

Particles and Universe

Lecture 8 Symmetry and SM

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- I. Theory of elementary particles – role of symmetry
- II. Standard Model, generation of mass, Higgs particle
- III. P , C , CP symmetry and matter-antimatter asymmetry

GOAL

.. dotrzeć do tych uniwersalnych elementarnych praw przyrody, z których kosmos może być zbudowany przez czyste wnioskowanie.

I want to know how God created this world. I am not interested in this or that phenomenon.. I want to know His thoughts, the rest are details.

Albert Einstein

Laws and *laws*

Many **phenomenological laws** like Hooke's law:

... the more force we apply to a metal spring, the more it stretches... $F = k x$

In 30 XXw → it arises from properties of electromagnetic interaction in the metal

At the fundamental level we expect
a minimal set of the simplest laws.

Beauty in physics = symmetry

„Oh, how ugly” - Einstein on a equation

Paul Dirac

The beauty of an equation is more important than its correctness, in the sense that if an equation is beautiful, sooner or later it will be demonstrated to be correct.

Herman Weyl

„Symmetry, as wide or as narrow as you may define its meaning, is one idea by which man through the ages has tried to comprehend and create order, beauty, and perfection.”

H. Weyl, Symetria (Prószyński i S-ka 1997)

In April 1915, Emmy Noether was completing her groundbreaking theorem that links conservation laws with the symmetries of Nature.



from L. Molt blog

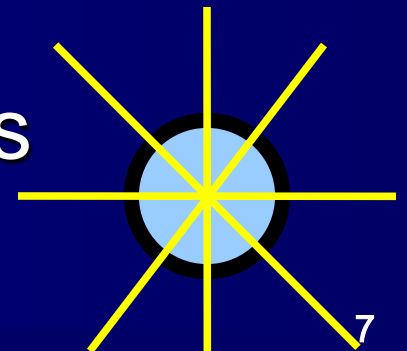
Symmetry or invariance

Geometrical figure is symmetric with respect to some operations, if these operations do not change it, eg.

- rotation
around
origin



-reflection with respect to planes, lines



Symmetry of laws (invariance, independence)

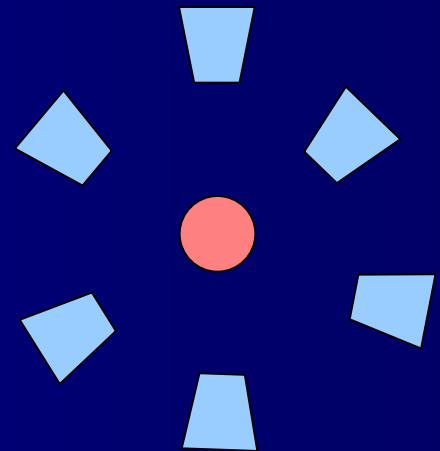
E. Wigner 1930r – does emission of light by an atom depend on the direction?

Experiment: detectors around the emitting atom

The same results

→ so spherical symmetry

Similarly, one can consider invariance of laws on a shift of position or time



Fundamental laws of nature are related to symmetry

Emma Noether, 1918

■ Momentum and energy conservation laws

Related to symmetry (invariance) of *equations of motion* under the transformation of the system:

- conservation of momentum - symmetry under space translation
- conservation of energy - symmetry under time translation
- conservation of angular momentum - symmetry under rotation

■ Electric charge conservation law

related to a symmetry? Later...

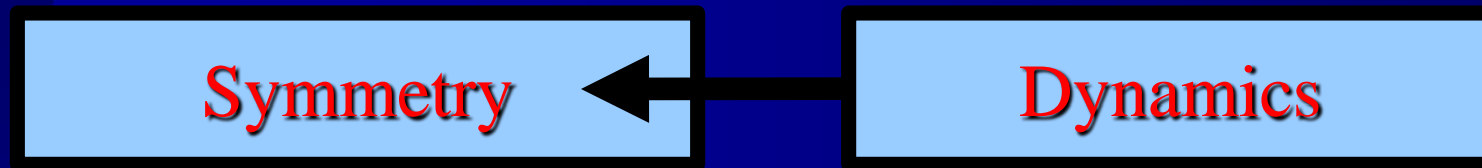
All these laws are valid in microworld as well, in addition there are other conservation laws (quantum numbers, like baryonic B)

SYMMETRY

D. Gross

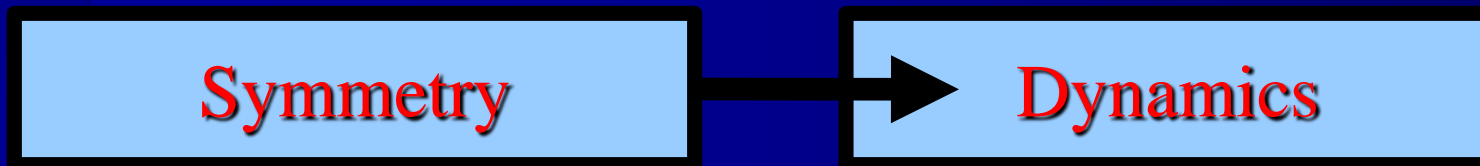
Before EINSTEIN

Symmetry as a consequence of dynamical laws



After EINSTEIN

Einstein realized relativistic symmetry of Maxwell's laws (under Lorentz transformation) and promoted it to a symmetry of space-time. Maxwell's equations were consequences of this symmetry...




Today: Symmetry as an primary property of nature, which determines possible dynamical laws of nature


SYMMETRY or INVARIANCE

■ **GLOBAL (does not depend on time and space):**
Regularity of the laws of motion; global symmetry transformation leads to a different physical situation, but observations are invariant – eg. in laboratory on an orbit distance between desk and window is constant, physical observation the same. Traditional symmetry in nature this type.

■ **LOCAL (depends on time, space), name GAUGE:**
Totally different, related to the laws themselves. Symmetry transformations do not yield to different physical situations. It means independence on **gauge** used to measure (**gauge symmetry**).
Observed for el-magn. interaction - for years without consequences ...

Gauge - a standard or scale of measurement: The capacity of barrels was measured according to the gauge in use at the time.

1912-17 symmetry of space-time under local transformation of reference frame  gravitation

1968-73 gauge symmetry  electroweak and strong interaction

Weyl – gauge symmetry (1918)

..... independence on gauge of physical device

- **Global changes of:** calendar, temperatur scale, position of zeroth meridian, etc do not change: time distance, heat needed to boil water, time of travel. Profit and loss are fixed, if the money is denominated.
- Situation is totally different if changes are local

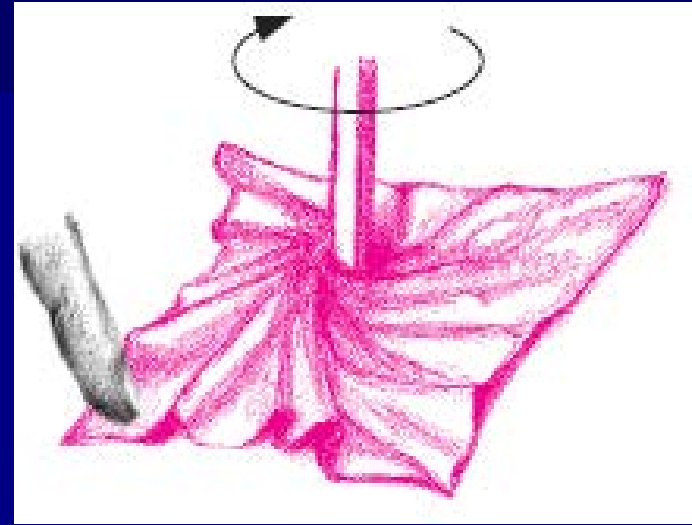
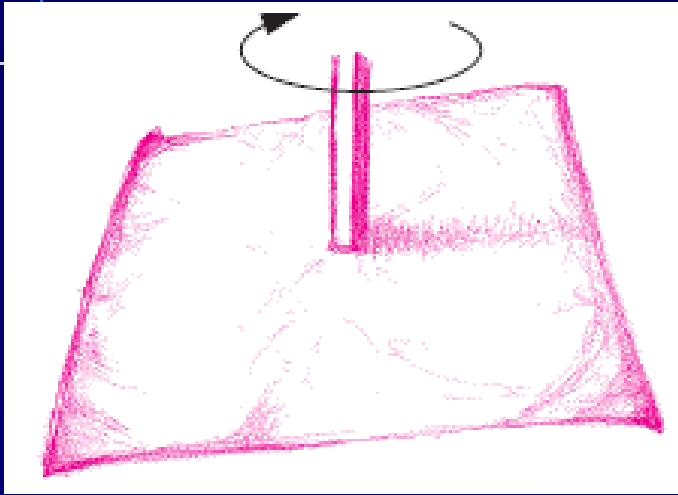
→ eg. speculation if local differences in values



Greenwich

Symmetry

global and local



Rotation of the whole tablecloth
– symmetry

Symetria materii-materia symetrii

M. Krawczyk

DELTA 5 (312) 2000

Local rotation – around a point
there appear wavelets - they can
be removed by force restoring
the symmetry...

We need to introduce a particular interaction everywhere
→ massless carriers of interaction – gauge bosons !

Local symmetry for physical system

- In every case we have to have two types of objects and interaction between them to ensure in each point of space a symmetry
→ only massless carriers of interaction!
- Relation between a type of interaction and particular type of a local symmetry

Gauge principle

Symmetry – main idea in modern particle physics

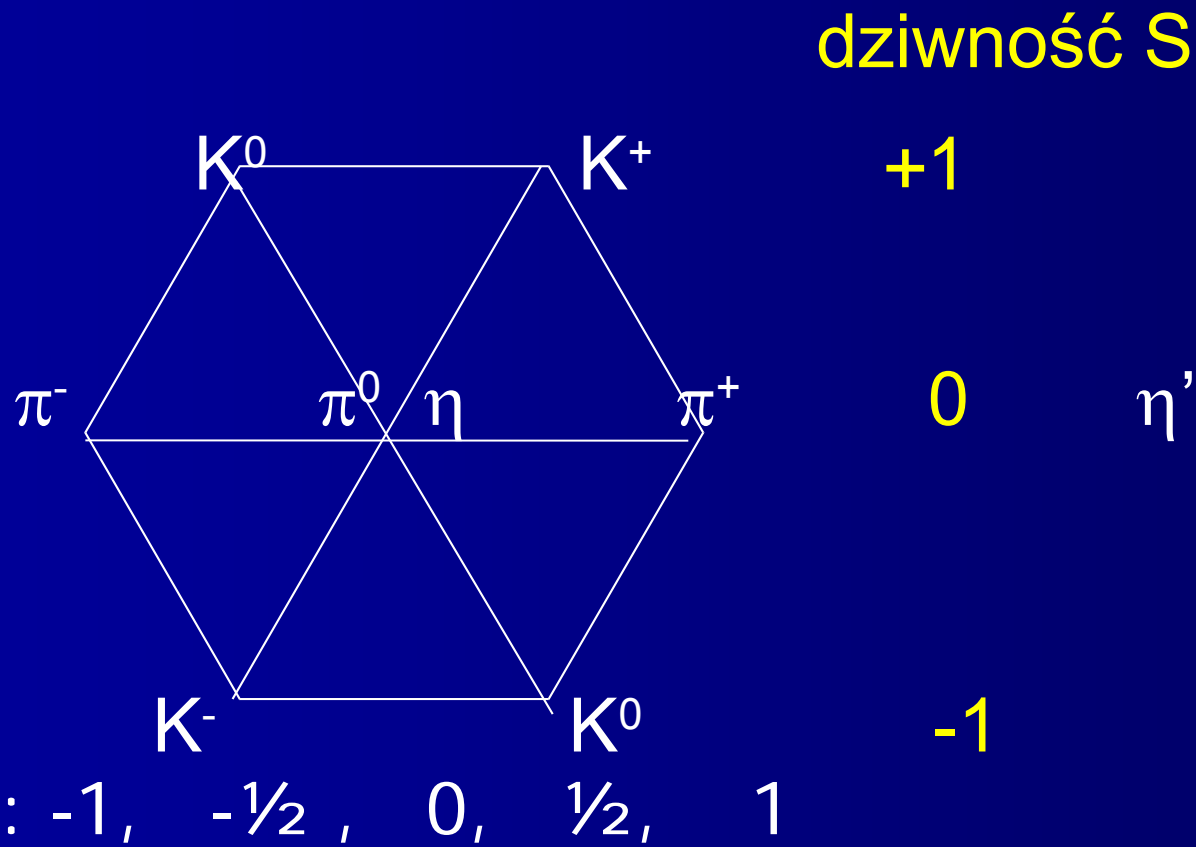
- Earlier used only for classification of particles
(-> *multiplets*)
- From 60' XX – also in the description of interaction

Types symmetries:

- Global and local symmetries (Note: if system has a local symmetry then it has also a global one (NOT vice versa))
- Continuous and discrete (under a continuous (eg. rotation over an arbitrary small angle) and a discrete transformation (eg. reflection off a mirror))

Multiplets of elementary particles

-> quark diagrams



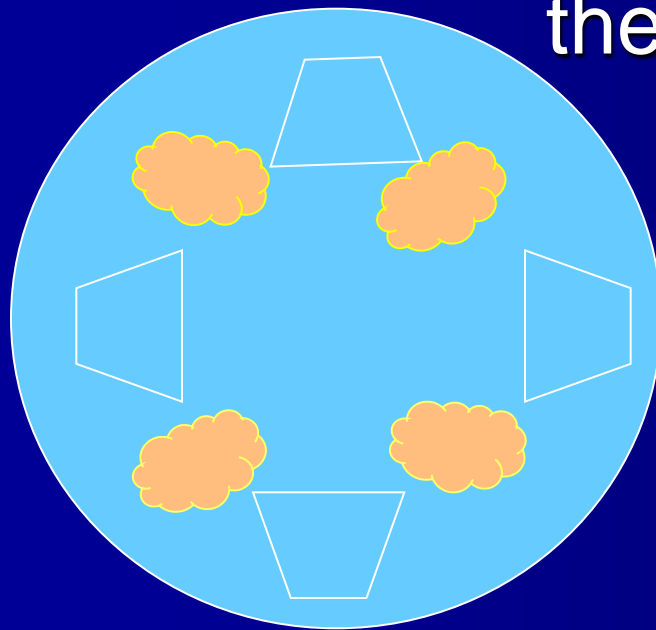
Symmetry and its violation

In physics important are all cases with exact , approximate or hidden symmetries

- Exact symmetry
- Violated (broken) symmetry:
 - dynamically by additional interaction, which does not respect symmetry (typically they are weaker → **symmetry is approximate**)
eg. isotopic symmetry ($p \leftrightarrow n$) for nuclear force, is violated by el-mag. interaction
 - spontaneously, when interaction respects symmetry while physical states not (**symmetry is hidden**).
eg. gravitational force does not depend on direction but Earth's orbit is not circular

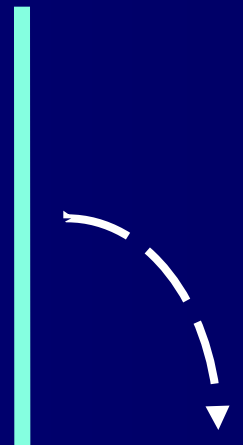
Spontaneous symmetry breaking- examples

- Sitting around the table : take a cake
(left-right?) : if left



then it forces others to
take the left

- Vertical stick – where it fall down ?
All direction good, however one is realised

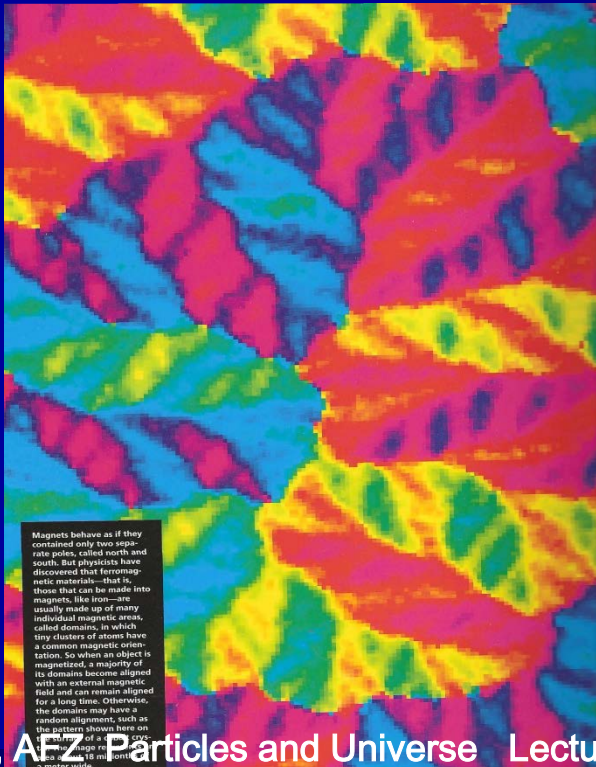


Domens in the metal



Ferromagnetic has domens below the Curie temperature in which atoms have the same direction of the magn. dipoles . (Different in the different domens). However there interaction does not depend on direction. In higher temperature domens disappear.

size 10^{-6} m



C. Suplee, Physics in the 20-th century

Spontaneous symmetry breaking



Structure, or smaller symmetry for lower temperature (smaller energy)

Structure disappears and symmetry grows when temperature rises (higher energy)

Lecture by F. Close

Gauge principle in theory of particle physics

- QED: invariance of wave function under the local change of **phase for the electron** $\psi(\mathbf{x}) \rightarrow \psi(\mathbf{x}) e^{i\theta(\mathbf{x})}$
→ existence of el.- magn field with a massless photon and a particular photon-electron interaction (*a minimal coupling*)
- **Gauge principle** is applied to other fundamental interactions. Invariance of wave function under the local change of **phase for the fundamental fermions**
→ there exist gauge fields with gauge bosons: photon, $W^{+/-}$, Z (*EW interaction*) and gluons (*QCD*).

Description of fundamental interactions – also these beyond the Standard Model - is based on this principle.

Symmetry transformations (groups)

Phase transformations of wave functions
constitute **a group**

there are *rotation group, group of translation...*

E. Noether theorem – with every global, continuous symmetry transformation group conservation laws are connected

Electric charge conservation – arises **from symmetry** of el-magn. interaction under change of

a phase $e^{i\theta}$, $\theta \in \mathbb{R}$

→ group of unitary transformations $U(1)$

Fundamental interactions and local symmetries (groups)

- Electromagnetic:

gauge boson: photon;

group $U(1)_{em}$ ($U(1)_Q$ Q – conserved el. charge)

- Weak (fundamental eg. $d \rightarrow u e^- \text{antineutrino}$ el.)

e-m and weak fundamental: unification = electroweak (EW)

gauge bosons W^+, W^-, Z and photon γ ;

group $SU(2)_{I_{weak}} \times U(1)_{Y_{weak}}$ (I_{weak}, Y_{weak} – conserved quantum numbers)

- Strong (**color**);

gauge bosons – gluons;

group $SU(3)_{color}$

$SU(n)$ - unitary $n \times n$ matrices
with determinant 1

Electroweak interaction -

$$SU(2)_{I_{\text{weak}}} \times U(1)_{Y_{\text{weak}}}$$

I_{weak} – weak isospin (similar to spin $\frac{1}{2}$)

Y_{weak} – weak hypercharge (similar to electric charge)

All fundamental fermions have $I_{\text{weak}} = \frac{1}{2}$

Relation with el. charge Q :

$$Q = (I_{\text{weak}})_3 + Y_{\text{weak}} / 2$$

$(I_{\text{weak}})_3 =$ projection of isospin : $\frac{1}{2}$ lub $-\frac{1}{2}$

Upper fermions (quarks u, c, t ; neutrinos) : $(I_{\text{weak}})_3 = + \frac{1}{2}$

Lower fermions (quarks d, s, b ; e^-, μ^-, τ^-) : $(I_{\text{weak}})_3 = - \frac{1}{2}$

Standard Model

Role of symmetry so large, that we describe a model by writing its groups of symmetry:

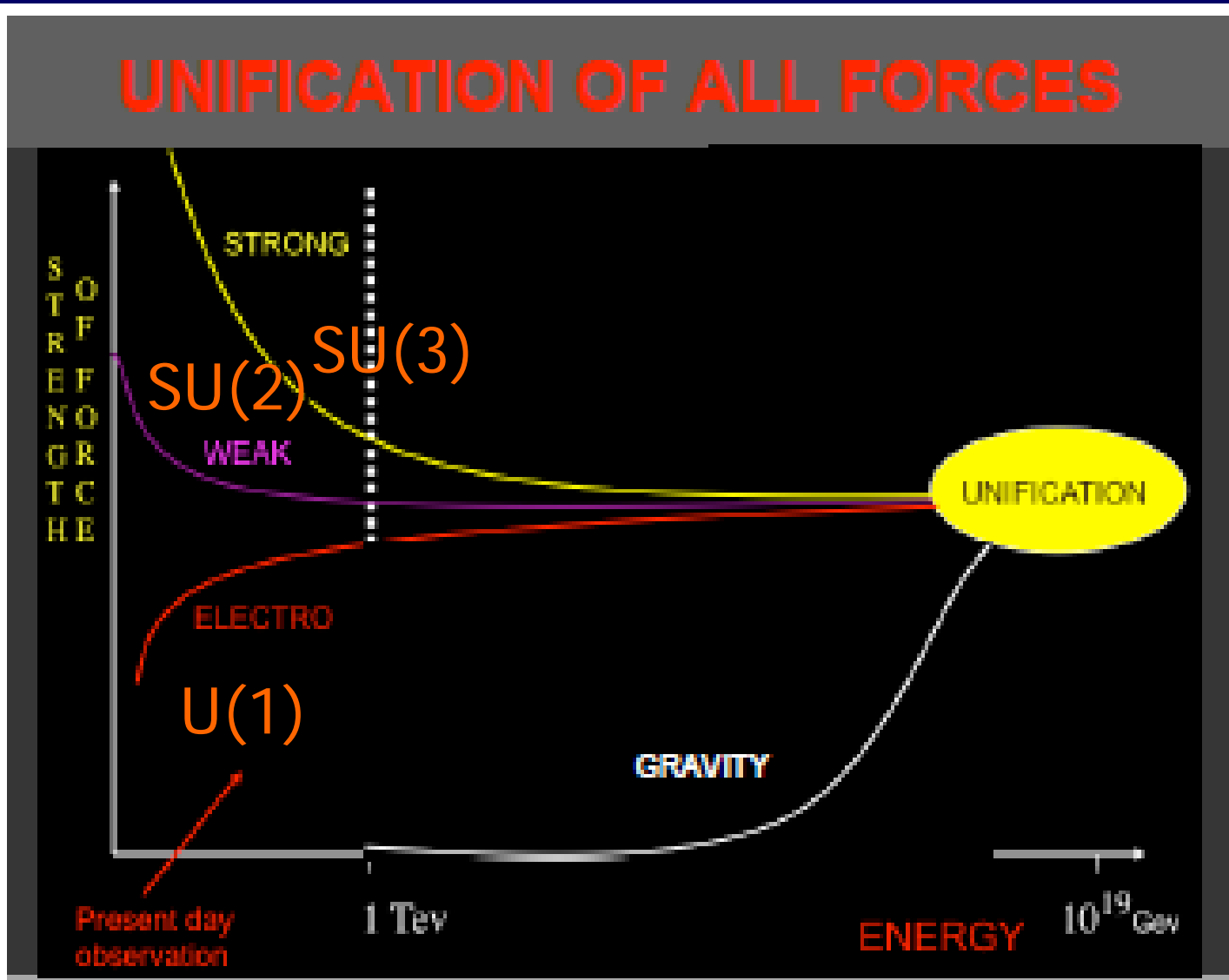
$$SM = SU(2)_{I_{\text{weak}}} \times U(1)_{Y_{\text{weak}}} \times SU(3)_{\text{color}}$$

Where $U(1)_{em}$?

in a product $SU(2)_{I_{\text{weak}}} \times U(1)_{Y_{\text{weak}}}$

wiecej o tym ponizej

D. Gross, Photon 2005



Local symmetry and mass of gauge bosons

Only massless bosons have an infinite range,
however W/Z are massive (80-90 GeV)

*We want to have a local symmetry and massive
gauge bosons !*

HOW?

Generate mass for W/Z

- Massive bosons with spin 1: 3 spin states (-1, 0, +1), massless spin 1 – only 2 (-1 and +1 – as for photon) !
- We need to add fundamental objects to the SM to build longitudinal, 0 polarization states – at least 3
- In SM we add a doublet of spin 0 fields

$$\Phi = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix}$$

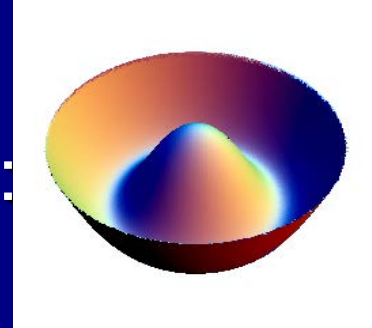
Interacting with W/Z in agreement with gauge symmetry

Spontaneous symmetry breaking

$$SU(2)_{I \text{ weak}} \times U(1)_{Y \text{ weak}} \rightarrow U(1)_{em}$$

Interaction of the doublet Φ :

Potential energy of the system: the lowest state –



a vacuum

Potential for Φ is in the form:

radius –
vacuum

many vacuum states – a symmetry!

parametr v

Choosing one particular vacuum state – spontaneously breaking of the symmetry $SU(2)_{I \text{ weak}} \times U(1)_{Y \text{ weak}}$

- still the symmetry $U(1)_{em}$ holds !

Mass generation in SM

- Brout-Englert-Higgs (BEH) mechanism ~1964
generation of mass for gauge bosons from SSB

Nobel 2013

- In the Standard Model

→ generation of W/Z mass spontaneously

$$\text{mass } W/Z \sim g v$$

g- weak coupling and v- vacuum parameter

→ masses of quarks and leptons similarly

(here additional parameters)

Higgs particle

- Field φ^0 can be decomposed

$$\varphi^0 = v + H$$

where H – represents particle with spin 0
→ the **Higgs boson**.

- Remaining fields from Φ are used to create missing spin states for W^+, W^-, Z

(fields φ^0 and φ^+ are complex → **4 degrees of freedom**)

Prediction **B-E-H** \rightarrow Higgs boson in SM

- Neutral, spin 0, Higgs particle H
- Selfinteraction: λ HHH, λ^2 HHHH
- Mass $M = \sqrt{2\lambda v}$?(unknown); **125 GeV (LHC 2012)**
- Known couplings to $W^{+/-}$, Z and
- to quarks and leptons (Yukawa interaction)



proportional to their mass

- And such that probability of EW processes not larger than 100% - (danger for energy ~ 300 GeV !)

LHC 4.07.2012

- Higgs particle with mass ~ 125 GeV observed at ATLAS+CMS

(+Tevatron)

BROKEN SYMMETRY AND THE MASS OF GAUGE VECTOR MESONS*

F. Englert and R. Brout

Faculté des Sciences, Université Libre de Bruxelles, Bruxelles, Belgium

(Received 26 June 1964)

BROKEN SYMMETRIES, MASSLESS PARTICLES AND GAUGE FIELDS

P. W. HIGGS

Tait Institute of Mathematical Physics, University of Edinburgh, Scotland

Received 27 July 1964

VOLUME 13, NUMBER 16

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19 OCTOBER 1964

BROKEN SYMMETRIES AND THE MASSES OF GAUGE BOSONS

Peter W. Higgs

Tait Institute of Mathematical Physics, University of Edinburgh, Edinburgh, Scotland

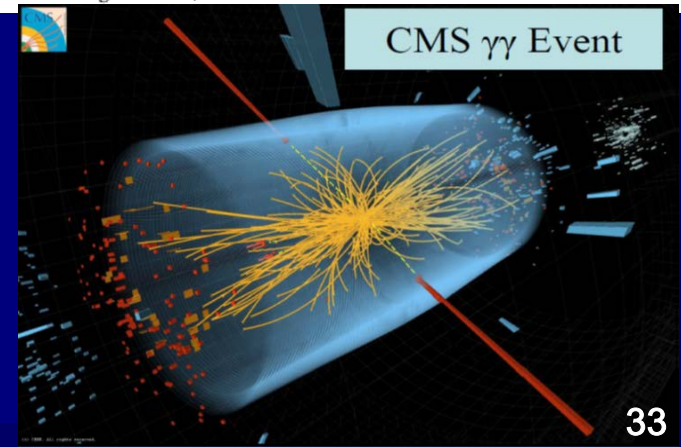
Received 31 August 1964)

GLOBAL CONSERVATION LAWS AND MASSLESS PARTICLES*

G. S. Guralnik,[†] C. R. Hagen,[‡] and T. W. B. Kibble

Department of Physics, Imperial College, London, England

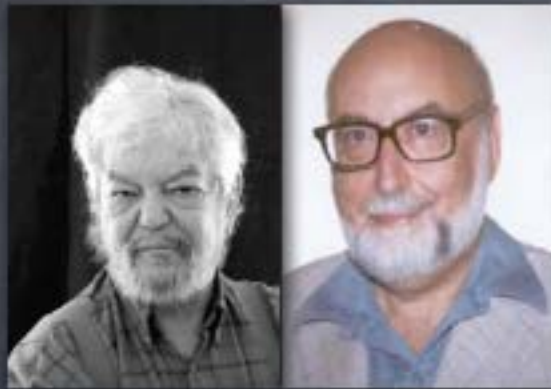
(Received 12 October 1964)



Important loop couplings $ggH, \gamma\gamma H$

2010 Sakurai Prize

... for “elucidation of the properties of spontaneous symmetry breaking in four-dimensional relativistic gauge theory and of the mechanism for the consistent generation of vector boson masses.”



Brout

Englert



Higgs



Hagen

Guralnik

Kibble

PRL 13, 321-323 (1964)

PRL 13, 508-509 (1964)

PRL 13, 585-587 (1964)



Nambu, Nobel 2008

For introduction of SSB to particle physics



Ben Kilminster, ICHEP 2010

2013 NOBEL PRIZE IN PHYSICS

François Englert Peter W. Higgs



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The Nobel Prize in Physics 2013

François Englert and Peter W. Higgs

"for the theoretical discovery of a mechanism that contributes to our understanding of the origin of mass of subatomic particles, and which recently was confirmed through the discovery of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN's Large Hadron Collider"

Discrete symmetry P, C, CP...

Weak interaction sensitive to spin states of particles

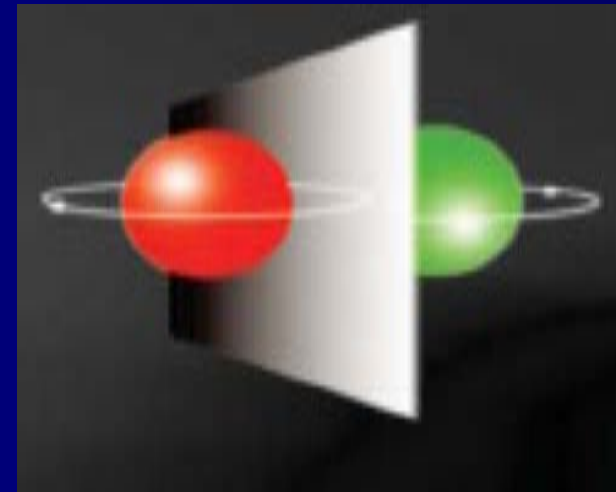
Particle with spin $\frac{1}{2}$ has two spin states $+\frac{1}{2}$ i $-\frac{1}{2} \rightarrow$
R (right) and L (left) particles

Weak interaction acts only between left states !

Yang-Lee 1956

Wu 1957

It means that weak interaction is not symmetric under reflection
(P symmetry, P - parity)
which corresponds to $L \leftrightarrow R$



P, C and CP in the EW interaction

Weak interaction – less symmetry

- **Symmetry P** (reflection): $L \leftrightarrow R$ violated!
- **Symetria C** (charge conjugation): transforms of a particle to an antiparticle (el. charge to the opposite) violated! C transforms neutrino L into antineutrino L, but in nature* antineutrino only right R
- **Combined symmetry CP** (combination of reflection and charge conjugation) transforms L neutrino to R antineutrino – OK! *Landau 1957*
- CP is almost conserved (violation 10^{-4}).
- **Almost makes difference** →
a lack of symmetry
matter - antimatter in the Universe!



Kobayashi and Maskawa



Nobel' 2008

For explaining SSB for matter-antimatter, ie. CP violation in K meson (s quarks) decays in experiment by Fitch-Cronin(1964)

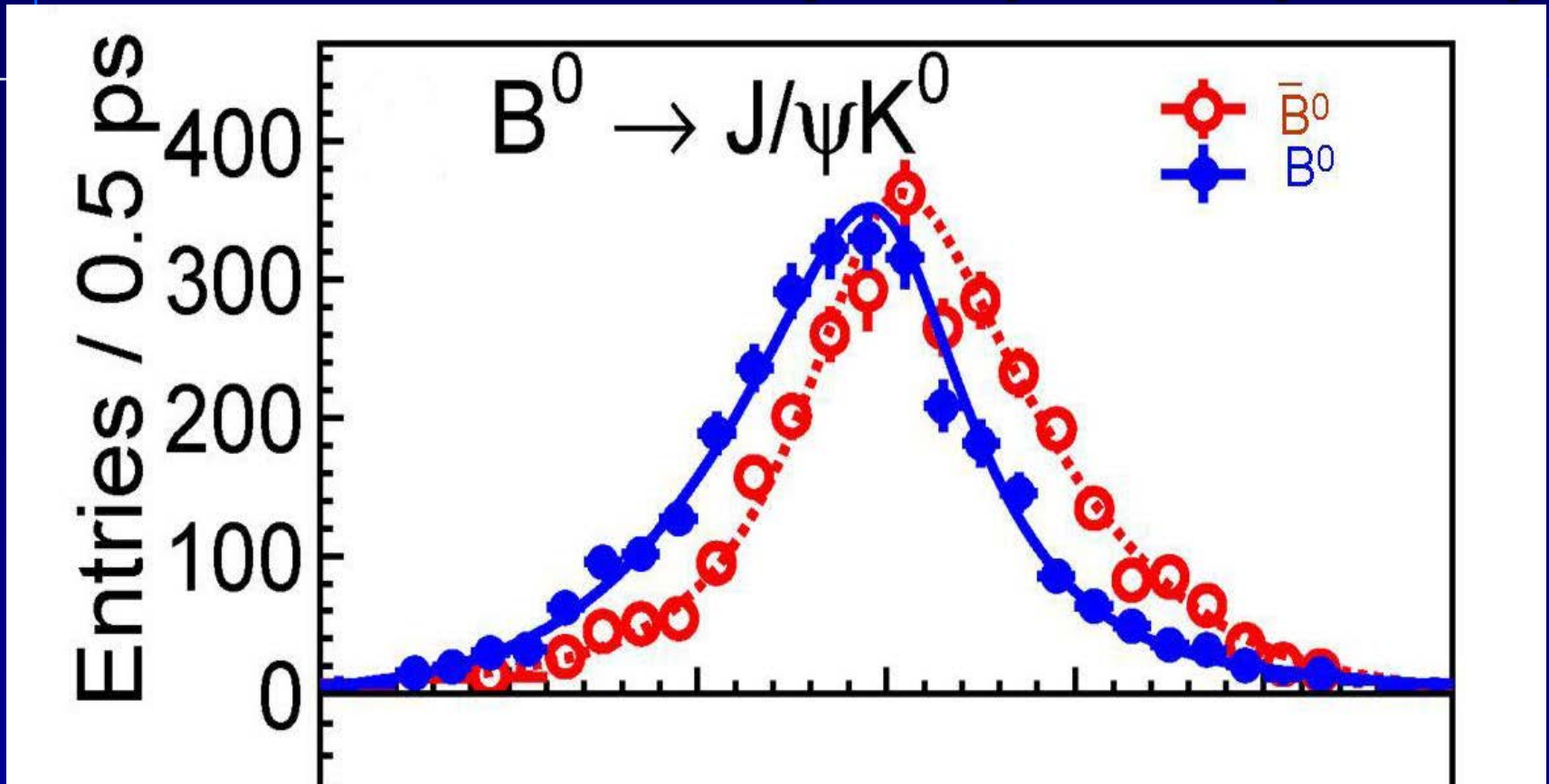
Kobayashi i Maskawa showed in 1973, że that broken of CP can appear if in the nature there exist 3 pairs of quarks.

Then known were only u, d and s quarks! Discovery in 1977 r. b quark from the 3 generation confirms the Kobayashi – Maskawa conjecture.

Full confirmation came when broken CP (eg. difference in decay of particle and antiparticle) observed in b systems.



Asymmetry in decays of mesons: $B(d\bar{b})$ i $\bar{B}(\bar{d}b)$



Discovery of asymmetry:

2001r for B mesons (SLAC USA, KEK Japan)

2011r for D mesons (c quarks) (CERN, Europe)

MATTER - ANTIMATTER

- Asymmetry in matter and antimatter observed in the Universe
- Sacharow's postulate (part of) ~1960:
At beginning of the Universe – symmetry of matter and antimatter , but if C and CP symmetry is broken there may appear a small dominance of matter over antimatter
- During an expansion of the Universe– this small effect yields a present day situation - where antimatter is produced only in the laboratory and in cosmic rays.

more later...

Standard Model in agreement with experiment

- Give two examples of continuous transformations
- Does a global symmetry is a consequence of a local one, or vice versa?
- Is a local symmetry the same as a gauge symmetry?
- Does the symmetry dictate the dynamics??
- Noether theorem describes ...?
- Does the gauge principle apply only to the Standard Model?
- Give two examples of spontaneously symmetry breaking
- How many spin (polarisation) states has massive Z boson ?
- Does in the weak interaction participate a right electron ?
- What is spin of Higgs particle?
- Is Higgs particle interaction stronger with more massive particle?
- Do Higgs particles interact with themselves ?
- For what Y. Nambu got Noble prize?
- What is a Sacharow postulate?