



Particles and Universe

Lecture 12 Beyond SM

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I. Standard Model - problems

II. Beyond SM

Standard Model very successful- however they are problems:

- Many parameters (masses) ~20 *more in other models*
- Why 3 fermion families? *no answer in other models*
- Nonzero mass of neutrinos *easy extension of the SM*

- Hierarchy problem -

$$M_H (\sim 100 \text{ GeV}) \ll M_{\text{Planck}} (10^{19} \text{ GeV})$$


often formulated as difference of the EW ($\sim 1 \text{ TeV}$) and Planck scales

- Gravitation (gravity)?
- Describes 4 % of Universe - no candidate for Dark Matter

Deviation from the SM? Higgs boson as in SM ?

Non-zero neutrino mass

⇒ ograniczenie na masę
neutrina elektronowego:

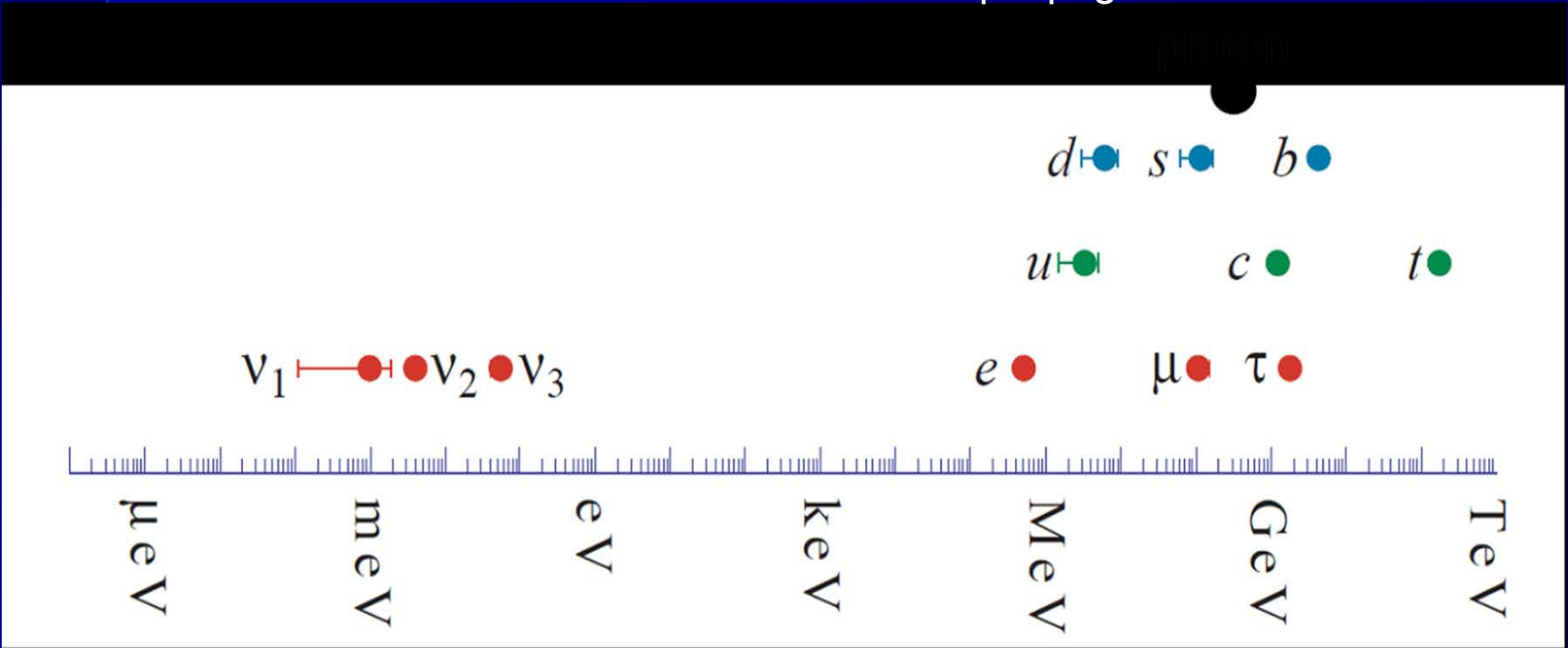
$$m_\nu < 2.2 \text{ eV} \text{ (95\% CL)}$$

- In the SM (neutrino mass **ZERO**)
 - only left neutrinos and right antineutrinos
- However from ~ 2001 we know that neutrinos have masses \rightarrow extra neutrino/ antineutrino states
- For sure weak interaction of these extra states very, very weak (experiments)

- SM extension in the EW sector – with extra SU(2) symmetry for left and right states, and suppression mechanism explaining very small masses of neutrinos (seesaw ..)

Masses of fermions

neutrino.ift.uni.wroc.pl/?page=Neutrina/neutrina.html



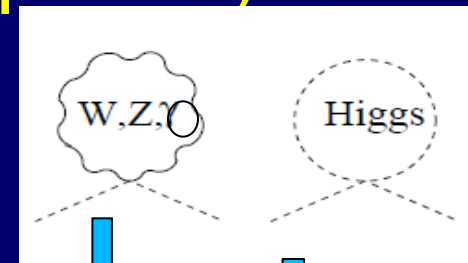
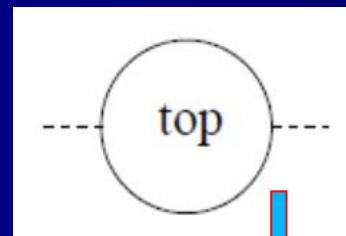
Hierarchy problem in the SM

- SM works at present energies – up to which energy (Λ) can we apply it?
- Quantum corrections to the Higgs mass - loops with arbitrary large energies.
- If we include contributions only up to energy Λ (cut –off)
- Corrections to the Higgs mass (squared)

$$\sim \{\text{couplings}^2\} \times \Lambda^2$$

For $\Lambda = 10 \text{ TeV}$

and mass $\sim 200 \text{ GeV}$



$$m_h^2 = m_{tree}^2 - [100 - 10 - 5] (200 \text{ GeV})^2$$

Fine-tuning for SM

- 10 TeV

$$m_h^2 = m_{tree}^2 - [100 - 10 - 5] (200 GeV)^2$$

1/100 fine tuning

- $\Lambda = 1 \text{ TeV}$ no fine tuning (SM natural)

$$-\frac{3}{8\pi^2} \lambda_t^2 \Lambda^2 \sim -(2 TeV)^2$$

from the top loop,

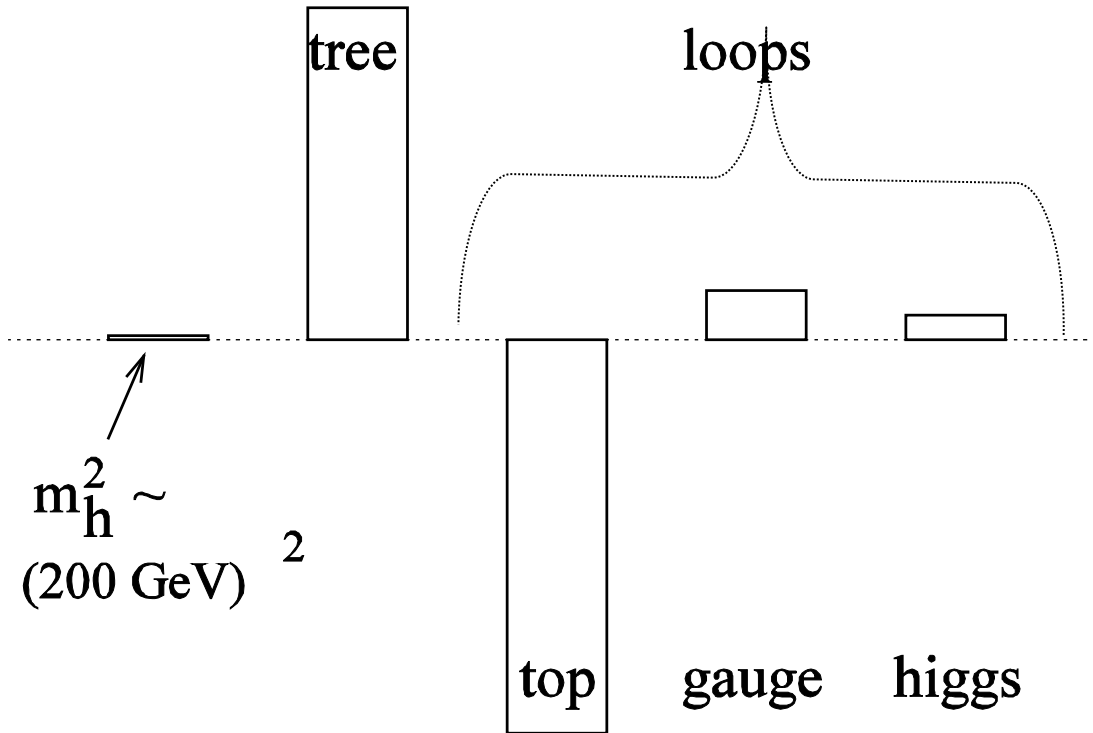
$$\frac{1}{16\pi^2} g^2 \Lambda^2 \sim (700 GeV)^2$$

from the gauge loop, and

$$\frac{1}{16\pi^2} \lambda^2 \Lambda^2 \sim (500 GeV)^2$$

from the Higgs loop. Thus

Fine tuning for $\Lambda = 10 \text{ TeV}$



Schmaltz'
2000

Fine tuning in the SM \rightarrow new physics

In LHC energy ~ 10 TeV (Λ)

fine tuning 1/100

\rightarrow new physics expected:

new particles and/or new interactions

Gravitation

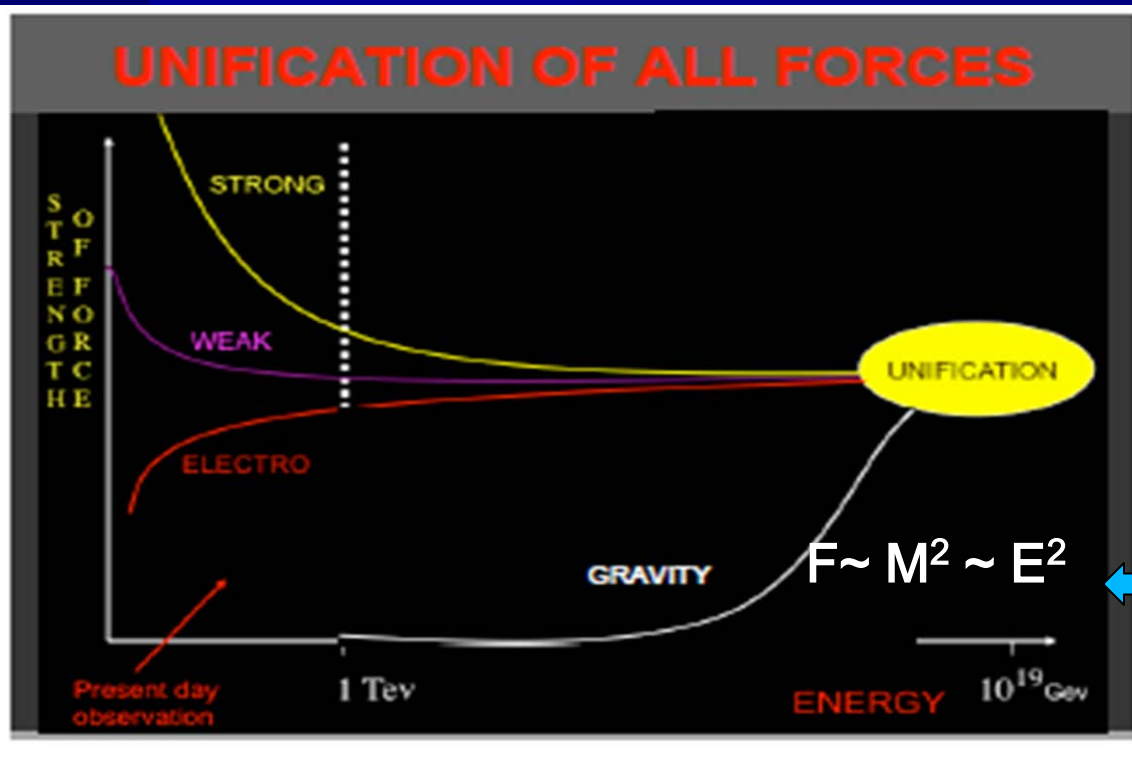
- New physics - gravitation?
- Gravitation- very weak for small energies. It is strong at very large energies
→ „strength” equal to other couplings for

Planck energy

David Gross: The Coming
Revolutions
in Theoretical Physics

[http://www.youtube.com/
watch?v=AM7SnUlw-
DU&feature=channel](http://www.youtube.com/watch?v=AM7SnUlw-DU&feature=channel)

Newton law



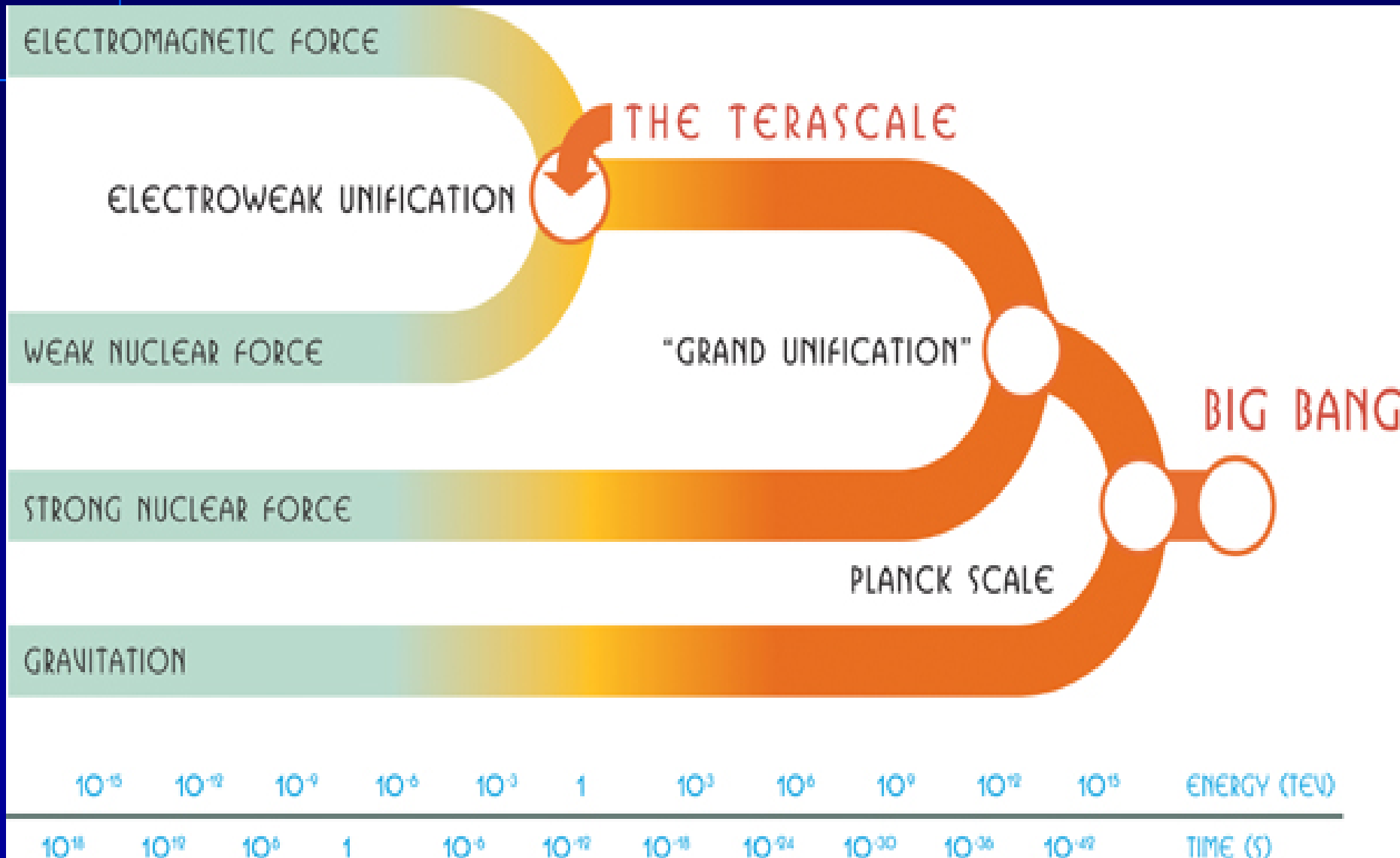
Beyond SM → towards unification

- Standard Model: gauge symmetry $SU(2) \times U(1) \times SU(3)_c$
EW: $SU(2) \times U(1)$ → partial unification of weak and e-m interactions
- **Grand Unified Theory – GUT** (various models)
→ unification of EW and strong interaction.
Gauge symmetry GUT acts at energies above 10^{15-16} GeV.
- In fundamental description of gravity → Planck scales:
Planck mass 1.2×10^{19} GeV
Planck length 1.6×10^{-35} m
- **Theory of Everything** - full unification of interactions
(together with gravity)

J. Lukierski: Od Modelu Standardowego do teorii M: Teorie Wszystkiego

<http://postepy.fuw.edu.pl/zjazdy/Gdansk2003/PF404Lukierski.pdf>

UNIFICATION WITH GRAVITATION AND EARLY UNIVERSE



Beyond the Standard Model

1/ Extension of symmetry

→ supersymmetry

2/ Extension of space-time

→ extra space dimensions

3/ Extension of size of particles

→ extended fundamental particles
(strings, membrans and p-brans)

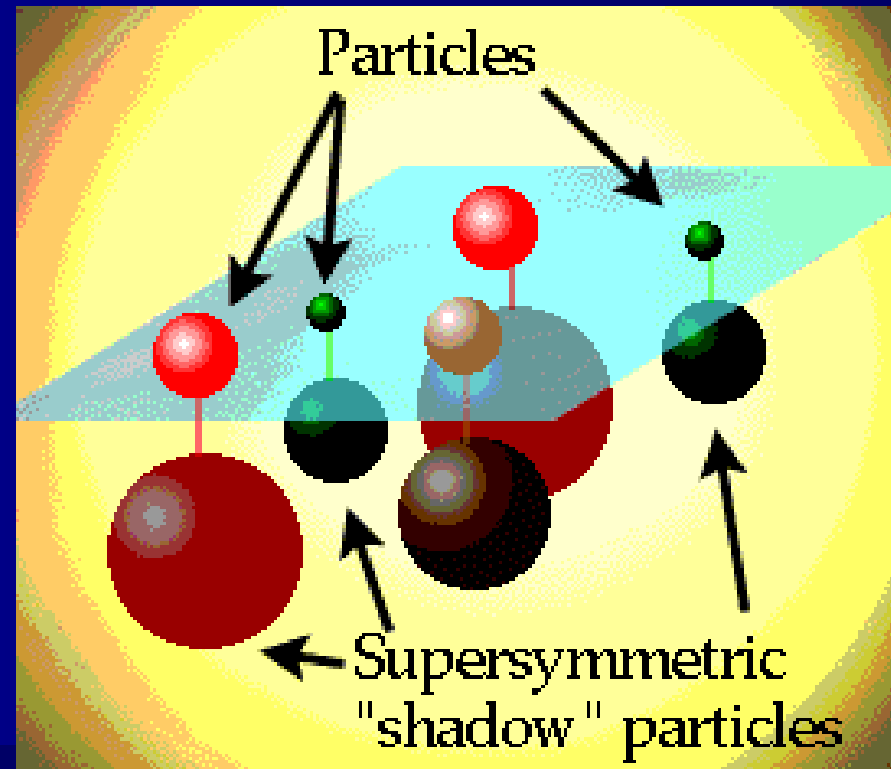
Towards the Theory of Everything (TOE)

(almost no works on substructure₁₂.)

SUPERSYMMETRY

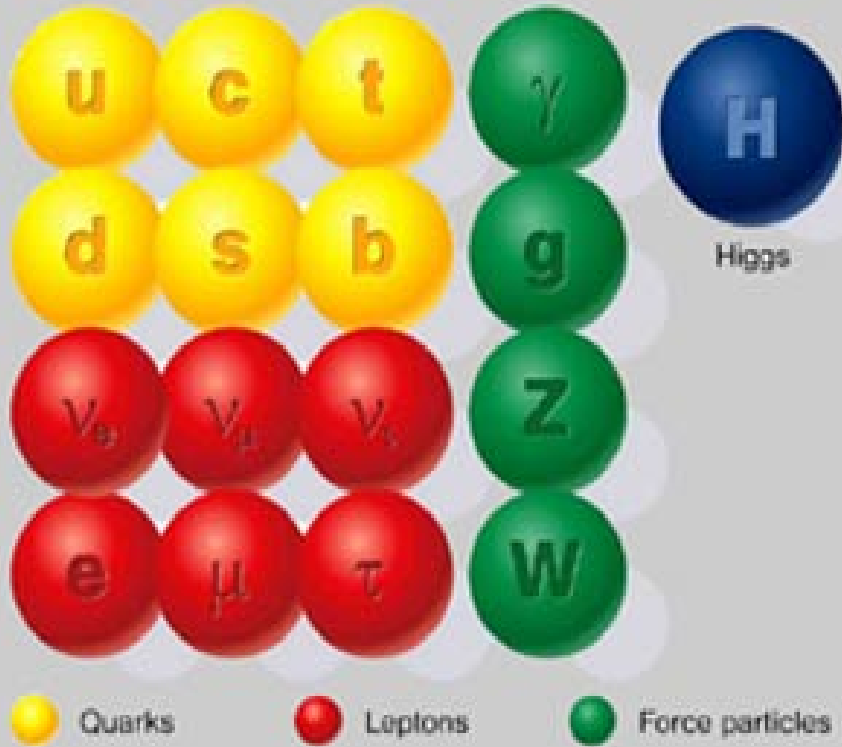
- In Nature only two types of particles: fermions and bosons
- In Supersymmetry there is a symmetry **fermion** \leftrightarrow **boson**, so doubling of fundamental particles is assumed
- Supersymmetric partners of all known SM fundamental particles = **SUSY particles**

However SUSY particles have to be very massive- we do not see them (even at LHC) !
Supersymmetry must be violated !

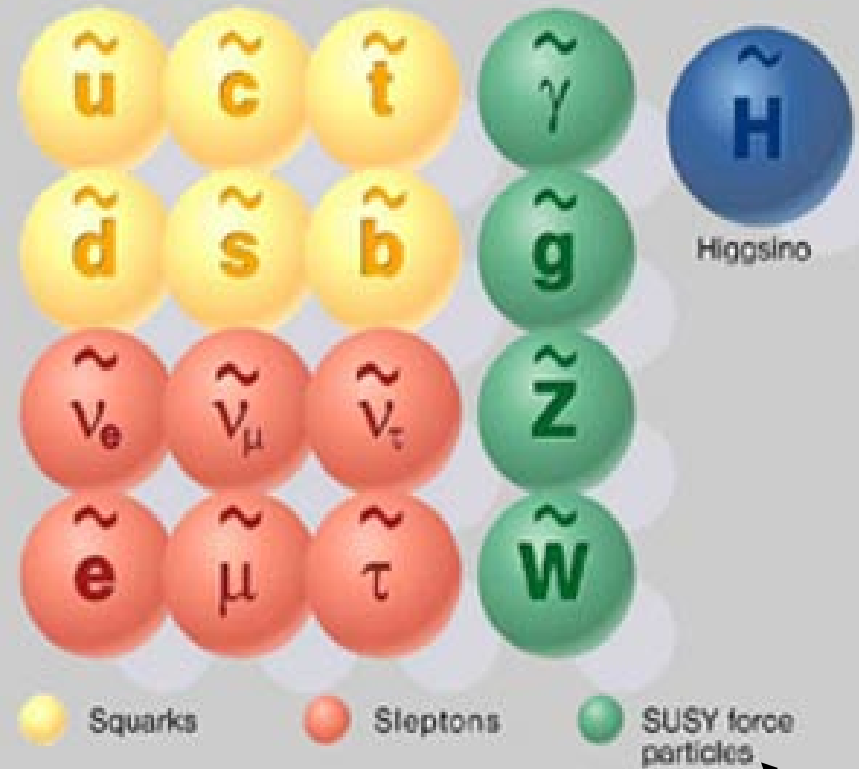


SUSY particles

Standard particles



SUSY particles



skwarki, sleptony, gaugina, higgsino
 spin 0 spin 1/2

Masses ~ 1 TeV?

Two spin 0 doublets Φ_1 and Φ_2

Supersymmetry is super

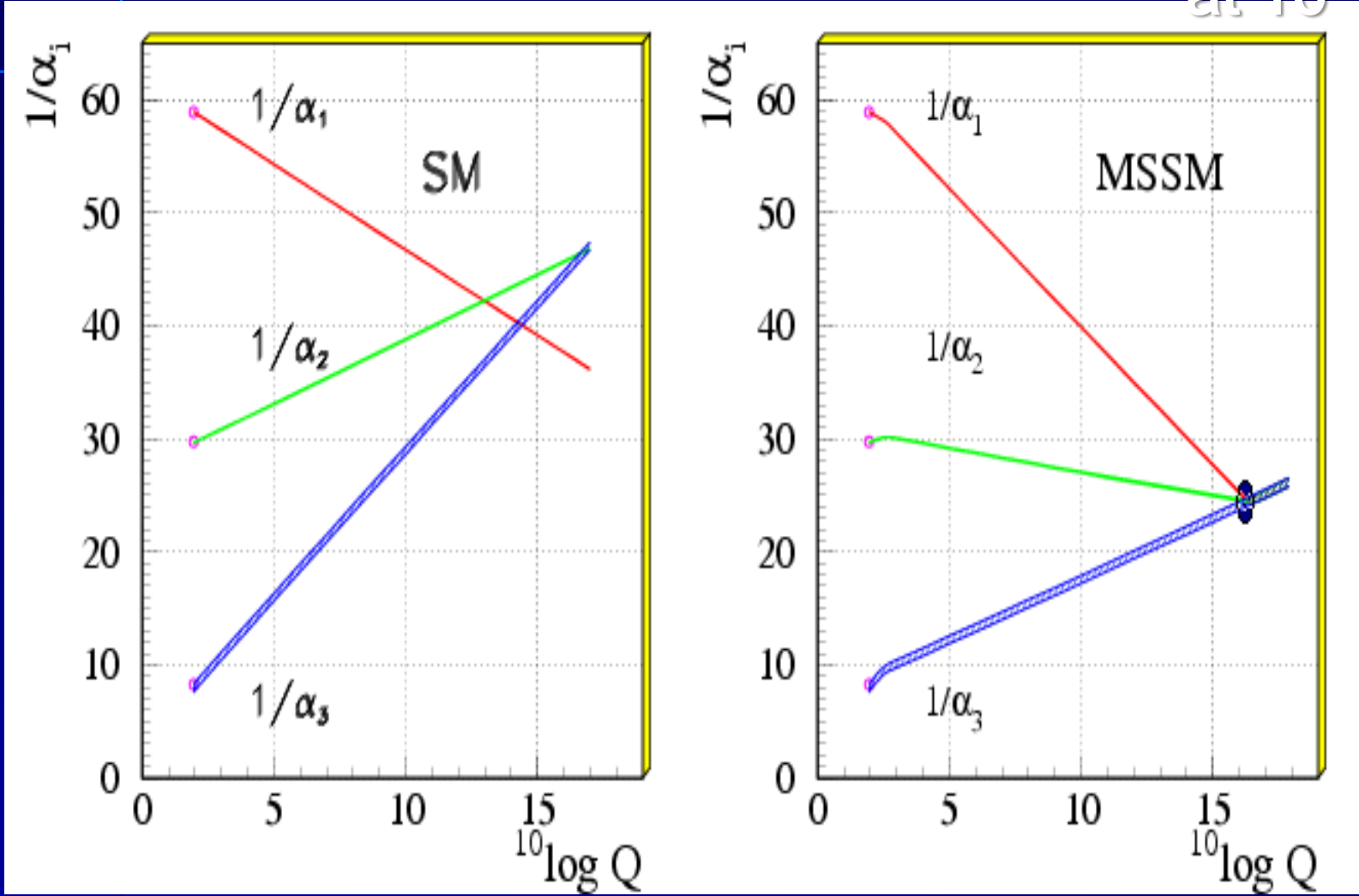
- Hierarchy ?– no problem here (almost), since cancelation of fermionic and bosonic loops



- Unification of interaction(GUT): better than in SM
- Prediction: SM-like Higgs particle with mass below 135 GeV
- Additional assumption: **R symmetry**
(and conservation of additive quantum number **R** for SUSY particles), then the lightest neutral SUSY particle is stable → **dark matter candidate**

Unification of forces(couplings) in SM and MSSM (Minimal Supersymmetric Standard Model)

at 10^{16} GeV



axis y: from top $1/\alpha_{U(1)}$, $1/\alpha_{SU(2)}$, $1/\alpha_{SU(3)}$; axis x: log of energy Q/GeV

MSSM – Higgs sector

- **Two** doublets with spin-0 fields to generate masses of fundamental particles
- Prediction: existence of 5 Higgs particles (spin 0)
h, H, A (neutral) i H[±] (charged)
Note - h has properties as the SM Higgs particle,
that why LHC does not exclude MSSM !
But no SUSY particle seen....
- **Higgsino** - spin 1/2
Gauginos (spin 1/2: *photino, gluino, wino, zino*) mix with higgsino →
neutralinos (neutral) and **charginos** (charged)
→ **DM particle**

SUPERSYMMETRY

D. Gross

Discovery of supersymmetry -
discovery of quantum dimension of space-time
(in addition to normal coordinates there are non-commuting ones)

Natural and unique extension of relativistic
symmetries of nature

LHC - two main directions of searches:
Higgs and SUSY particles
No signal of SUSY yet...

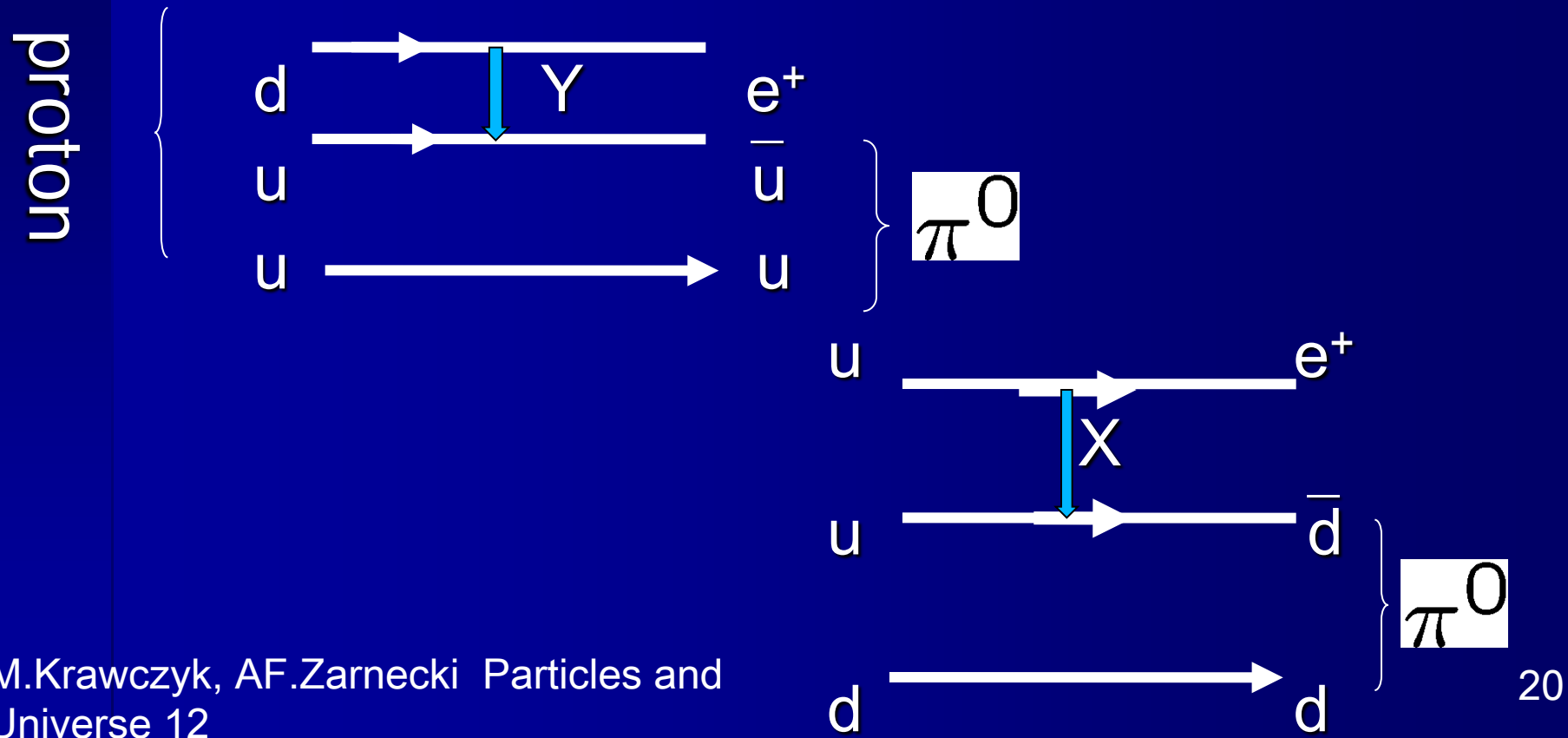
First Theory of Grand Unification :SU(5)

- Gauge symmetry SU(5) - it contains SM symmetry SU(2)xU(1)xSU(3) – idea in 1974 by Glashow, Georgi
- In multiplets of SU(5) they are both quarks and leptons so they can transform to each other !
(nonconservation of baryonic B and leptonic quantum number L!)
- 12 color gauge bosons (leptoquarks):
 X (el. $-1/3$) ; Y ($-4/3$)
plus gluons, photon, W/Z – in total 24 gauge bosons
- 3 families of fermions(15 states) eg. for right states
5-plet= $(d_R, d_G, d_B, e^+, \bar{\nu}_e)$, there are also 10-plets (u)
- In this model quantisation of el.charge.:
charge of electron = - charge of proton

Proton decay $p \rightarrow e^+ \pi^0$ in $SU(5)$

Proton decays with exchange of X/Y bosons too fast \rightarrow
 life time of proton 10^{30-31} y , however experiment $>10^{31-33}$ y
 - that why this model has been rejected

Example of processes with exchange of X/Y



KALUZA-KLEIN THEORY

First theory with extra dimensions (compact) ; unification of gravity and electromagnetism



(1919-21) If space-time is dynamical there might exist new, curled up, spatial dimensions.

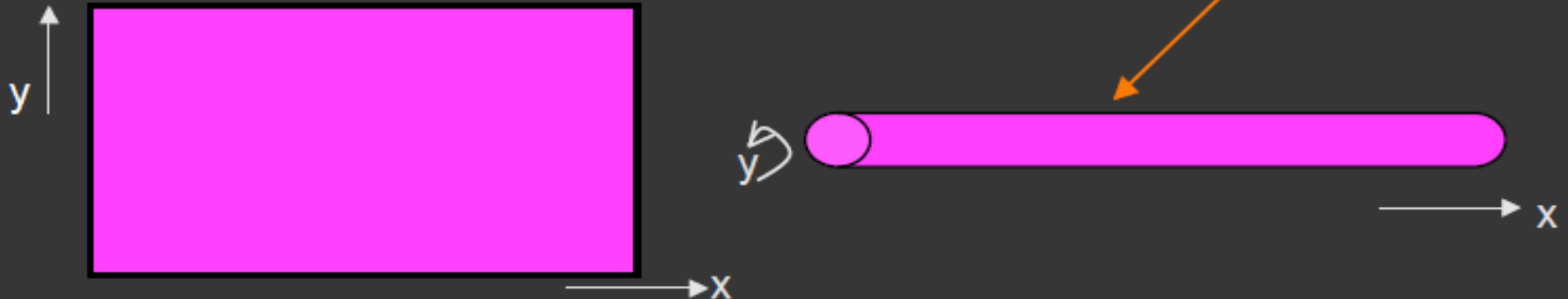
Klein 1926 (quantum)

In April 1919 Kaluza noticed that when he solved Einstein's equations for general relativity using five dimensions, then Maxwell's equations for electromagnetism emerged ..



Einstein was fascinated by this idea and came back to it over and over again---for over 30 years.

Can explain E&M as an effect of gravity in 5 dimensions



New idea – 1998 Arkani-Hamed, Dimopoulos, Dvali

large extra dimensions

Assumption: Gravity and EW interaction may have similar strength already for energy $\sim 1-10$ TeV!

Since gravity was studied (tested) up to distance of 1 cm (what about 1 cm down to 10^{-33} cm ???)

Newton law can be modified, eg.

$$1/r^2 \rightarrow 1/r^4$$

the weak scale, which we take as the only fundamental short distance scale in nature. The observed weakness of gravity on distances $\gtrsim 1$ mm is due to the existence of $n \geq 2$ new compact spatial dimensions large compared to the weak scale. The Planck scale $M_{Pl} \sim G_N^{-1/2}$ is not a fundamental scale; its enormity is simply a consequence of the large size of the new dimensions. While gravitons can freely propa-

with two extra curled (compact) space dimensions

Idea: particles of SM live in 4 dimensions (3+1), while graviton in extra dimensions

M. Shifman <http://arxiv.org/pdf/0907.3074v2.pdf>

Superstrings

- Theory of Everything TOE - all interaction including gravity
 - In quantum field theory – interactions are pointlike, this leads to infinities
- **Superstrings** – example of TOE. Pointlike particles are replaced by **strings with finite length**.
- Planck scales are relevant $l_{Pl}=1.6 \cdot 10^{-35}$ m, $M_{Pl}=1.2 \cdot 10^{19}$ GeV
- Various excitation of strings → different fundamental particles (open and closed strings)
- **Superstrings** – renormalized theory in 10 (or 26 for nonsupersymmetric strings) dimensions
- Parameter described strings α' - the same as for hadronic strings (*see below*)
- Superstrings – no clear predictions and many versions

THE ACHIEVEMENTS OF STRING THEORY

- A Consistent, Logical Extension of the Conceptual Framework of Physics

REVOLUTIONS IN PHYSICS

Relativity	c	Velocity of light
Quantum Mechanics	h	Quantum of action
String Theory	G	Planck length

- A Consistent and Finite Quantum Theory of Gravity
- A Rich Structure That Could Yield a Unique and Comprehensive Description of the Real World (a T.O.E)

There are other opinions as well

M. Veltman (Facts and Mysteries in Elementary Particle Physics, 2003):

..this book is about a physics, and this implies that the theoretical ideas discussed must be supported by experimental facts. Neither supersymmetry nor string theory satisfy this criterion. They are figments of the theoretical mind.

To quote Pauli: „They are not even wrong.”

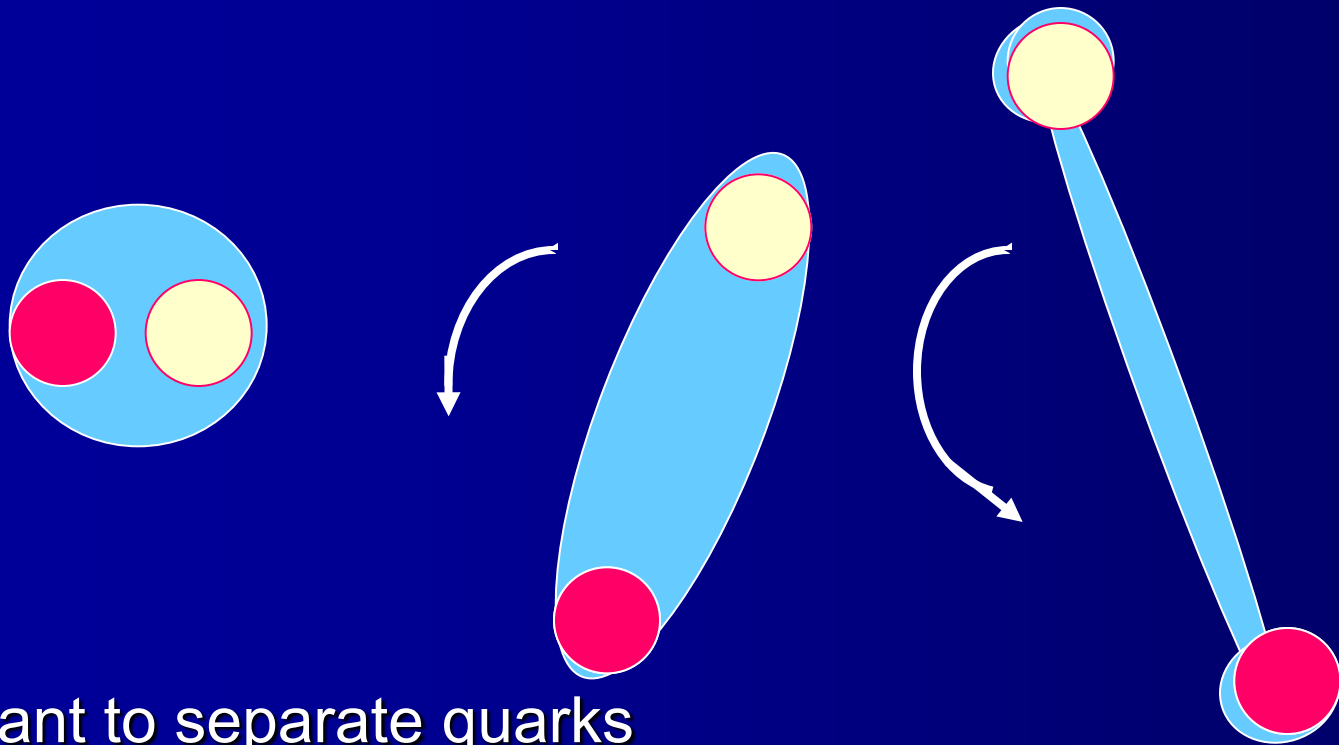
They have no place here.

Questions to lecture 12

- Write 3 problems of the SM
- What is a meaning of GUT?
- GUT – is this a common (unified) description of all fundamental interaction including gravity?
- What is energy of GUT?
- Has supersymmetry been discovered ?
- How many Higgs particles is predicted in the MSSM?
- Is life time of the proton predicted in the SU(5) in agreement with experiment?
- Is the baryonic number conserved in SU(5) ?
- Do exist models with more than 4 space-time dimensions?
- What is main idea of superstring theory?
- Does the superstring theory include gravity?
- What is the parameter of the superstring theory existing in the hadronic interactions?

Gluonic String

- Inside hadrons



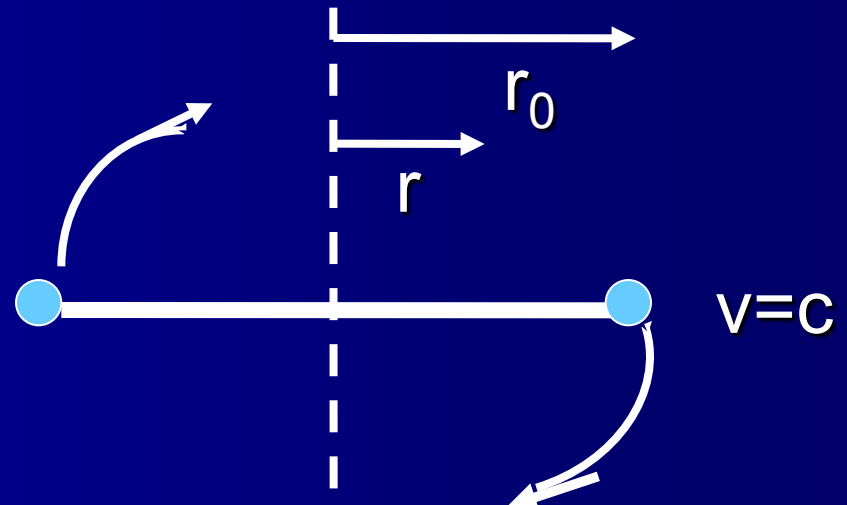
- If we want to separate quarks

→ gluonic string, excitations – higher masses and spins of hadrons

Spin of hadron = total angular momentum of string

- Total angular momentum $J =$
orbital angular momentum $L +$ spin of quarks

- L for string



Result: $J = \alpha' E^2 + \text{const}$

Slope $\alpha' = 1/(2\pi k\hbar c)$

Exp $\alpha' = 0.93 \text{ GeV}^{-2} \rightarrow$ density of energy $k = 0.87 \text{ GeV fm}^{-1}$

Perkins Introduction to High Energy Physics

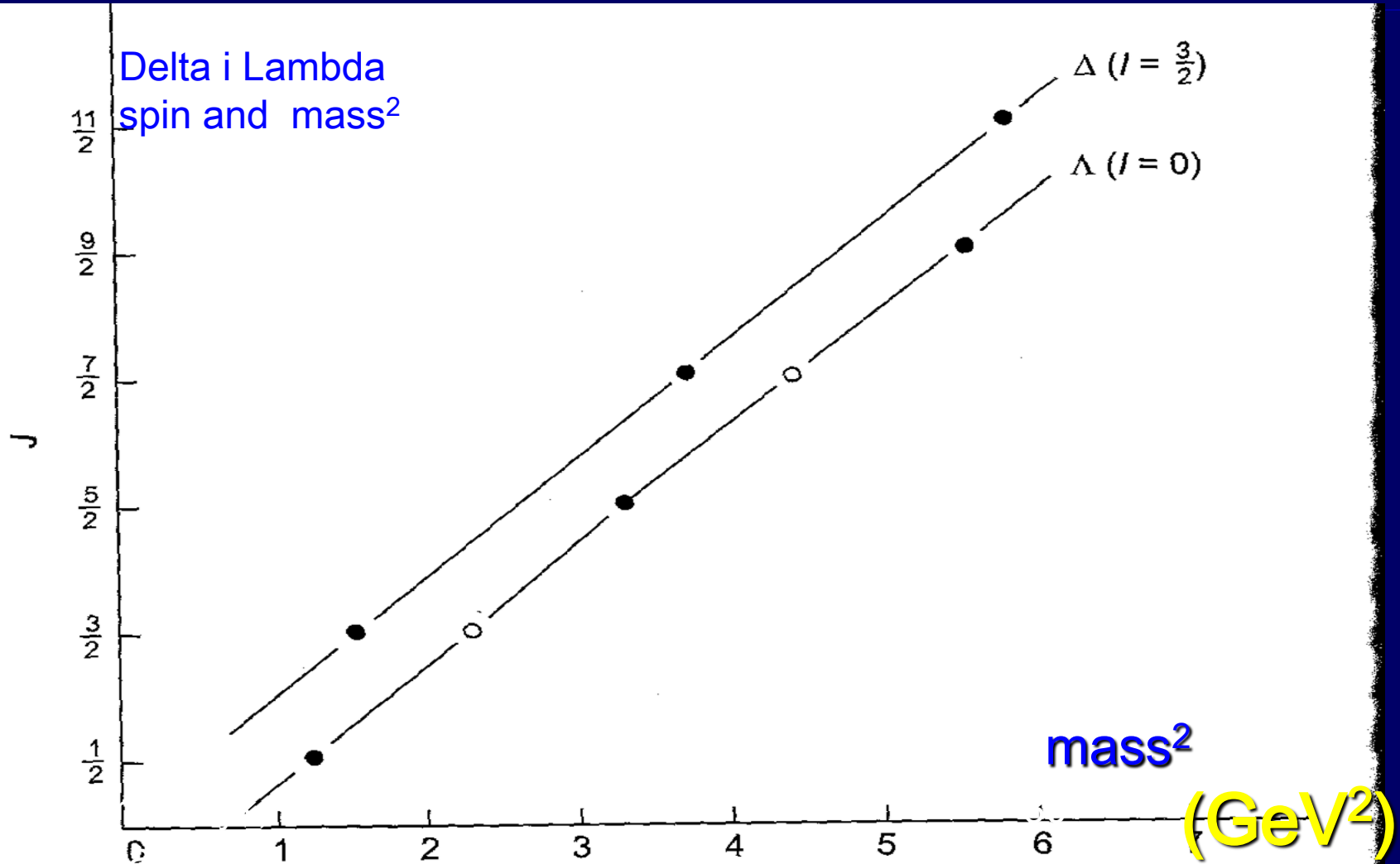
Spectra of hadrons

→ Regge trajectories

The gluonic string model → linear relation between mass squared and spin of particles observed for hadrons – both baryons and mesons.

Linear relation → Regge trajectories for groups of hadron with the same isospin (and the quantum numbers) but different masses and spins

Regge trajectory $J=J_0+\alpha'm^2$ here for baryons (isospin 3/2 i 0)



Model struny gluonowej

(wg D. Perkins, *Wstęp do fizyki wysokich energii str.* 178-9)

- Gęstość energii na jednostkę długości struny = k
- Na końcach struny dwa (w przybliżeniu) bezmasowe kwarki (q i \bar{q}) wirują z prędkością $v = c$
- Prędkość liniowa elementu struny w odl. r od środka wynosi

$$v/c = r/r_0$$

- Energia (masa) struny (całka od $r=0$ do $r=r_0$)
$$E=mc^2=2\int_0^{r_0} k dr (1-v^2/c^2)^{-1/2} = kr_0\pi$$

- A moment pędu

$$L=2/\hbar c^2 \int_0^{r_0} k r v dr (1-v^2/c^2)^{-1/2} = kr_0^2\pi/2 \hbar c$$

Czyli dla struny istnieje zależność: $J=\alpha'E^2 + \text{const}$

Nachylenie $\alpha'=1/(2\pi\hbar c)$ - z doświadczenia: $\alpha' = 0.93 \text{ GeV}^{-2} \rightarrow$

$k=0.87 \text{ GeV fm}^{-1}$

Oszacowanie np. dla protonu: energia układu=masa hadronu, tu $\sim 1 \text{ GeV}/c^2$, promień 1 fm, stąd gęstość energii $k \sim 1 \text{ GeV fm}^{-1}$