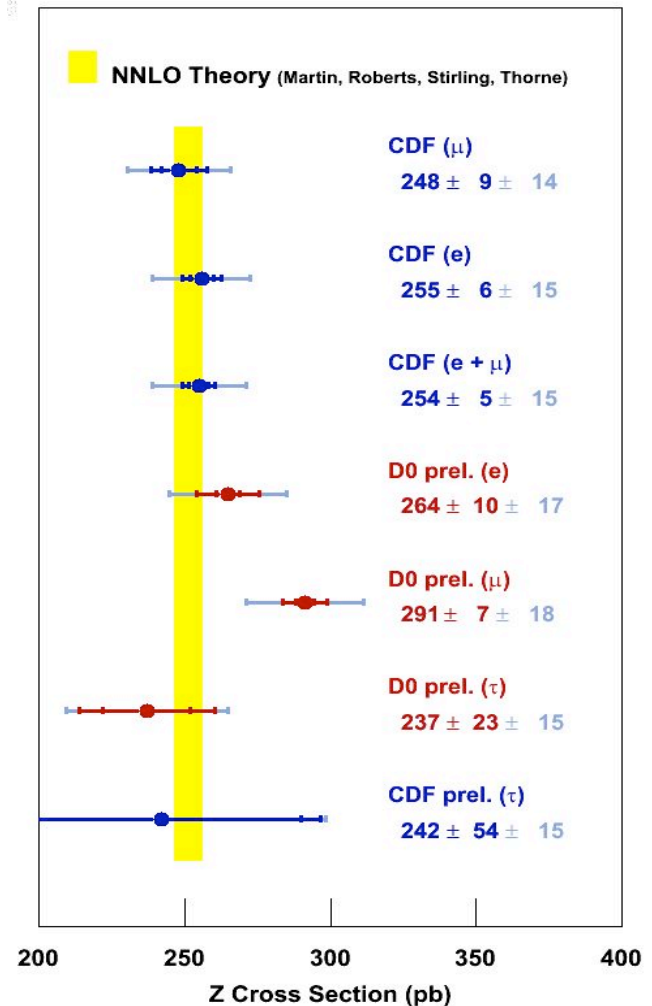
Comparison to Theory

- Experimental uncertainty: ~2%
- Luminosity uncertainty: ~6%
- Theoretical uncertainty: ~2%



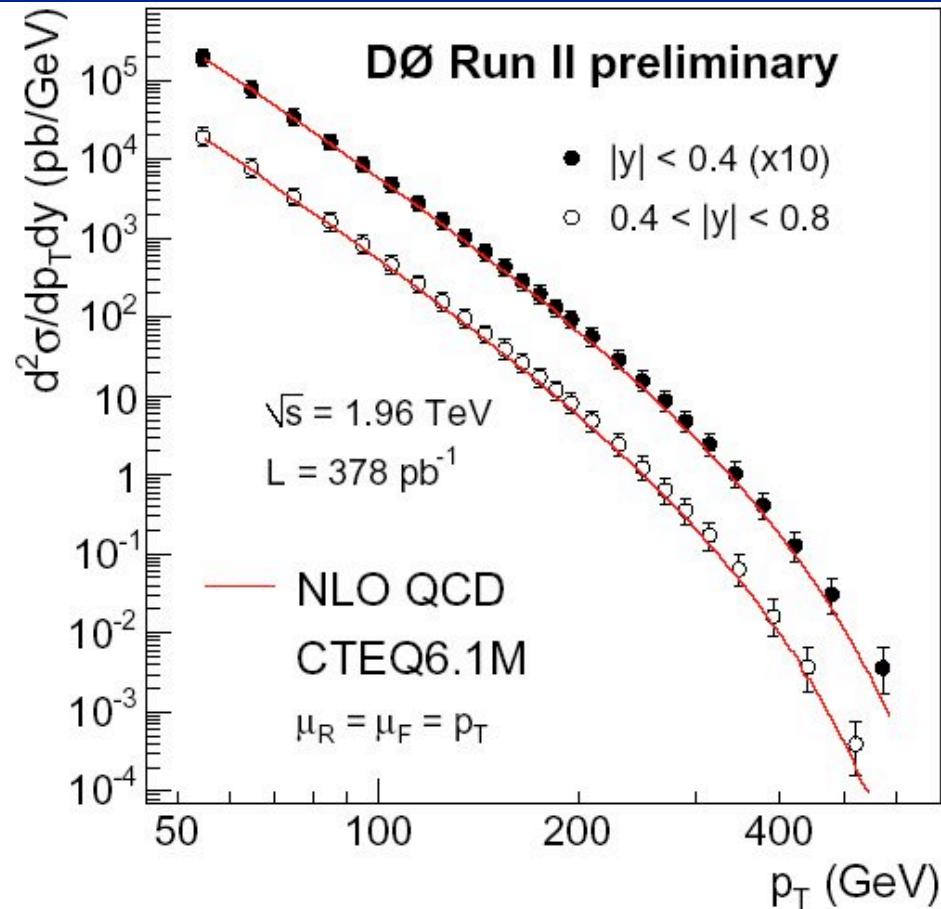
partons: MRST2002
 NNLO evolution: Moch, Vermaseren, Vogt
 NNLO W,Z corrections: van Neerven et al. with Harlander, Kilgore corrections

$\sigma_{Th,NNLO} = 251.3 \pm 5.0 \text{ pb}$
 (Martin, Roberts, Stirling, Thorne)



- Can use these processes to normalize luminosity absolutely
 - However, theory uncertainty larger at LHC and theorists don't agree (yet)⁴⁷

Differential Cross Section



- Measure jet spectra differentially in E_T and η
- Cross section in bin i :
$$\sigma(\mathbf{i}) = \frac{N_{\text{obs}}(\mathbf{i}) - N_{\text{BG}}(\mathbf{i})}{\int L dt \epsilon(\mathbf{i})}$$

Differential Cross Section: Unfolding

- “Unfolding” critical for jet cross sections
- Measure:
 - Cross section for calorimeter jets
- Want:
 - Cross section for hadron-jets

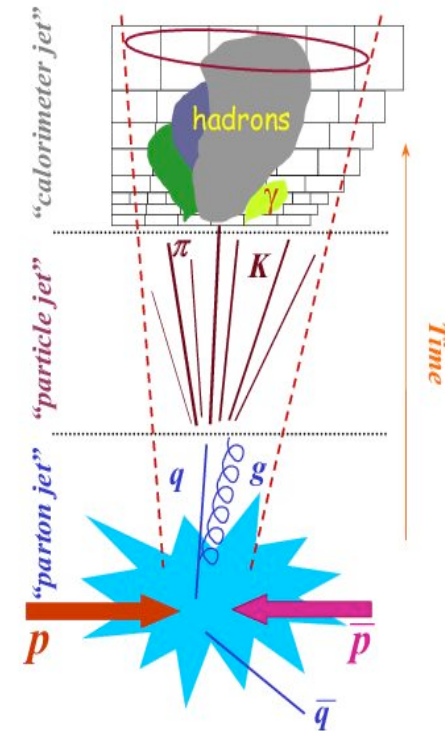
Unfolding factor (bin by bin):

$$C_i = \frac{N_{JET\ i}^{HAD}}{N_{JET\ i}^{CAL}}$$

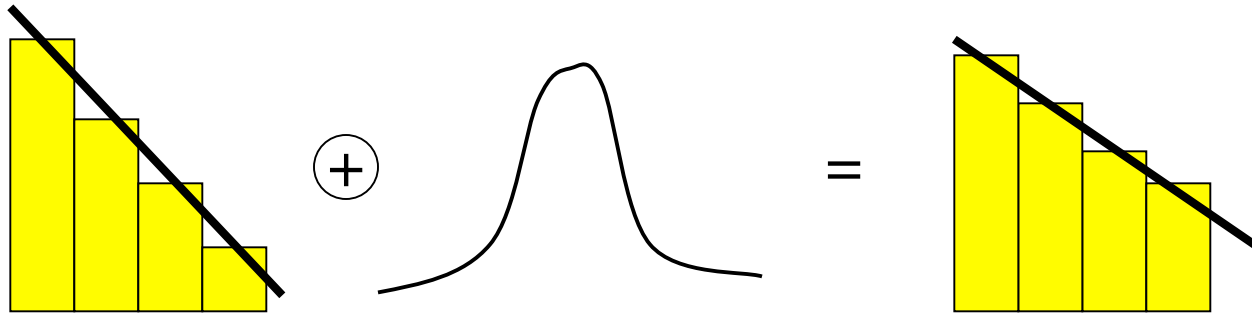
Then:

$$N_{JET\ i}^{DATA\ UNFOLDED} = C_i \cdot N_{JET\ i}^{DATA\ NOT\ UNFOLDED}$$

- But, unfolding factors depend on MC E_T spectrum



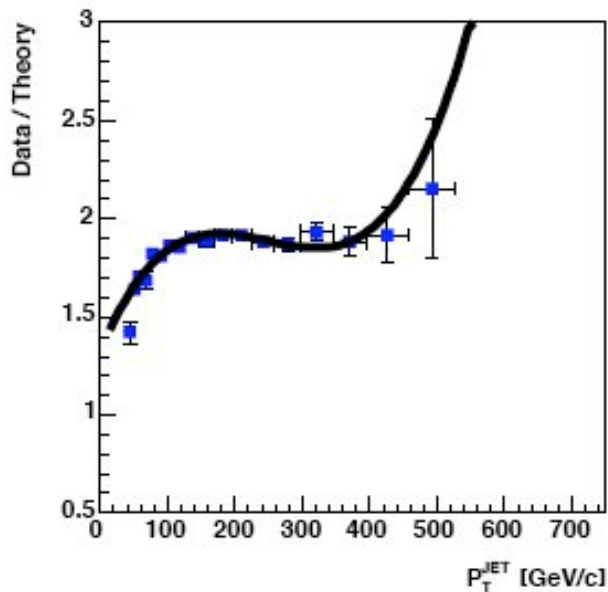
Differential Cross Section: Unfolding



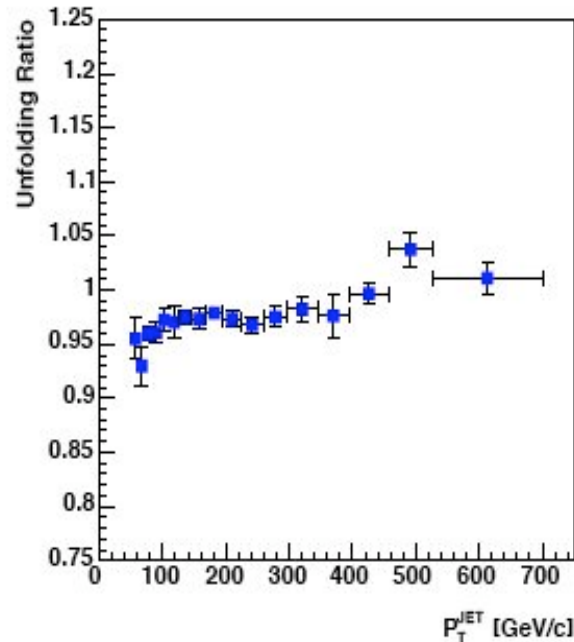
- **Problem:**
 - Steeply falling spectrum causes migrations to go from low to high p_T
 - Measured spectrum “flatter” than true spectrum
 - Size of migration depends on input spectrum
- **Requires iterative procedure** (bin-by-bin unfolding):
 1. Measure using spectrum from MC
 2. Fit measurement
 3. Reweight MC to reflect data measurement => go back to 1.

Example for Bin-by-Bin Unfolding

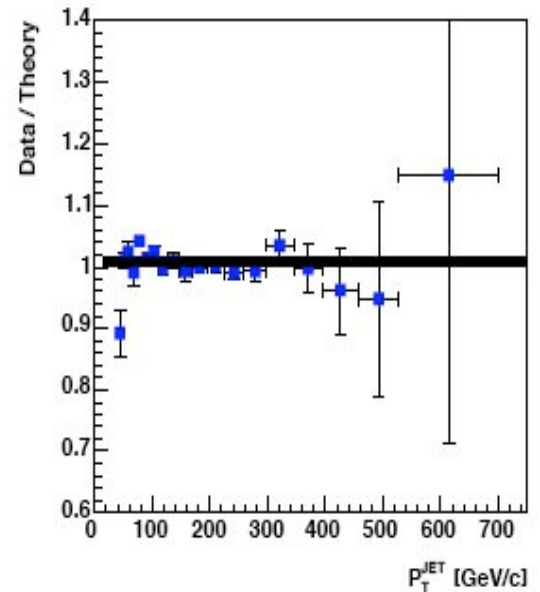
Data / Unweighted Herwig (D=0.7)



Weighted Herwig / Weighted Pythia (D=0.7)



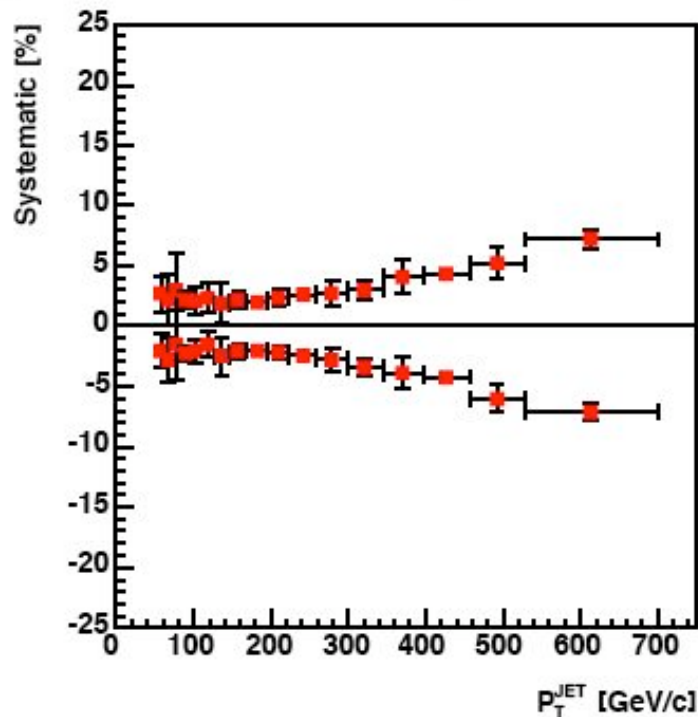
Data / Weighted Herwig (D=0.7)



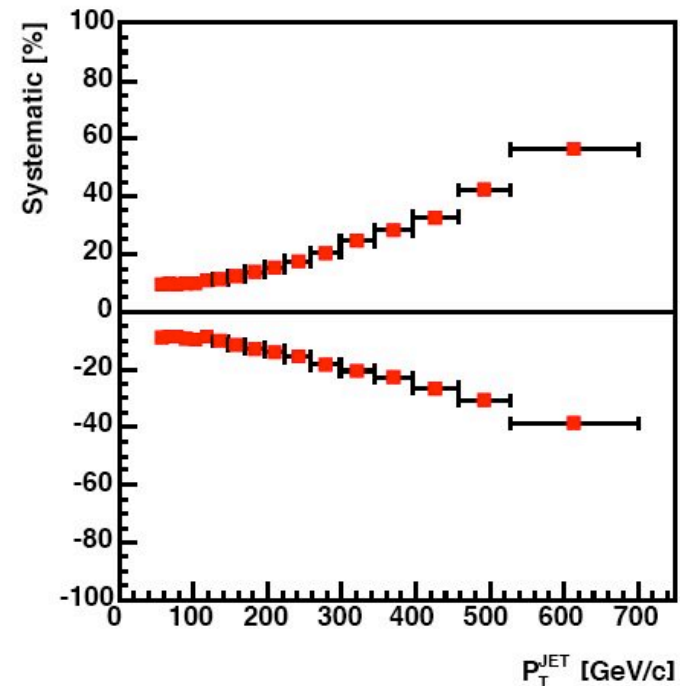
- Correction to unfolding factors <10%
 - One iteration sufficient in this example
 - Starting spectrum was already quite close to data

Systematic Uncertainties: Jet Cross Section

8% uncertainty on resolution (D=0.5)

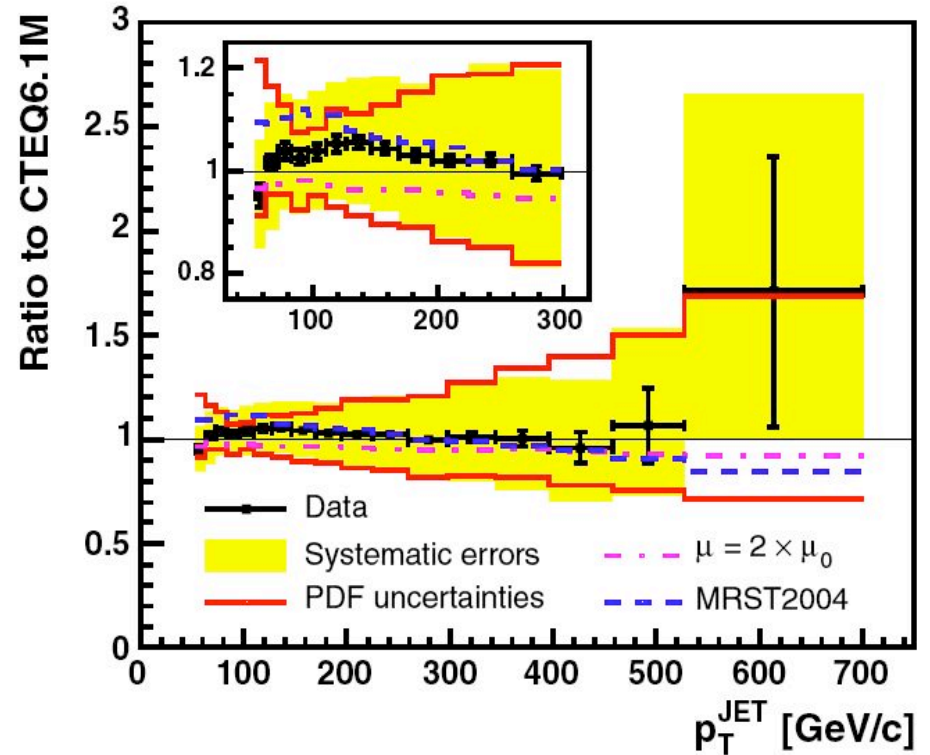
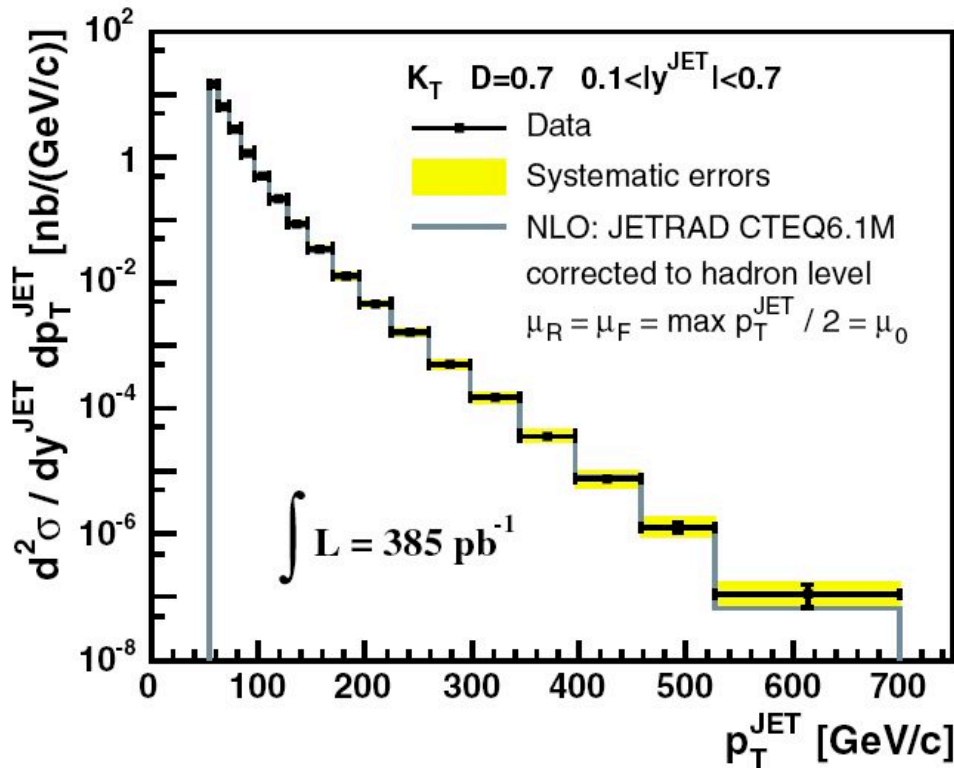


Jet Energy Scale Uncertainty (D=0.5)



- For Jet Cross Section the Jet Energy Scale (JES) uncertainty is dominant systematic error
 - 3% uncertainty on JES results in up to 60% uncertainty on cross section
 - 8% uncertainty on JE resolution causes <10% uncertainty on cross section

Jet Cross Section Result



- Cross section falls by 8 orders of magnitude in measured E_T range
- Data in good agreement with QCD prediction
 - Experimental and theoretical errors comparable

Introduction

HERA

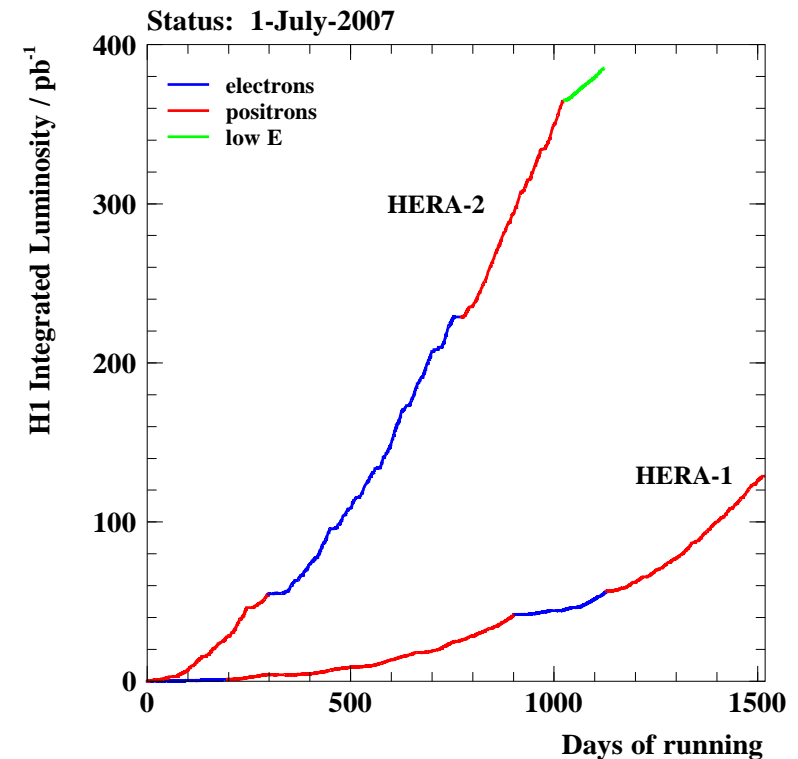
electron(positron)-proton collider at DESY



HERA I 1994-2000
 over $100 pb^{-1}$ collected per experiment
 mainly e^+p data

HERA II 2002-2007
 about $400 pb^{-1}$ per experiment
 similar amount of e^-p and e^+p data

$\sim 20 pb^{-1}$ of data from low and medium energy running: not considered here

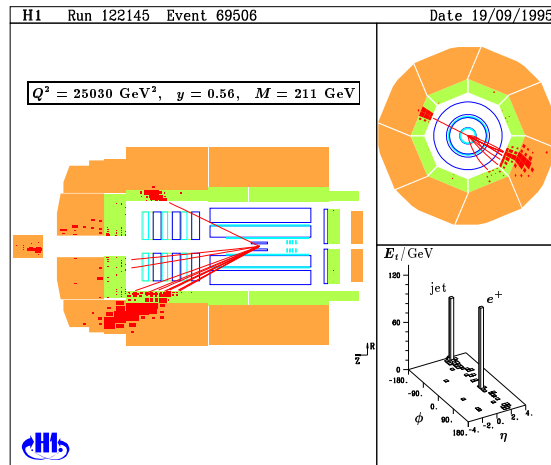


Deep Inelastic $e^\pm p$ Scattering

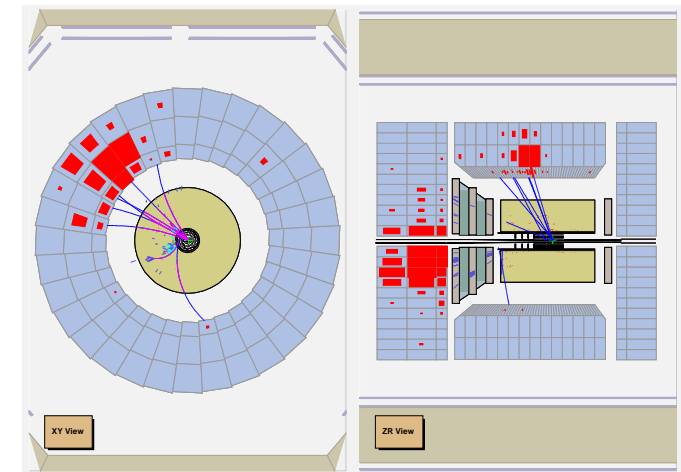


Main process studied at H1 and ZEUS

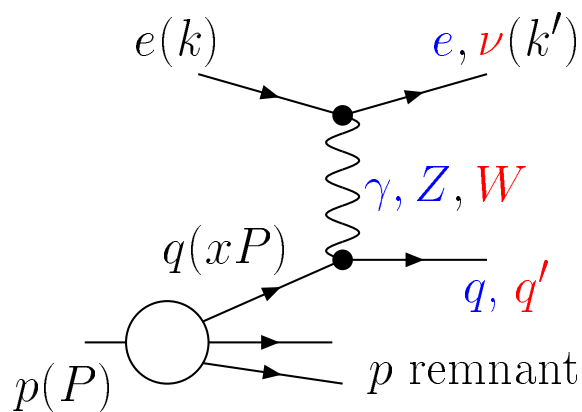
NC DIS



CC DIS



Kinematic variables:



$$Q^2 = -(k - k')^2$$

[virtuality] of the exchanged boson

⇒ spatial resolution $\lambda \sim 1/Q$

$$x = \frac{Q^2}{2P \cdot (k - k')}$$

⇒ sensitivity to mass scales $\Lambda \sim Q$

$$y = \frac{P \cdot (k - k')}{P \cdot k}$$

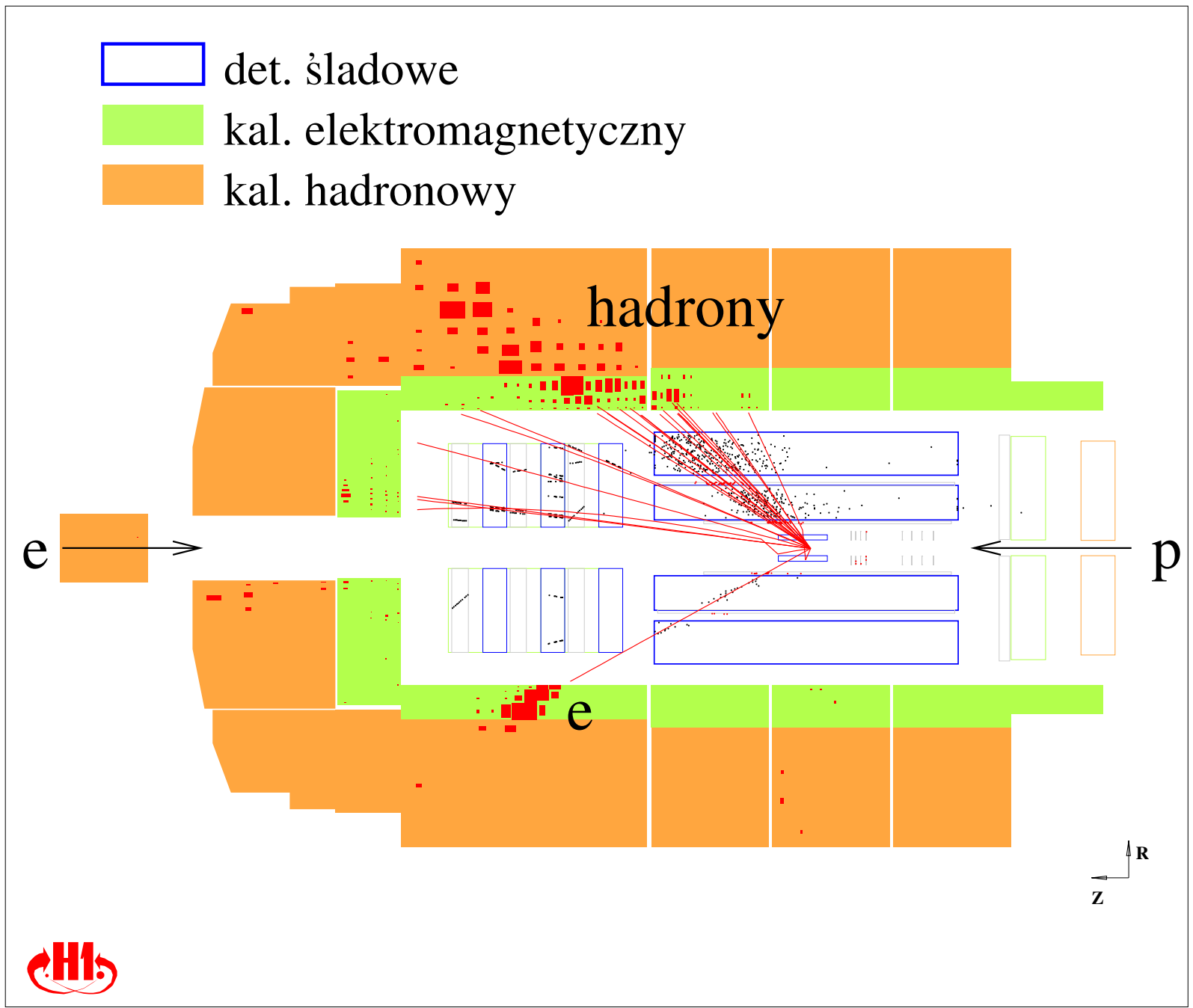


Przypadek
NC DIS

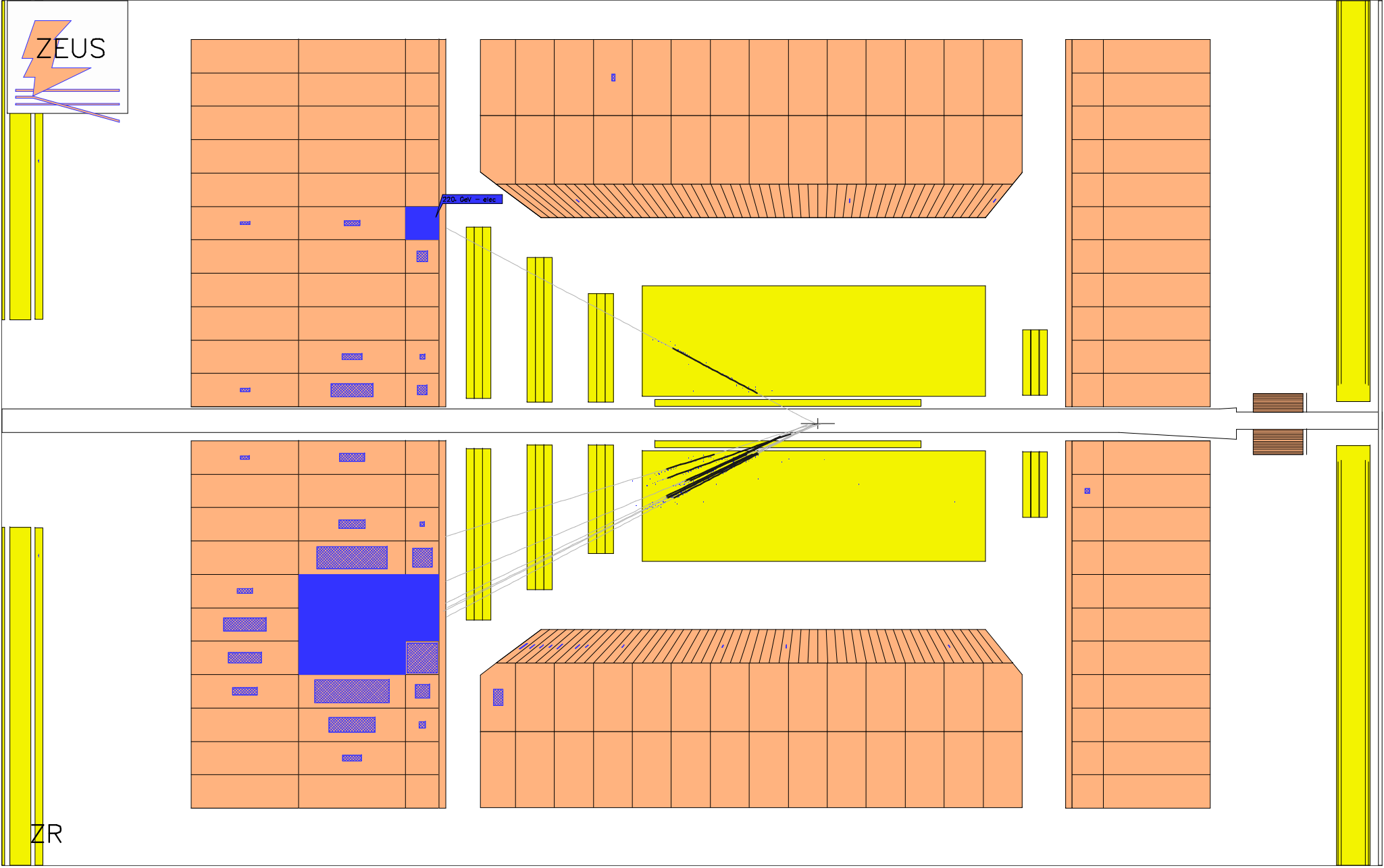
Ekspertment H1

mierzymy **energie**
i **kąt** rozproszenia
elektronu
 $\Rightarrow x, Q^2$

można też mierzyć
stan hadronowy...



Przypadek NC DIS **Ekspertment ZEUS**

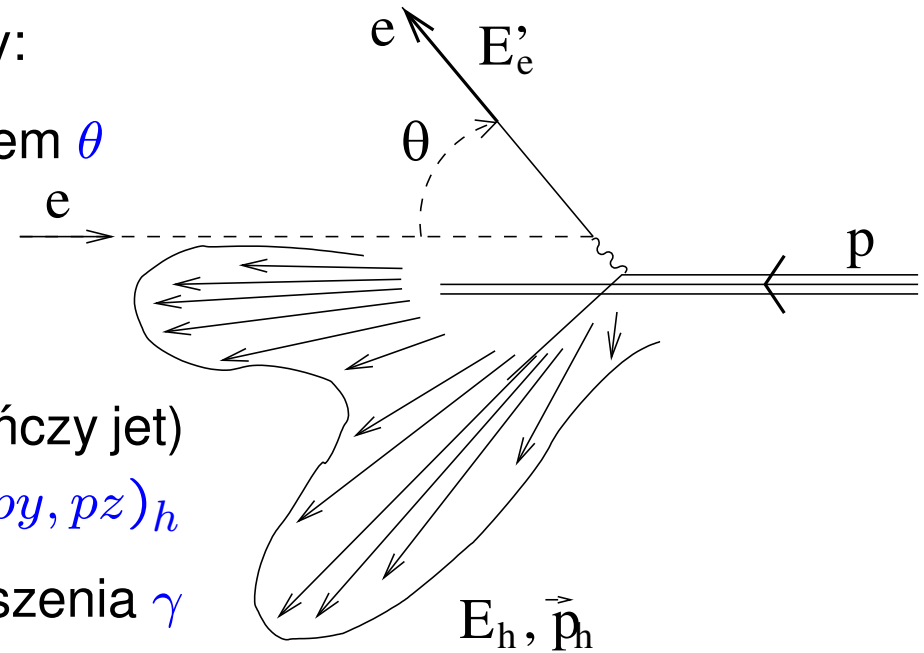


Rekonstrukcja przypadków

Pomiar w detektorze

W przypadkach **NC DIS** w detektorze mierzymy:

- **elektron** o energii E'_e rozproszony pod kątem θ
 - stan **hadronowy** (na ogół nie jest to pojedynczy jet) o całkowitej energii E_h i pędzie $\vec{p}_h = (p_x, p_y, p_z)_h$
- ⇒ możemy wyznaczyć **efektywny kąt** rozproszenia γ i **energię** E_q jetu ⇒ **partonu**



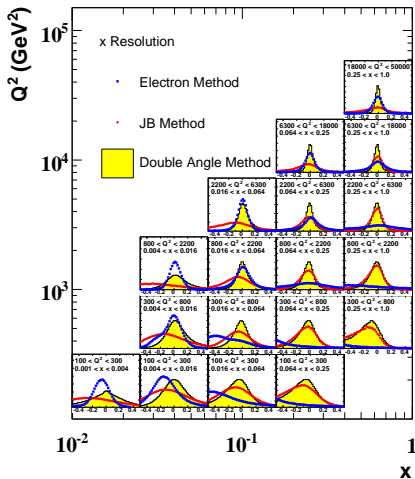
Chcemy wyznaczyć **dwie** zmienne, np. x i Q^2 (trzecią zmienną mamy z relacji: $Q^2 = xys$)

Mamy **cztery** wielkości mierzone: E'_e , θ , E_q i γ ⇒ **mamy dużą swobodę wyboru metody**

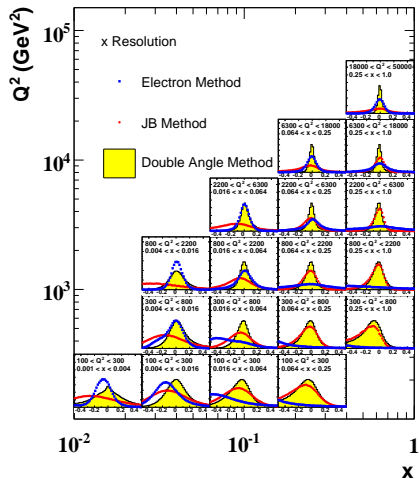
Teoretycznie (nieskończenie dokładny pomiar) wszystkie metody są **równoważne**.

Efekty doświadczalne (**błędy pomiarowe**) powodują jednak znaczne **różnice w dokładności** wyznaczenia x , y i Q^2 różnymi metodami ⇒ wybór zależy od eksperymentu...

Nominal



Using MEPS



Wyznaczanie funkcji struktury

Przekrój czynny

Funkcję struktury $F_2(x, Q^2)$ wyznaczamy bezpośrednio z pomiaru różniczkowego **przekroju czynnego** na **NC DIS**:

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4} \left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) (1 + \delta_L + \delta_Z + \delta_{rad})$$

Wyznaczane **teoretycznie poprawki** pochodzą od:

- δ_L – tzw. podłużnej funkcji struktury F_L
(wkład gluonów powoduje, że $F_L \equiv F_2 - 2xF_1 \neq 0$)
- δ_Z – wymiany bozonu Z^0
(istotne tylko dla bardzo dużych Q^2)
- δ_{rad} – procesów radiacyjnych
(poprawki radiacyjne; emisja γ przez elektron przed lub po zderzeniu)

Wyznaczanie funkcji struktury

Przekrój czynny

Różniczkowy przekrój czynny wyznaczamy mierząc liczbę przypadków zrekonstruowanych w przedziałach x i Q^2 :

$$\Delta N(x \pm \frac{\Delta x}{2}, Q^2 \pm \frac{\Delta Q^2}{2}) = \frac{d^2 \sigma}{dx dQ^2} \cdot \Delta x \cdot \Delta Q^2 \cdot \mathcal{L}_{int} \cdot \mathcal{E} \cdot \mathcal{A}$$

gdzie:

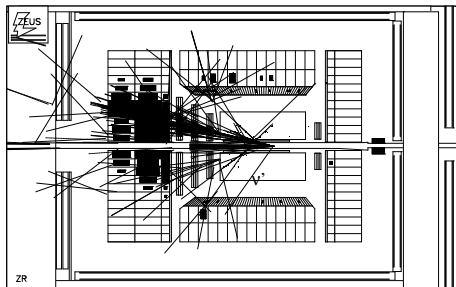
- \mathcal{L}_{int} – scałkowana świetlność
- \mathcal{E} – efektywność selekcji przypadków
- \mathcal{A} – poprawka związana z niedokładnością pomiaru (“przesypywanie” przypadków pomiędzy przedziałami)

NC Selection Part 1

- EVtake, POLtake, MVDtake, REG trk
- FLT: 28, 30, 39, 40, 41, 43, 44, 46
- SLT: DIS07, EXO1, EXO2, EXO3
- TLT: DIS03
- $Q_{DA}^2 > 185 \text{ GeV}^2$
- $38 \text{ GeV} < \delta < 65 \text{ GeV}$
- $|Z_{vtx}| < 50 \text{ cm}$
- $y_e < 0.95$
- $y_{JB}(1 - x_{DA})^2 > 0.004$
- Elastic QEDC rejection
- P_T balance
 - $P_T / \sqrt{E_T} < 4 \text{ GeV}^{1/2}$
 - $P_T / E_T < 0.7$
- Chimney, supercrack, box cuts
- $R_e^{RCAL} < 175 \text{ cm}$
- $R_{had}^{FCAL} > 18 \text{ cm}$
- Electron identification
 - First EM candidate
 - $EM_{prob} > 0.001$
 - $E'_e > 10 \text{ GeV}$
 - $E^{cone}(\text{not e-}) < 5 \text{ GeV}$
- Yongdok's new alignment and electron energy corrections
- Umer's new backplash cut for CorAndCut

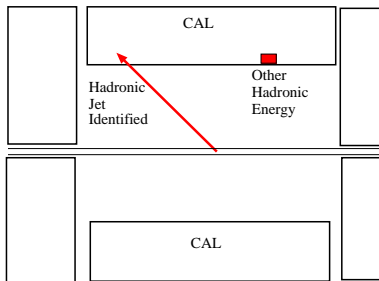
Backsplash

MC CC Event (MC tracks
overlayed)



- Proper reconstruction of hadronic final state important
- Can use to determine kinematic variables
- Measured hadronic quantities can be altered by
 - Backsplash from the CAL
 - Scattering from dead material
- Cause energy deposits far from true particle direction
- Notably increases measured $(E - P_z)_h$ and γ_h at low y

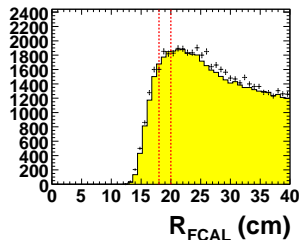
Using Data to Derive Backsplash Cut Parameters



- We began a new jet based approach
- Use most backward jet found and associate its jet axis with the “true entry” position
- Look for cone islands backward from the jet
- Use distance from jet axis to cone islands to flag backsplash deposits
- Method can be applied to data and MC

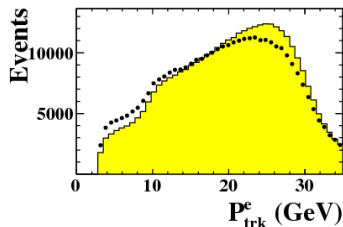
NC Selection Part 2

- Inside CTD acceptance:
 - CTD exit Radius > 45 cm
 - $P_{ele}^{trk} > 3$ GeV
 - DCA < 10 cm
 - DME > 1.5 cm
- Forward of CTD acceptance:
 - $P_{T,ele} > 30$ GeV



Changes to standard selection:

- $Q_{DA}^2 > 200 \rightarrow 185$ GeV²
 - Lower bin edge of reduced cross section
- $R_{had}^{FCAL} > 20 \rightarrow 18$ cm
- $P_{ele}^{trk} > 5 \rightarrow 3$ GeV
 - Constrain systematics



Wyznaczanie funkcji struktury

Rozkład mierzonych przypadków **NC DIS** w zmiennych x, Q^2 .

Dane współpracy **ZEUS** \Rightarrow

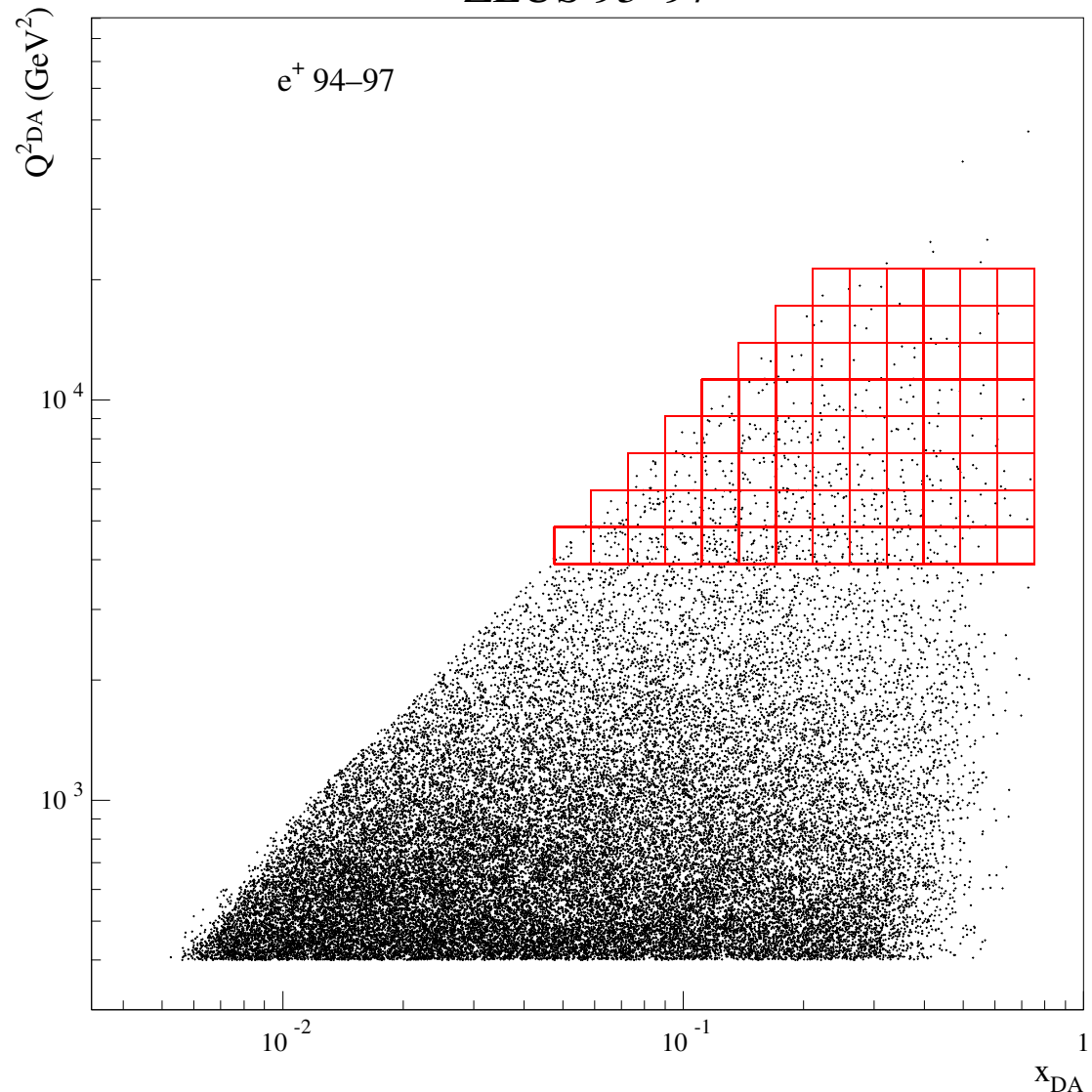
Liczba przypadków w binach **maleje szybko z Q^2**

$$\Delta N \sim \frac{1}{Q^4}$$

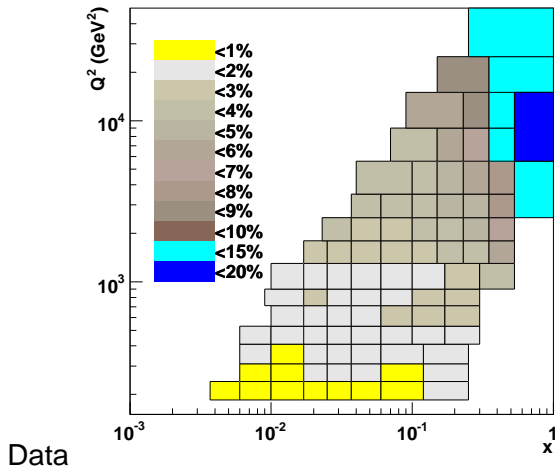
\Rightarrow pomiar ograniczony do

$$Q^2 \leq 2 \cdot 10^4 \text{ GeV}^2$$

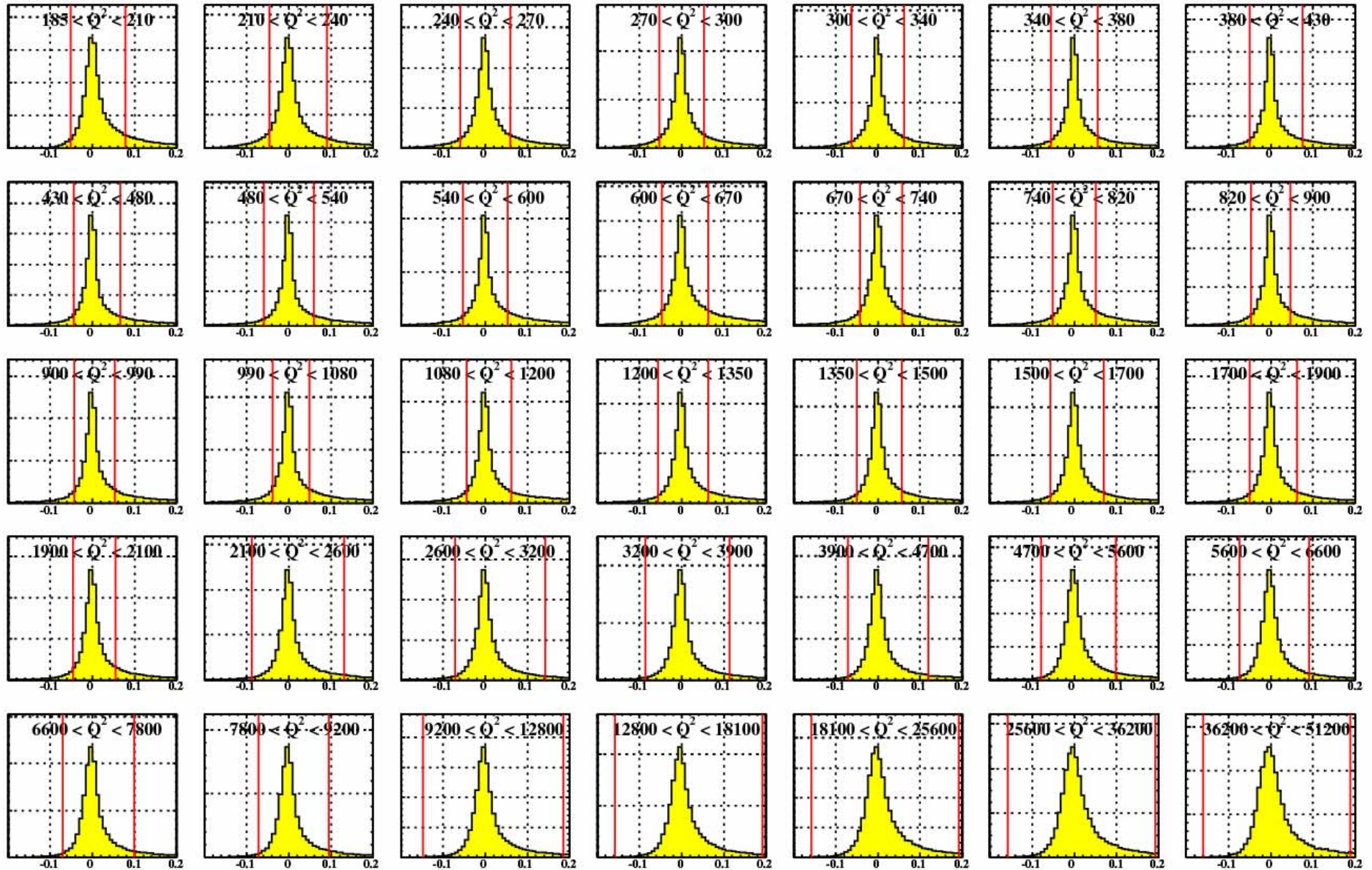
ZEUS 93–97



Statistical Error in Bins used for $d^2\sigma/dxdQ^2$

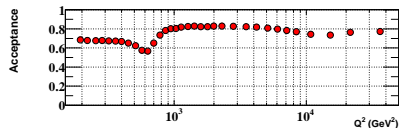
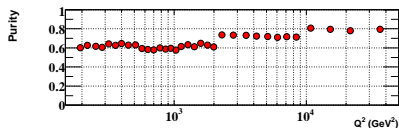
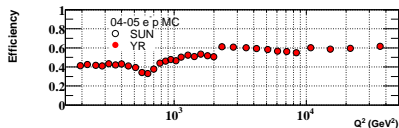


$d\sigma/dQ^2$: Bias and Resolution



$$(Q^2_{DA} - Q^2_{true})/Q^2_{true}$$

Efficiency and Purity for $d\sigma/dQ^2$

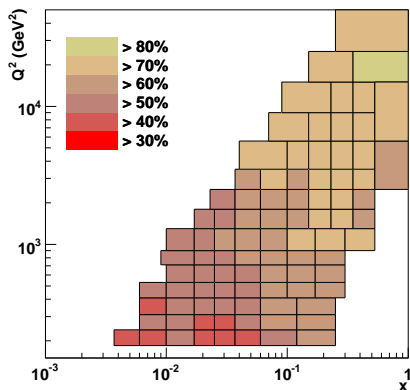
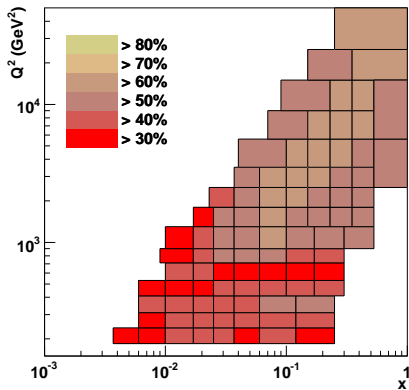


- Efficiency = $\frac{\text{Generated \& Accepted}}{\text{Generated}}$
- Purity = $\frac{\text{Generated \& Accepted}}{\text{Accepted}}$
- Acceptance = $\frac{\text{Efficiency}}{\text{Purity}}$

Efficiency and Purity in $d^2\sigma/dxdQ^2$

$$\text{Efficiency} = \frac{\text{Generated \& Accepted}}{\text{Generated}}$$

$$\text{Purity} = \frac{\text{Generated \& Accepted}}{\text{Accepted}}$$

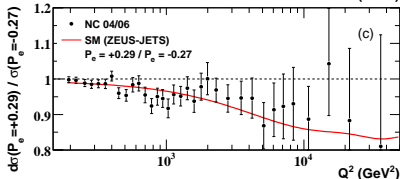
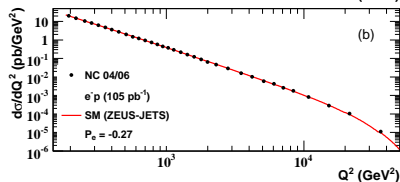
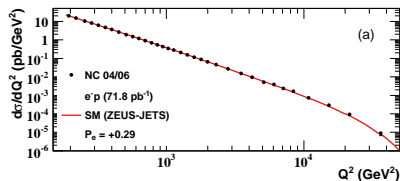


Unfolding Cross Sections

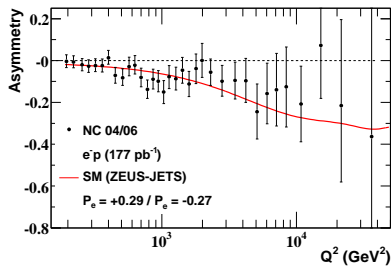
Cross sections extracted using:

- $\frac{d\sigma}{dQ^2} \Big|_{Q_0^2} = \frac{(N_{DATA} - N_{BG})}{N_{MC}} \frac{d\sigma}{dQ^2} \Big|_{Q_0^2}^{theory}$
- With Born-level unpolarised MC and theory values
- See backup for bin selection (based on HERA I binning)
 - Finer in $d\sigma/dQ^2$
 - Higher/lower bins in $d\sigma/dx$, $d\sigma/dy$
 - Keep same for reduced cross sections

$$d\sigma/dQ^2$$



- χ^2 test for all ratio points:
- +ve P_e / -ve $P_e = 1$ case
 - $\chi^2 / \text{ndf} = 83 / 34$
- +ve P_e / -ve $P_e = \text{SM}$ case
 - $\chi^2 / \text{ndf} = 28 / 34$



Wyznaczanie funkcji struktury

Liczba mierzonych przypadków decyduje o błędzie statystycznym wyznaczonych wartości $F_2(x, Q^2)$:

$$\frac{\sigma_{F_2}^{stat}}{F_2} = \frac{1}{\sqrt{\Delta N}}$$

Błędy statystyczne dominują przy dużych Q^2 , przy małych Q^2 są zaniedbywalne.

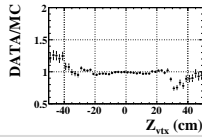
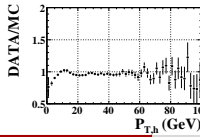
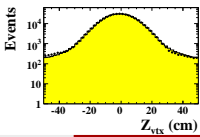
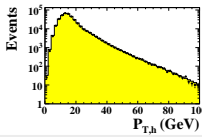
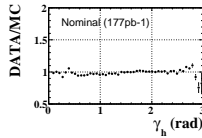
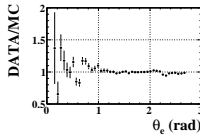
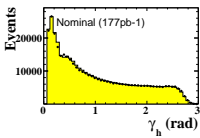
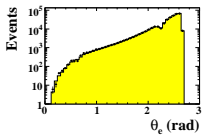
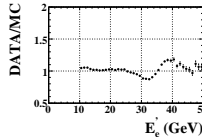
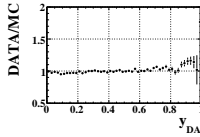
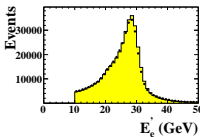
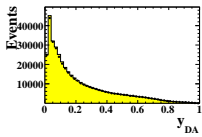
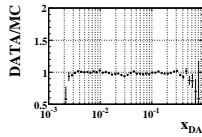
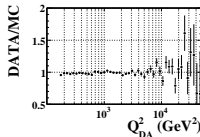
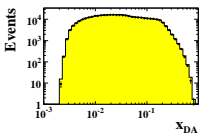
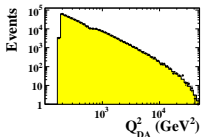
Błąd systematyczny pomiaru wynika z **niepewności**:

- poprawek teoretycznych δ_L , δ_Z i δ_{rad}
- pomiaru świetności \mathcal{L}_{int}
- wyznaczenia poprawek \mathcal{E} i \mathcal{A}
(niepewności związane z symulacją Monte Carlo badanego procesu i działania detektora)

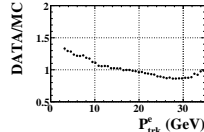
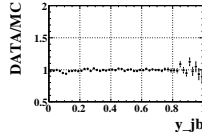
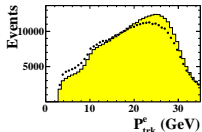
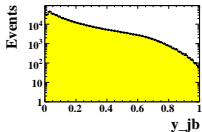
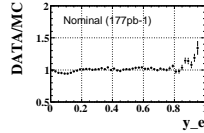
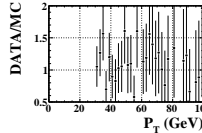
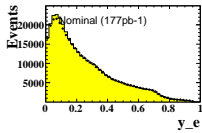
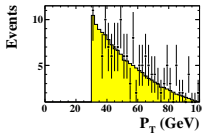
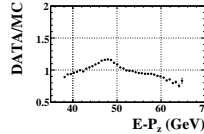
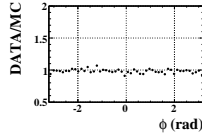
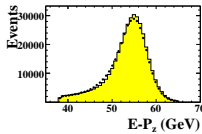
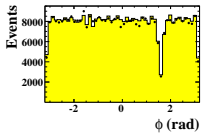
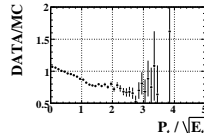
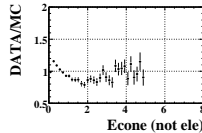
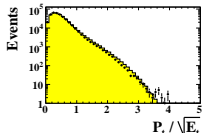
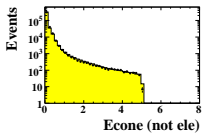
Błędy systematyczne dominują przy małych Q^2 .

Na ogół są na poziomie kilku % (obecne pomiary w HERA)

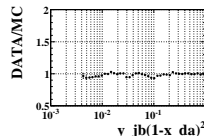
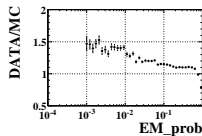
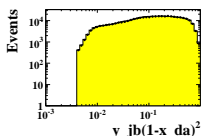
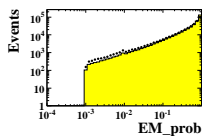
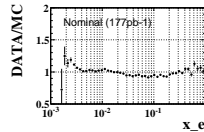
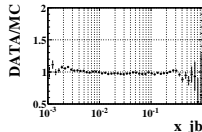
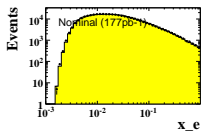
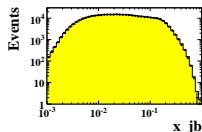
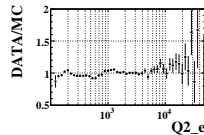
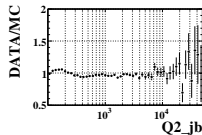
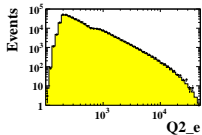
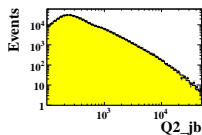
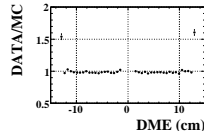
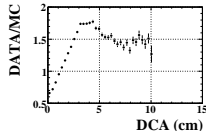
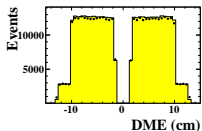
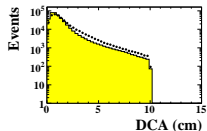
Control Plots



Control Plots



Control Plots

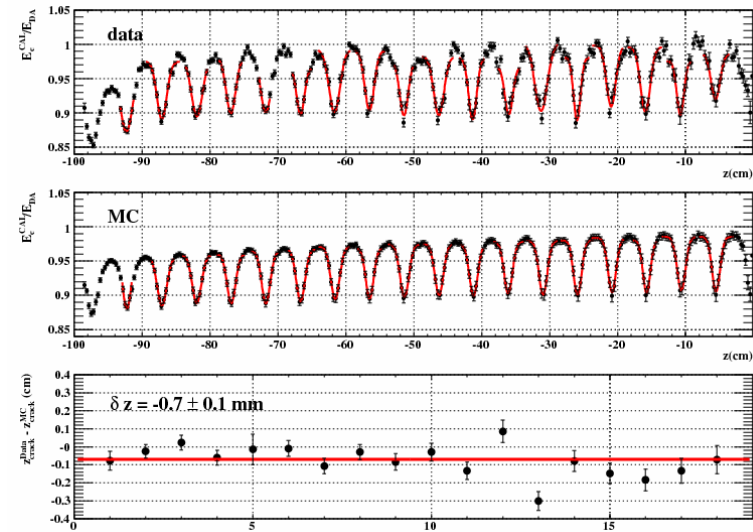


CAL alignment with respect to CTD

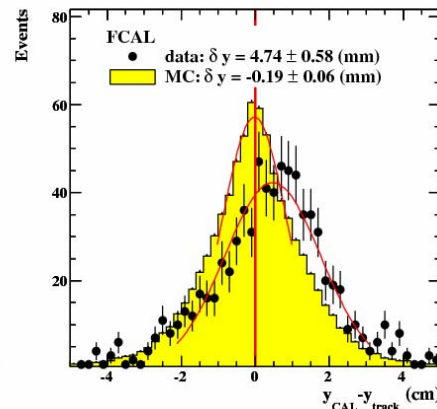
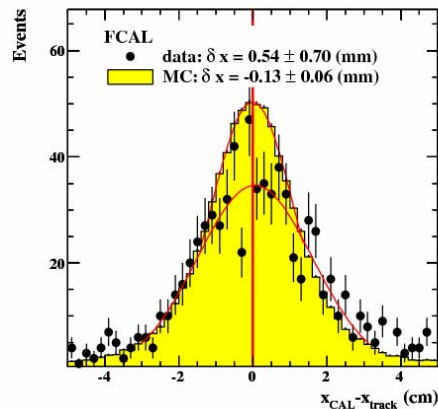
Stat error only.

	RHES left	RHES right
$\delta \phi$	$+1.6 \pm 0.1 \text{ mrad}$	$+0.9 \pm 0.1 \text{ mrad}$
δz	$+2.0 \pm 0.2 \text{ mm}$	$-0.9 \pm 0.2 \text{ mm}$
δx	<u>$+1.9 \pm 0.1 \text{ mm}$</u>	<u>$-1.7 \pm 0.1 \text{ mm}$</u>
δy	<u>$+1.4 \pm 0.1 \text{ mm}$</u>	<u>$-1.0 \pm 0.1 \text{ mm}$</u>

RCAL is aligned within **2.0mm** in x and y direction.



BCAL is aligned within **1.0mm**.
(Only z shift is checked.)



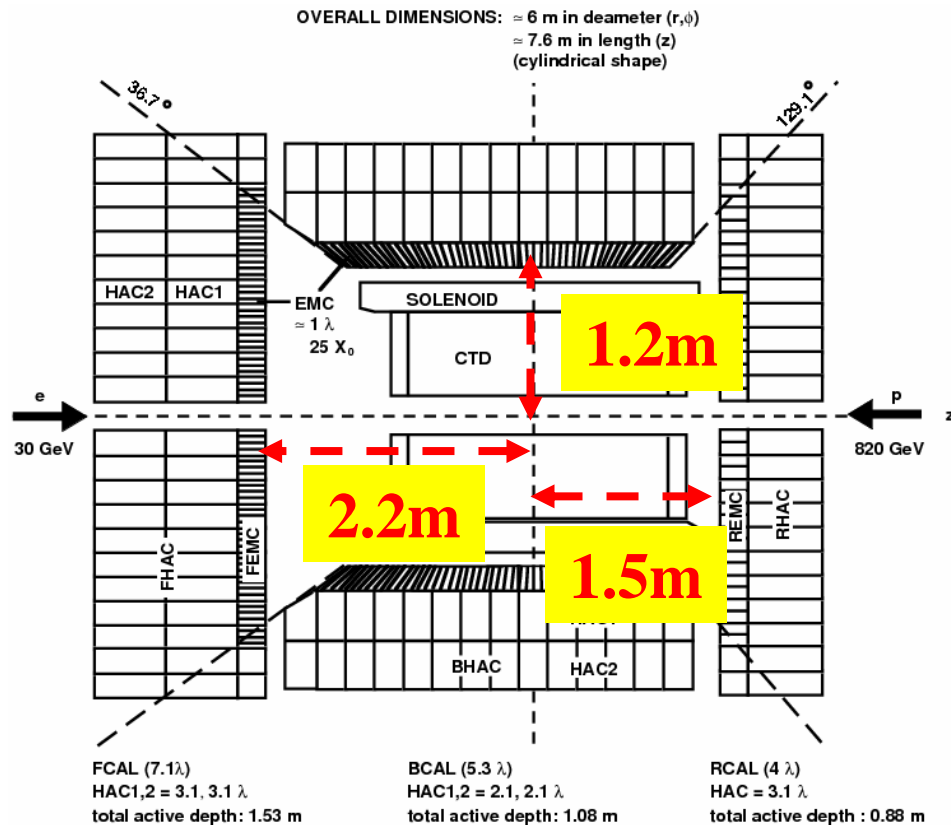
FCAL position correction : Shift the e position with -4mm in y for data. (Hadronic system is neglected.)

FCAL is aligned within **2.0mm**.

For more details, see talk at F_L review meeting on 09/Feb/2007.

Uncertainty of CAL position

Estimate the effect on cross section by varying the θ_e .



$$\delta \theta = \delta l / r$$

- RCAL : $\delta l=2\text{mm}, r=1.5\text{m}$

→ $\delta \theta = 1.3\text{mrad}$

- BCAL : $\delta l=1\text{mm}, r=1.2\text{m}$

→ $\delta \theta = 0.8\text{mrad}$

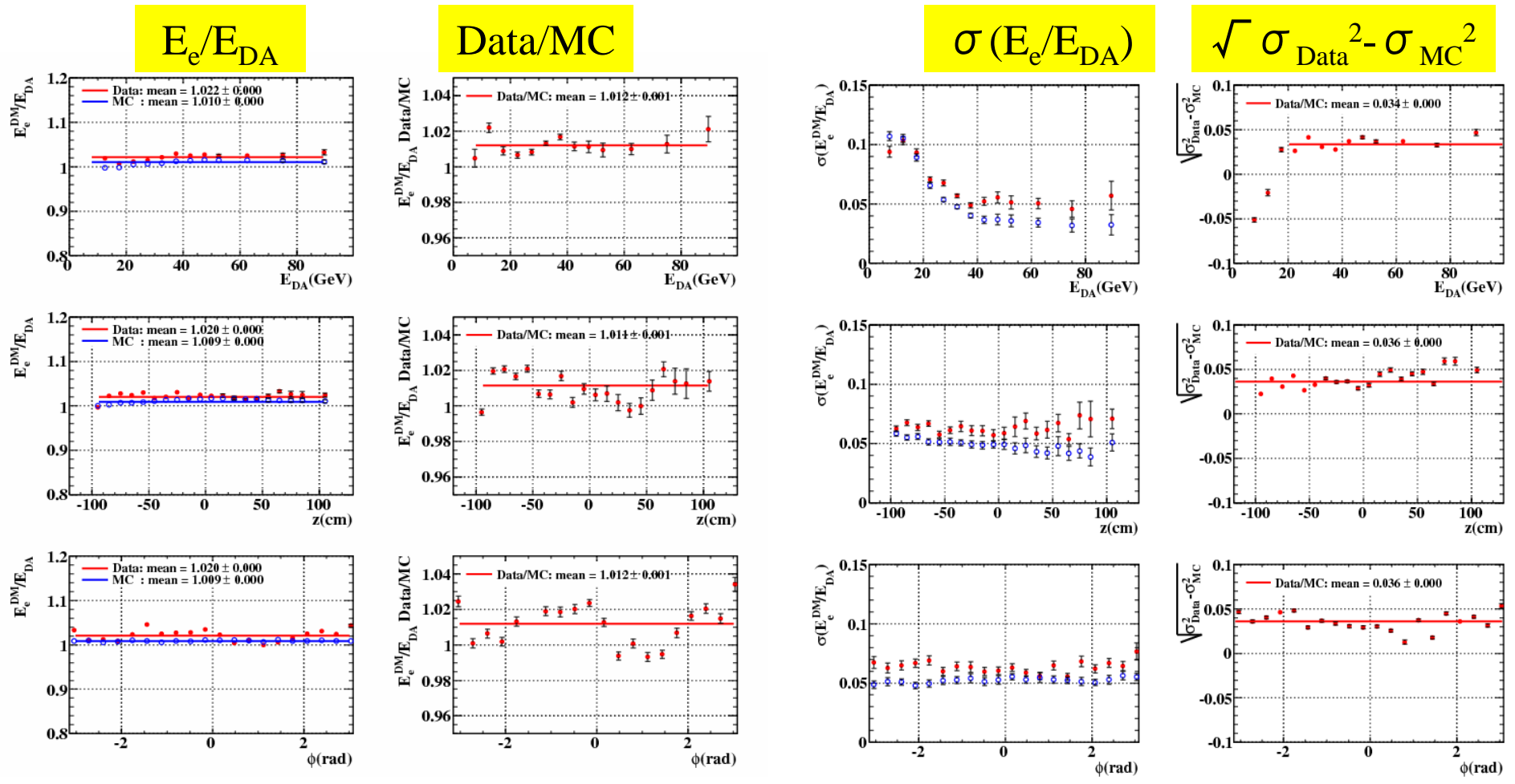
- FCAL : $\delta l=2\text{mm}, r=2.2\text{m}$

→ $\delta \theta = 0.9\text{mrad}$

$\theta_e \pm 1\text{mrad}$ is adequate as systematic check.

BCAL electron energy

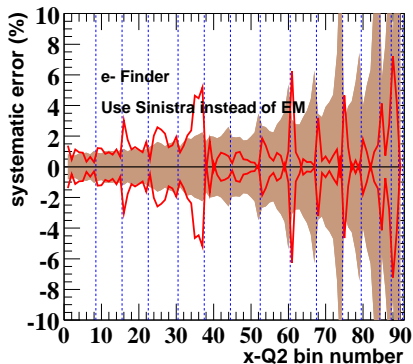
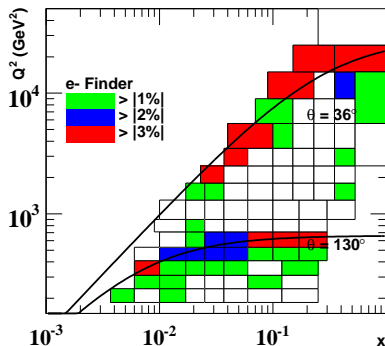
E_e is corrected by dead-material map and non-uniformity.



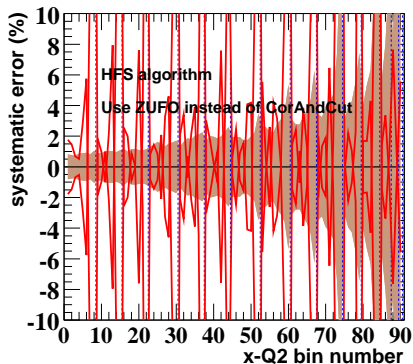
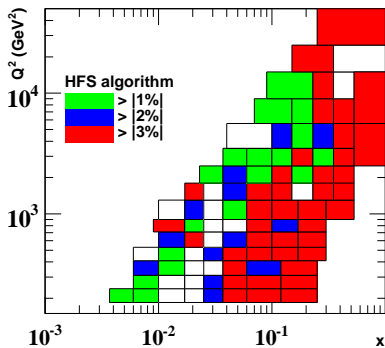
Scale uncertainty is 2%.

Smearing factor is 3.4%.

Systematics in $d^2\sigma/dxdQ^2$ for EM \rightarrow SINISTRA

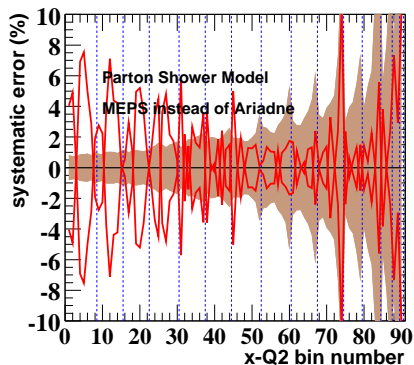
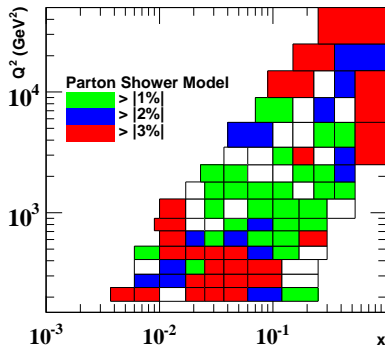


Systematics in $d^2\sigma/dxdQ^2$ for CorAndCut \rightarrow ZUFO



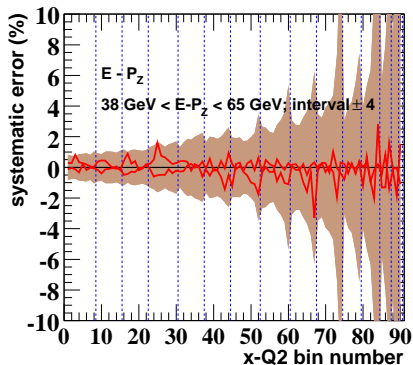
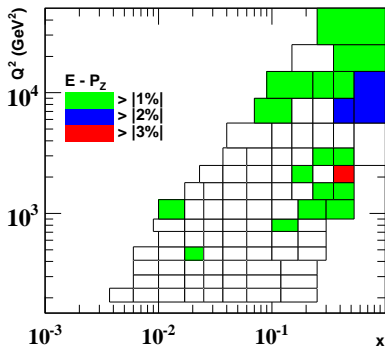
■ Using ZUFOs from EM_HAD block

Largest Systematics in Dbl Diff bins - MEPS

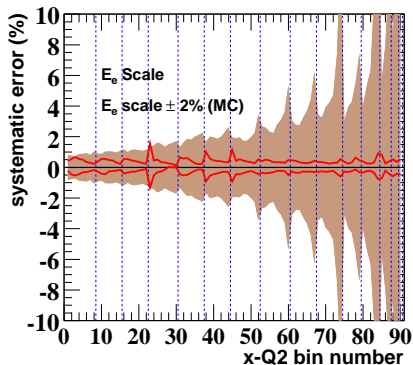
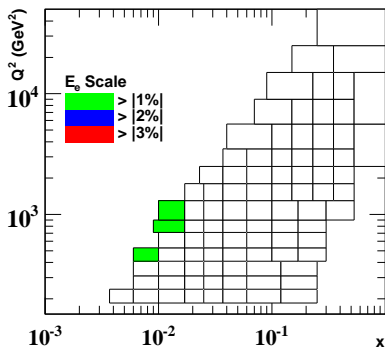


■ Dominates low Q^2 region

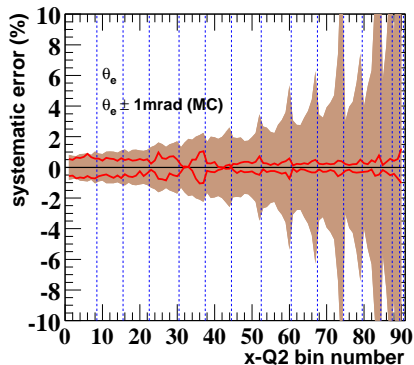
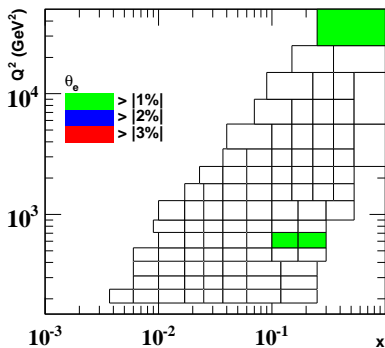
Largest Systematics in Dbl Diff bins - $E - P_Z$



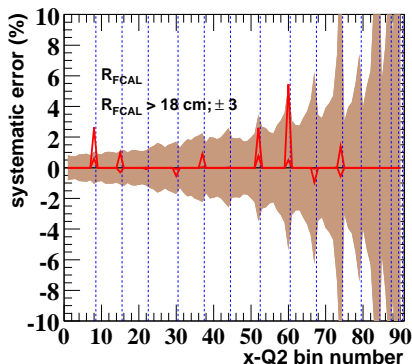
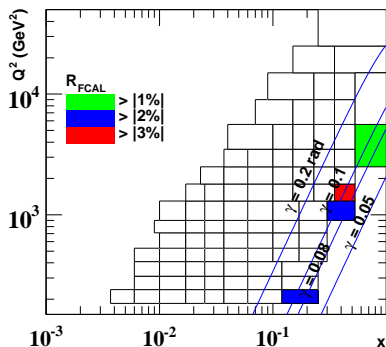
Largest Systematics in Dbl Diff bins - E_e scale



Largest Systematics in Dbl Diff bins - θ_e



Largest Systematics in Dbl Diff bins - R_{FCAL}

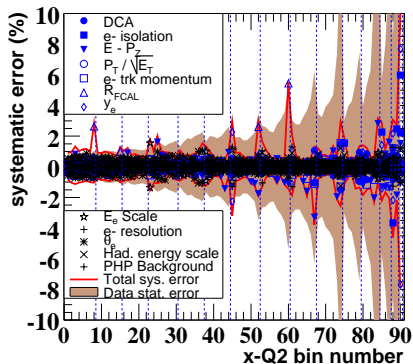
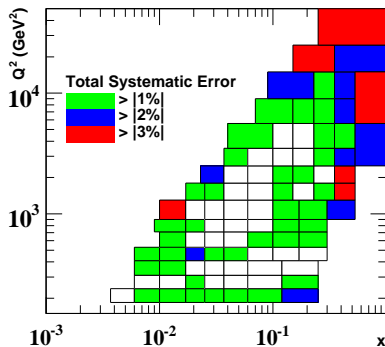


- Projection of γ_h onto face of FCAL
- Dominates in lowest γ_h regions

Systematic Checks

- $DCA > 10 \text{ cm}; 8\text{cm}$
- $E_{note}^{cone} < 5 \text{ GeV}; \pm 2 \text{ GeV}$
- $38 \text{ GeV} < E - P_Z < 65 \text{ GeV};$
interval $\pm 4 \text{ GeV}$
- $P_T / \sqrt{E_T} < 4\sqrt{\text{GeV}}; \pm 1\sqrt{\text{GeV}}$
- $P_{trk}^e > 3 \text{ GeV}; \pm 1 \text{ GeV}$
- $R_{FCAL} > 18 \text{ cm}; \pm 3 \text{ cm}$
- $y_e < 0.95; 0.9$
- $E_e \text{ scale } \pm 2\% \text{ (MC)}$
- $E_e \text{ smeared } \pm 1\% \text{ (MC)}$
- $\theta_e \pm 1\text{mrad (MC)}$
- $E_h \text{ scale } \pm 3\% \text{ (MC)}$
- PHP MC normalization $\pm 100\%$
- Checks not used in error calculations:
 - ARIADNE \rightarrow MEPS
 - EM \rightarrow Sinistra
 - CorAndCut \rightarrow ZUFOs

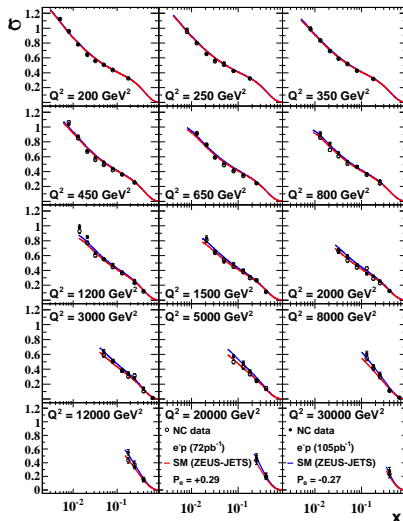
Systematics in $d^2\sigma/dxdQ^2$



Reduced Cross Sections

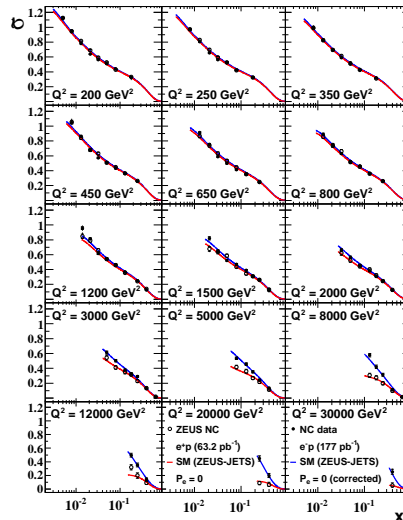
LH and RH separate

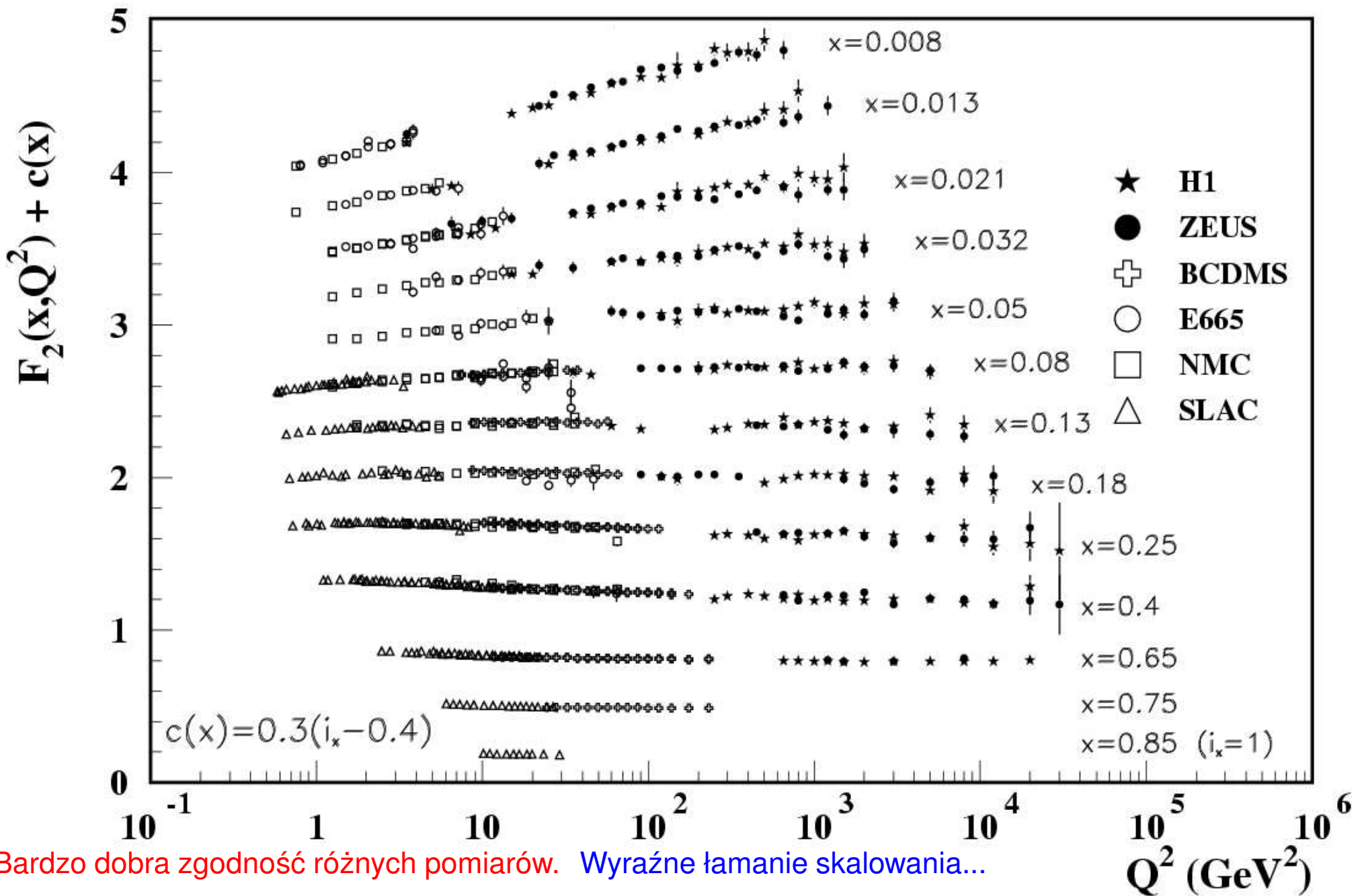
ZEUS



Entire data set

ZEUS





Bardzo dobra zgodność różnych pomiarów. Wyraźne łamanie skalowania...