

# Production of Inert Scalars at the LHC and the high energy $e^+e^-$ colliders

Aleksander Filip Żarnecki



Faculty of Physics, University of Warsaw

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This presentation is based on the results presented at the conference "**Scalars 2015**" (December 03-07,2015) by

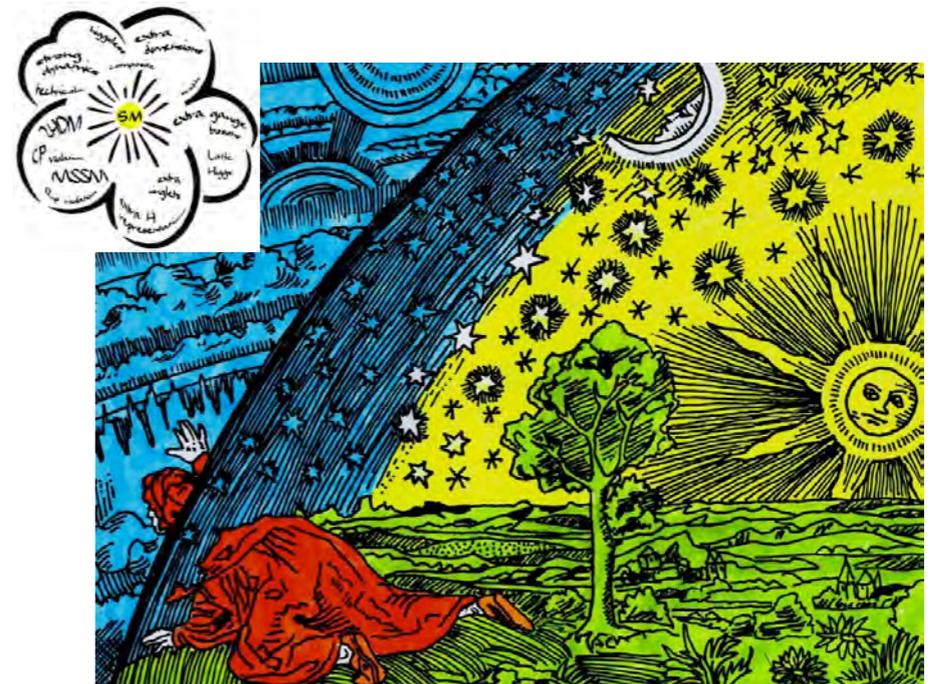
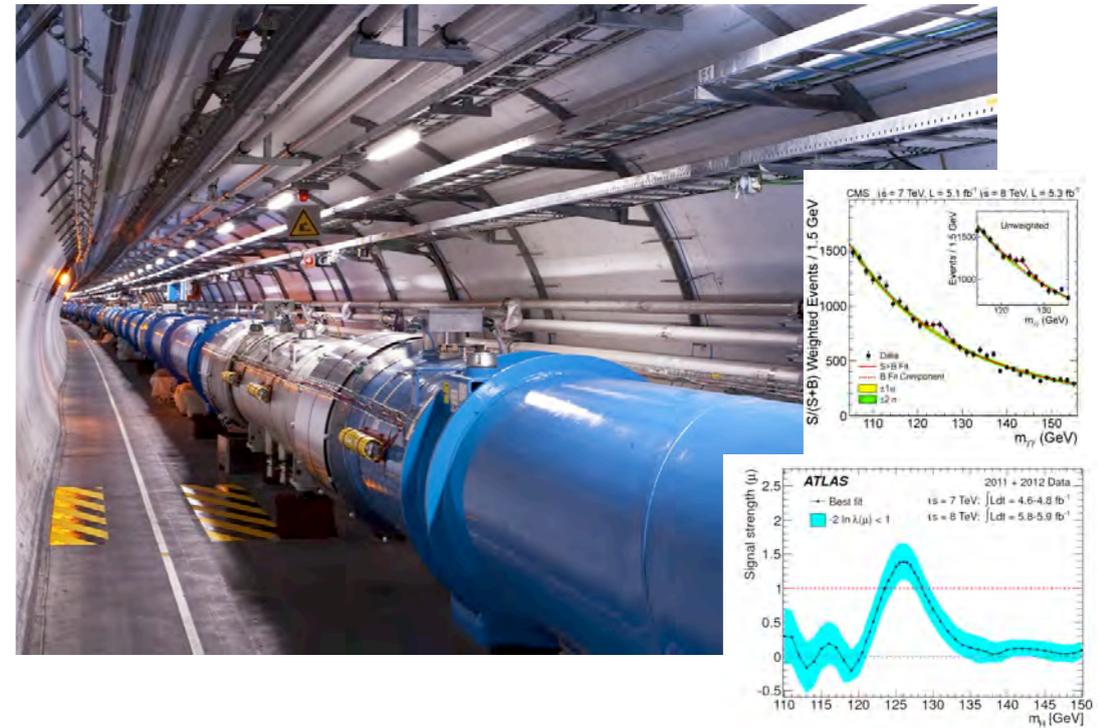
- Sabine Kraml (LPSC Grenoble)  
Recasting LHC searches: the case of the Inert Doublet Model and other examples  
based on work with/of D. Barducci, G. Belanger, S. Bein, G. Chalons, E. Conte, C. Delauney, B. Dumont, B. Fuks, B. Herrmann, A. Goudelis, S. Kulkarni, S. Pandey, S. Sharma, D. Sengupta, C. Wymant
- Tania Robens (IKTP, TU Dresden)  
The Inert Doublet Model in the light of LHC and astrophysical data  
based on work with A. Ilnicka and M. Krawczyk  
arXiv:1505.04734, arXiv:1508.01671, arXiv:1510.04159
- Saereh Najjari (University of Warsaw)  
Production of Inert Scalars at the  $e^+e^-$  Linear Colliders  
based on work with Majid Hashemi, Maria Krawczyk and AFŻ  
arXiv:1512.01175

- 1 Introduction
- 2 Inert Doublet Model (IDM)
- 3 IDM @ LHC
- 4 IDM @ high energy  $e^+e^-$  colliders
- 5 IDM mass reconstruction

# Introduction

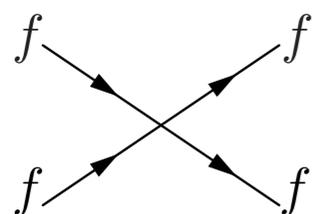
# The LHC endeavor

- The LHC was built as a **discovery machine** to explore new physics at the **TeV energy scale**.
- The discovery of a Standard Model (SM)-like **Higgs boson** was a tremendous first success for the LHC physics program.
- However, while the Higgs discovery completes our picture of the SM, it still leaves **many fundamental questions open** (naturalness, hierarchy problem, ... )
- **Run 2** of the LHC just started; the search for new phenomena **beyond the SM (BSM)** is one of its top priorities.
- The BSM theory might also provide the **dark matter (DM)** and generally enhance our understanding of the early Universe.

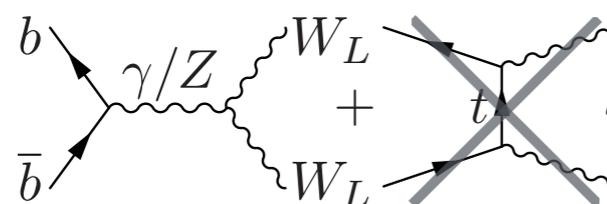


## No more no-loose theorem

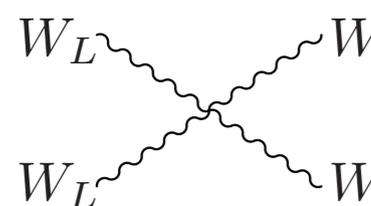
Guaranteed discoveries in the history of HEP (unitarity of scattering amplitudes):



$\sim G_F E^2 \simeq E^2 / v^2 < 16\pi^2 \longrightarrow m_W < 4\pi v$



$\sim g_W^2 E^2 / m_W^2 < 16\pi^2 \longrightarrow m_t < 4\pi v$



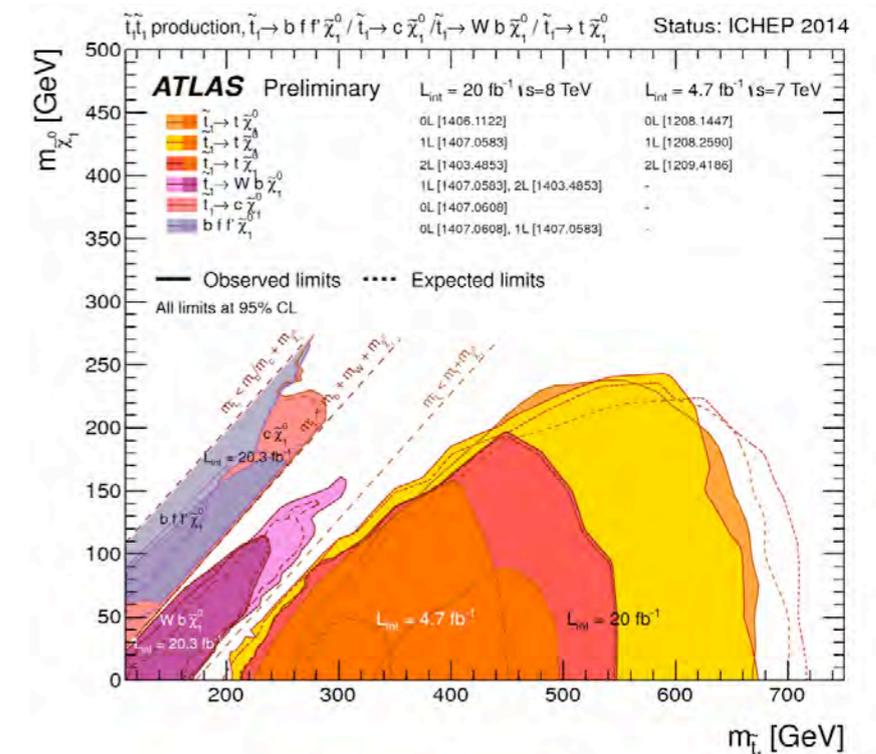
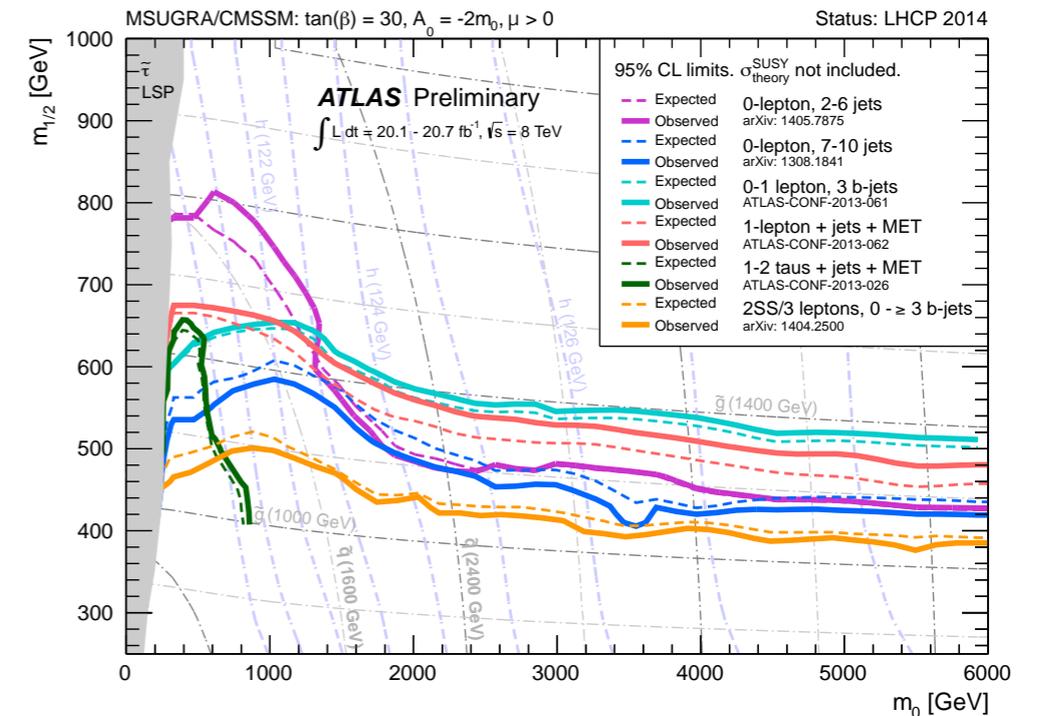
$+ \dots \sim g_W^2 E^2 / m_W^2 < 16\pi^2 \longrightarrow m_H < 4\pi v \quad \sim 3 \text{ TeV}$

The Higgs discovery completes the SM — and leaves us without any no-loose theorem to exploit for future discoveries.



# New physics searches

- ATLAS and CMS perform **searches for new physics in many different channels.**
- In the experimental publications, the **results are typically interpreted within popular models** as well as within topology-based “Simplified Model Spectra” (SMS).
- SUSY, VLQ, extra gauge bosons, DM models, other exotics, extra Higgses, etc.
- However, there **exists a plethora of models** and scenarios ....



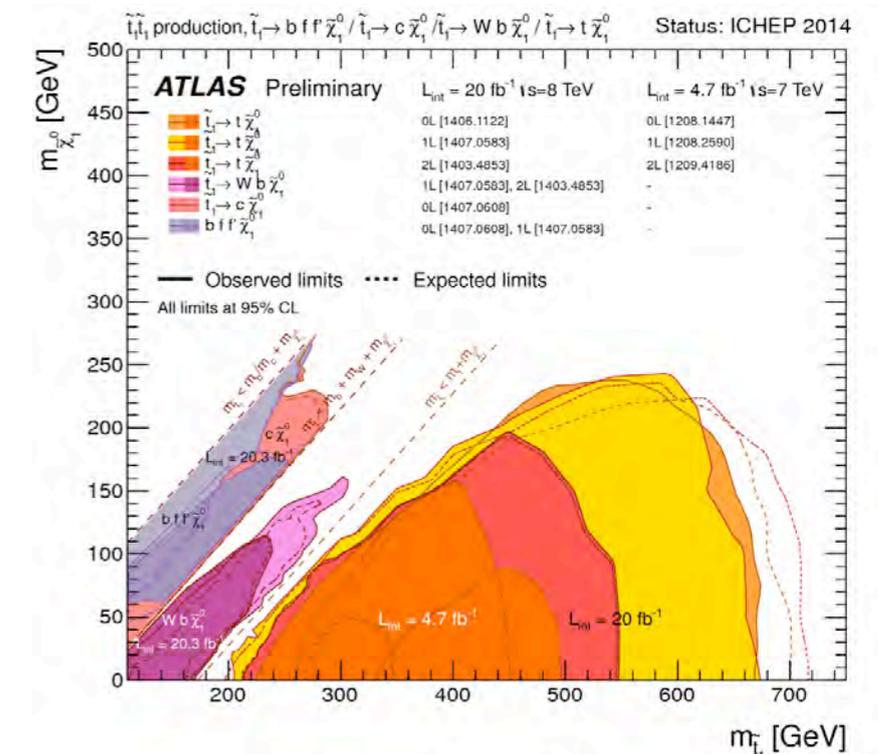
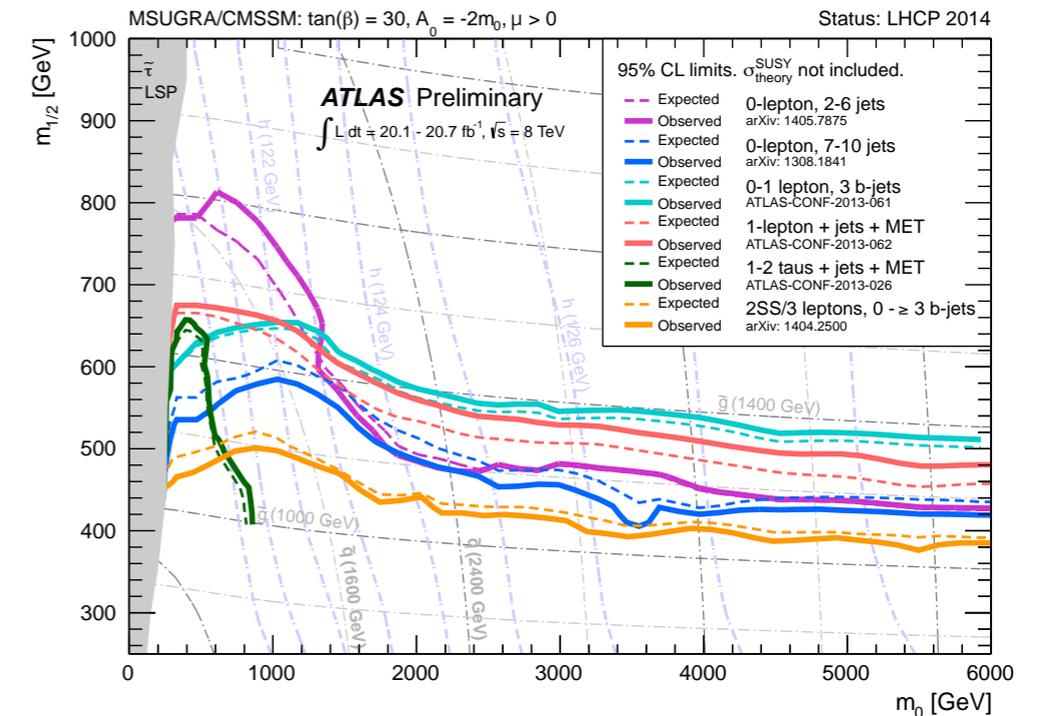
# A plethora of searches

## Examples of SUSY and exotics searches from ATLAS and CMS

Displaced vertex [RPV, GMSB, split-SUSY] <b>NEW</b>	Search for third-generation scalar leptoquarks in the top+tau channel <b>NEW</b>
Heavy resonance to $e\mu$ , $e\tau$ , $\mu\tau$ [RPV-LFV, Z'-LFV] <b>NEW</b>	Search for high mass resonances decaying to Z and Higgs bosons <b>NEW</b>
2 leptons (on/off-Z) + jets + Emiss [incl. squarks & gluinos, GGM] <b>NEW</b>	Search for physics beyond the standard model in the Dilepton Mass Distribution <b>NEW</b>
Multijets [RPV] <b>NEW</b>	Reinterpretation of HSCP Analysis in the pMSSM and other scenarios <b>NEW</b>
Monojet + Emiss (gravitino-squark, gravitino-gluino) <b>NEW</b>	Search for Stopped Long-Lived Particles <b>NEW</b>
Chargino neutralino decaying via Higgs <b>NEW</b>	Search for Heavy Majorana Neutrinos with same sign dimuons <b>NEW</b>
1/2 leptons + jets + Emiss [incl. squarks & gluinos, mUED] <b>NEW</b>	Search for Resonances using the Dijet Mass Spectrum <b>NEW</b>
Search for scalar charm <b>NEW</b>	Search for pair-produced resonances decaying to jet pairs <b>NEW</b>
Top spin correlations (stealth stop)	Search for displaced dilepton pairs <b>NEW</b>
Long-lived particles (sleptons, charginos, R-hadrons)	Search for contact interactions and extra dimensions in dijet angular distributions <b>NEW</b>
Mono-photon + Emiss [Degenerate squark/neutralino]	Search for new physics with monophotons <b>NEW</b>
Non-pointing, delayed photons [LLP, GMSB]	Search for new physics with monojets <b>NEW</b>
0 leptons + mono-jet/c-jets + Emiss [Stop in charm+LSP]	Search for Dark Matter, extra-dimensions, W' and contact interactions in lepton+MET final states <b>NEW</b>
1 lepton + 4(1 b-)jets + Emiss [Medium / heavy stop]	Search for long-lived neutral particles decaying to dijets
1-2 taus + 0-1 leptons + jets + Emiss [GMSB]	Search for disappearing tracks
0-1 leptons + $\geq 3$ b-jets + Emiss [3rd gen. squarks]	
2 taus + Emiss [EW production]	
Stop constraints from precise $t\bar{t}$ cross-section [Light stop]	
0 lepton + 6 (2 b-)jets + Emiss [Heavy stop]	
0 leptons + 2-6 jets + Emiss [Incl. squarks & gluinos]	
4 leptons + Emiss [EW production, RPV]	
2 same-sign / 3 -leptons + 0-3 b-jets + Emiss [Incl. squarks & gluinos]	

# A plethora of searches Need for interpretation studies

- ATLAS and CMS perform **searches** for new physics in many different channels.
- They also provide **interpretations** of their results within **constrained models**, like the CMSSM, or within topology-based “**Simplified Model Spectra**” (SMSs).
- However, there **exists a plethora of different BSM models and scenarios**
- Need to interpret LHC results **in the contexts of all kinds of models of new physics**
  - important for deriving the current limits on them, and for finding existing loopholes;
  - crucial once there is a discovery, if we are to unravel the correct theory and determine its parameters.



# Inert Doublet Model

# The Inert Doublet Model

- In the IDM, the SM is extended by the addition of a **second scalar,  $\Phi$** , transforming as a doublet under  $SU(2)_L$ . This  $\Phi$  is **odd under a new discrete  $Z_2$  symmetry**.

$$H = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v + h + iG^0) \end{pmatrix}, \quad \Phi = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}} (H^0 + iA^0) \end{pmatrix}$$

- Scalar potential**

$$V_0 = \mu_1^2 |H|^2 + \mu_2^2 |\Phi|^2 + \lambda_1 |H|^4 + \lambda_2 |\Phi|^4 \\ + \lambda_3 |H|^2 |\Phi|^2 + \lambda_4 |H^\dagger \Phi|^2 + \frac{\lambda_5}{2} [(H^\dagger \Phi)^2 + \text{h.c.}].$$

The  $Z_2$  symmetry forbids mixing among the components of  $H$  and  $\Phi$  and renders the lightest  $Z_2$ -odd particle stable.  
→  $H^0$  or  $A^0$  can play the role of a **DM candidate**.

$$m_h^2 = \mu_1^2 + 3\lambda_1 v^2 \\ m_{H^0}^2 = \mu_2^2 + \lambda_L v^2 \\ m_{A^0}^2 = \mu_2^2 + \lambda_S v^2 \\ m_{H^\pm}^2 = \mu_2^2 + \frac{1}{2} \lambda_3 v^2$$

$$\lambda_{L,S} = \frac{1}{2} (\lambda_3 + \lambda_4 \pm \lambda_5)$$

NB: all fermions couple to  $H$ , i.e. **2HDM Type-I** Yukawa couplings

# Number of free parameters

⇒ then, **go through standard procedure...**

⇒ minimize potential

⇒ determine number of free parameters

**Number of free parameters here: 7**

- e.g.

$$\mathbf{v}, \mathbf{M}_h, \mathbf{M}_H, \mathbf{M}_A, \mathbf{M}_{H^\pm}, \lambda_2, \lambda_{345} [= \lambda_3 + \lambda_4 + \lambda_5]$$

- $v, M_h$  fixed ⇒ left with **5 free parameters**

# Very brief: parameters determining couplings (production and decay)

dominant production modes: through  $Z$ ;  $Z, \gamma, h$  for  $AH$ ;  $H^+H^-$   
**important couplings:**

- $ZHA$ :  $\sim \frac{e}{s_W c_W}$
- $ZH^+H^-$ :  $\sim e \coth(2\theta_w)$
- $\gamma H^+H^-$ :  $\sim e$
- $hH^+H^-$ :  $\lambda_3 v$
- $H^+W^+H$ :  $\sim \frac{e}{s_W}$
- $H^+W^+A$ :  $\sim \frac{e}{s_W}$

**!! mainly determined by electroweak SM parameters !!**

# Benchmark planes

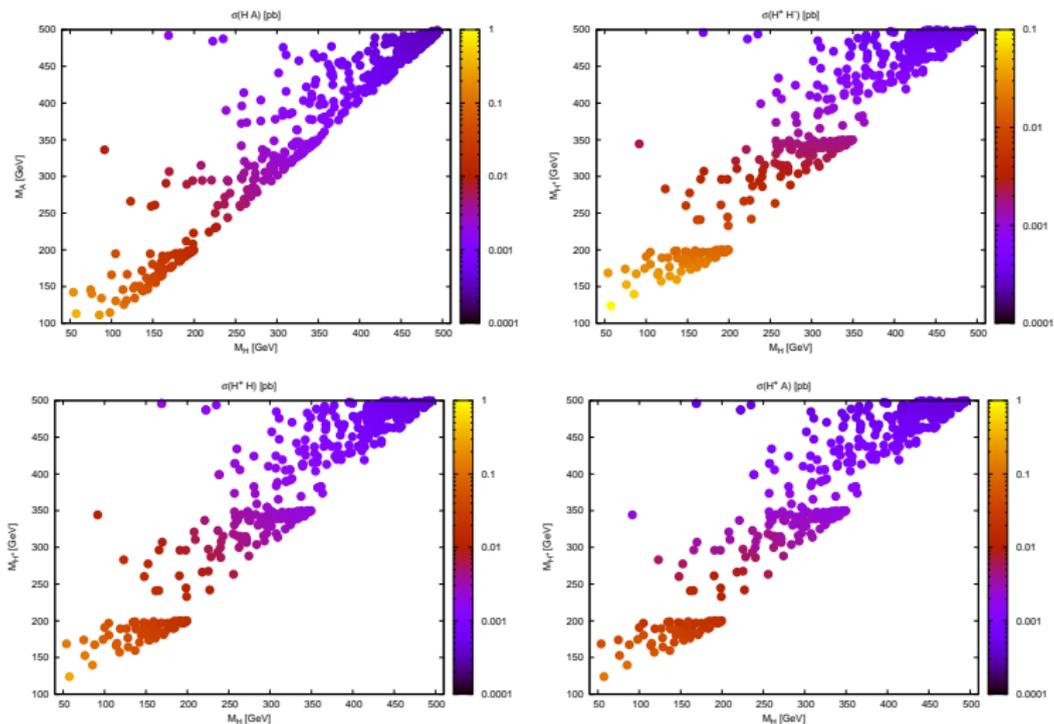
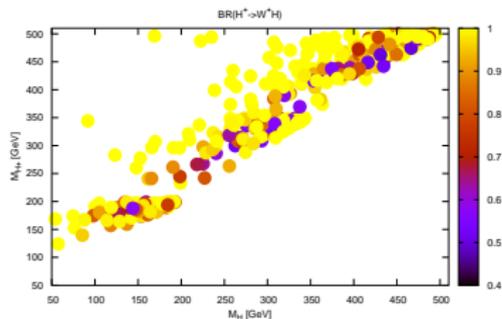


Figure : Production cross sections in pb at a 13 TeV LHC

## Aside: typical BRs

- decay  $A \rightarrow HZ$  always 100 %
- decay  $H^\pm \rightarrow HW^\pm$



second channel  $H^\pm \rightarrow AW^\pm$

**$\Rightarrow$  collider signature: SM particles and MET  $\Leftarrow$**

# Constraints: Theory

⇒ **consider all current constraints on the model** ⇐

- Theory constraints: **vacuum stability, positivity, constraints to be in inert vacuum**  
 ⇒ **limits on (relations of) couplings**, e.g.

$$\lambda_1 > 0, \lambda_2 > 0, \lambda_3 + \sqrt{\lambda_1 \lambda_2} > 0, \lambda_{345} + \sqrt{\lambda_1 \lambda_2} > 0$$

- **perturbative unitarity, perturbativity of couplings**
- **choosing**  $M_H$  as dark matter:

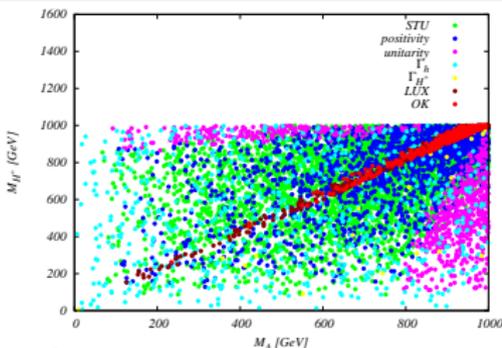
$$M_H \leq M_A, M_{H^\pm}$$

# Constraints: Experiment

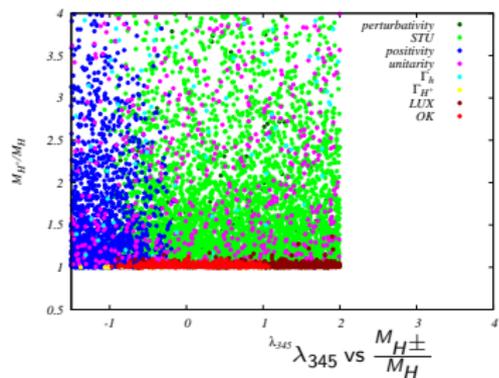
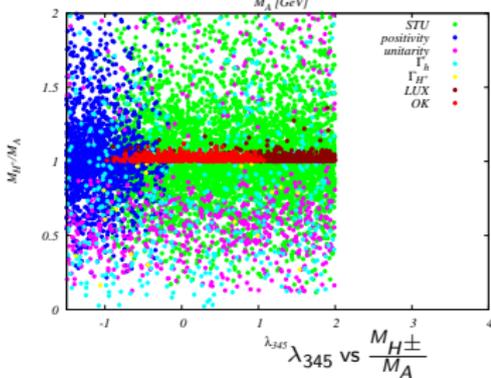
$$M_h = 125.1 \text{ GeV}, v = 246 \text{ GeV}$$

- total width of  $M_h$
  - total width of  $W, Z$
  - collider constraints from signal strength/ direct searches
  - electroweak precision through  $S, T, U$
  - unstable  $H^\pm$
  - reinterpreted/ recastet LEP/ LHC SUSY searches (Lundstrom ea 2009; Belanger ea, 2015)
  - dark matter relic density (upper bound)
  - dark matter direct search limits (LUX)
- ⇒ **tools used: 2HDMC, HiggsBounds, HiggsSignals, MicrOmegas**

Other constraints less obvious (interplay);  
result  $\Rightarrow$  mass degeneracies

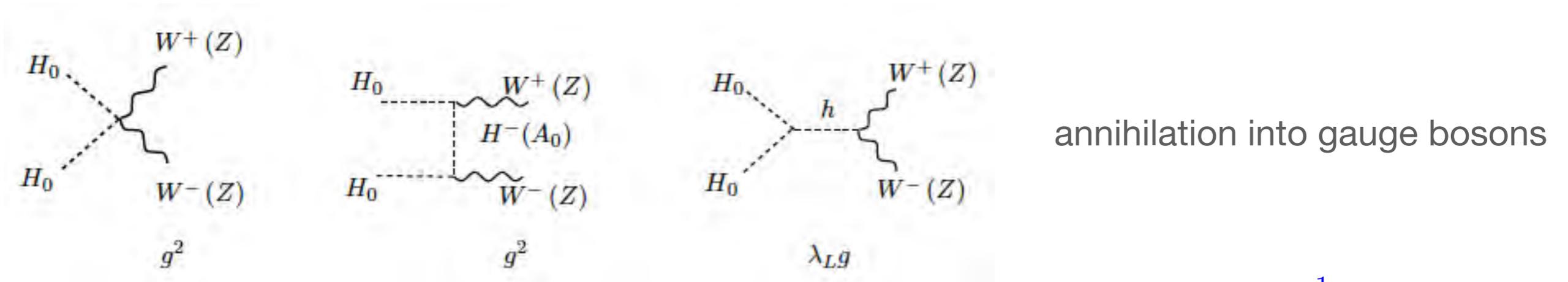


$M_A$  vs  $M_{H^\pm}$  after all constraints

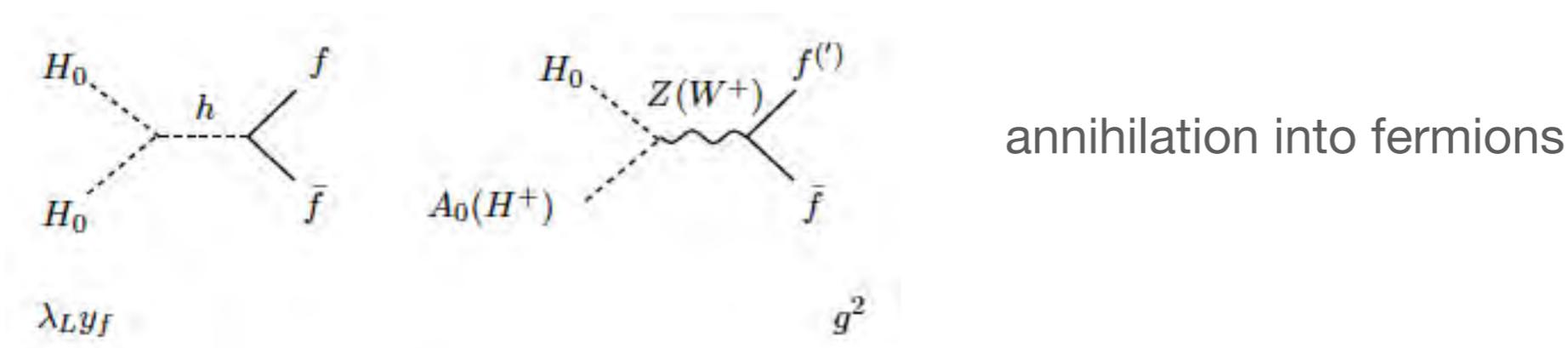
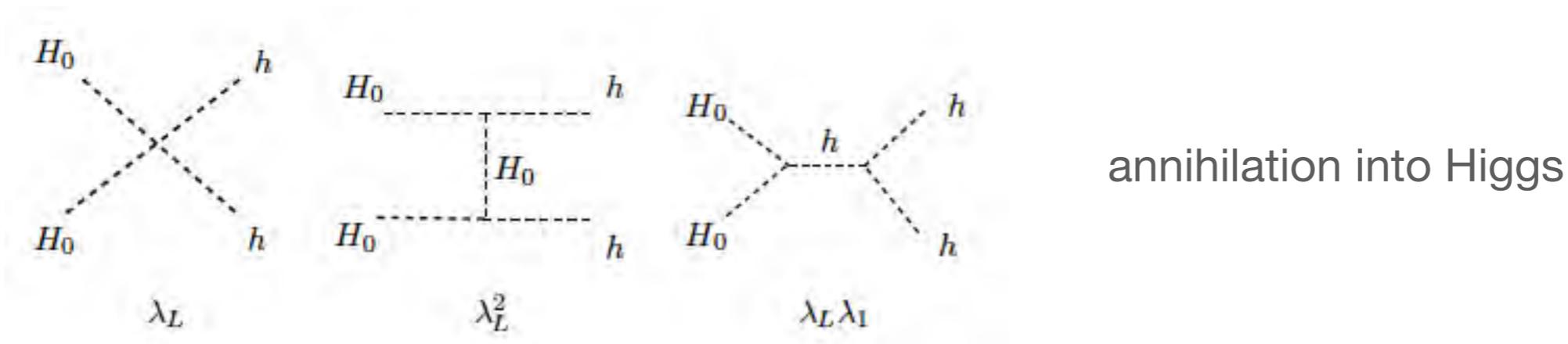


# DM annihilation channels

(taking  $H^0$  as the DM candidate)

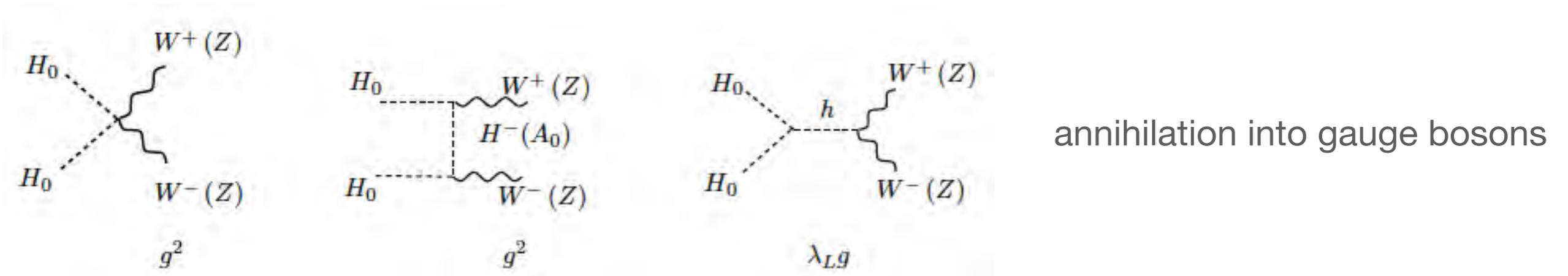


$$\lambda_L = \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)$$

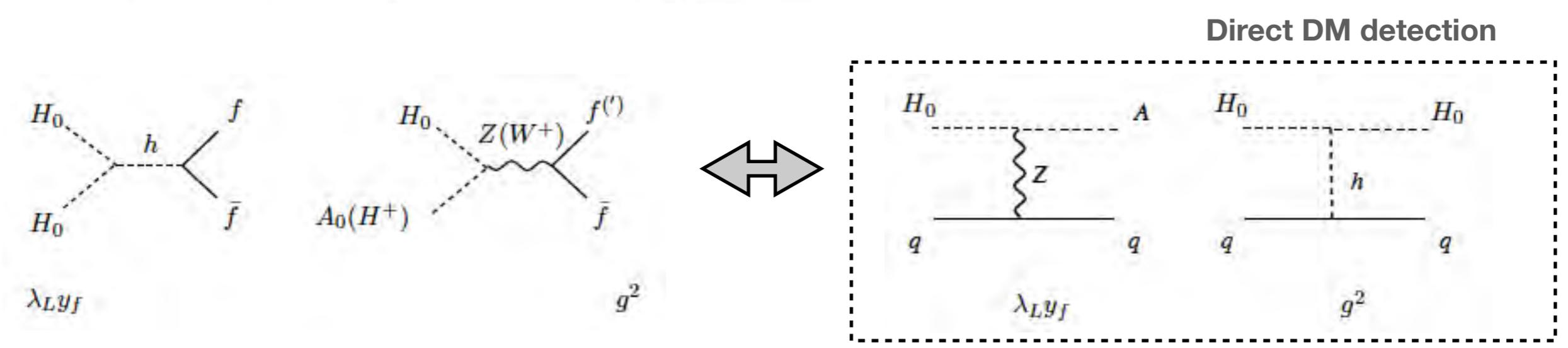
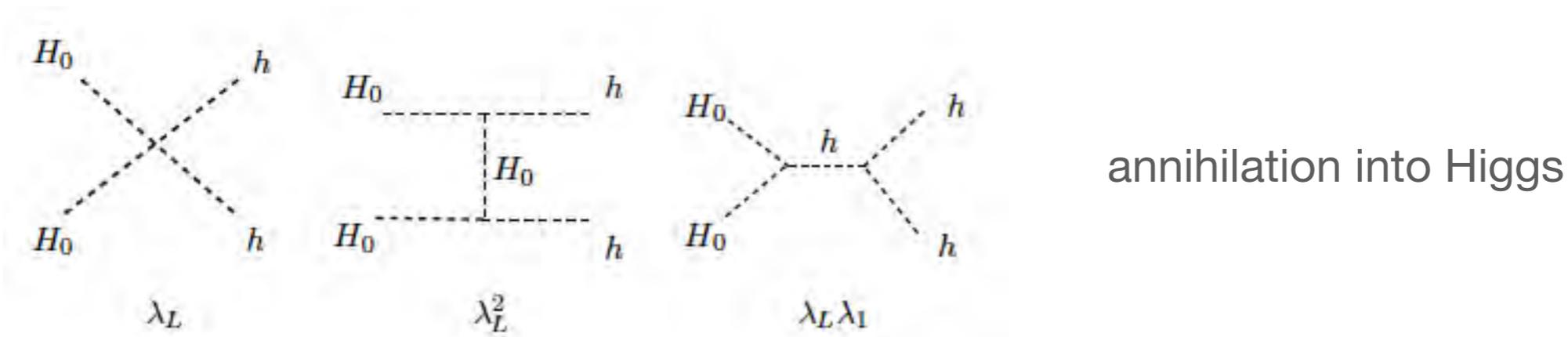


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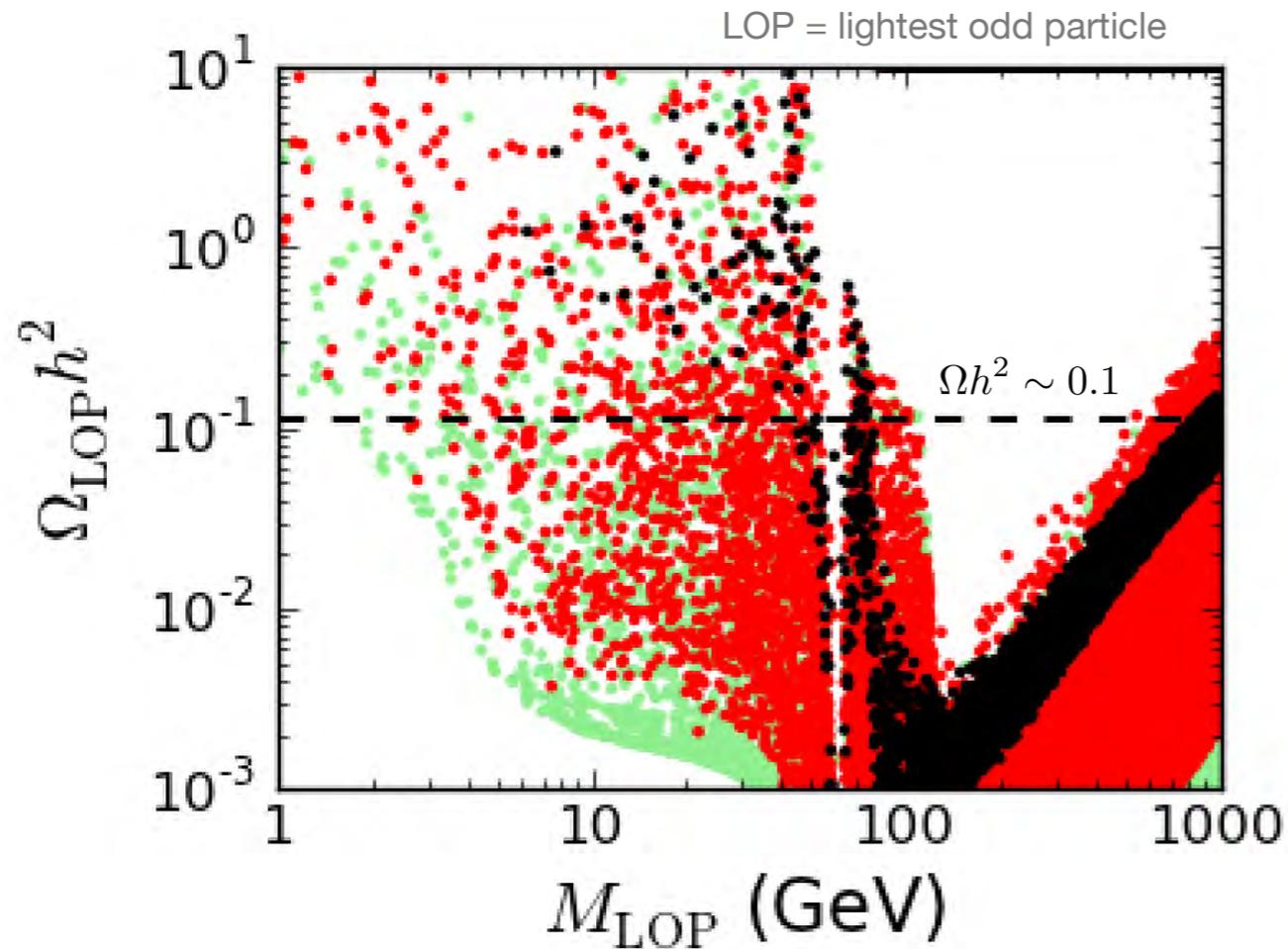


$$\lambda_L = \frac{1}{2}(\lambda_3 + \lambda_4 + \lambda_5)$$



# Constraints on the model

- **Relic density** (vanilla picture of thermal DM)

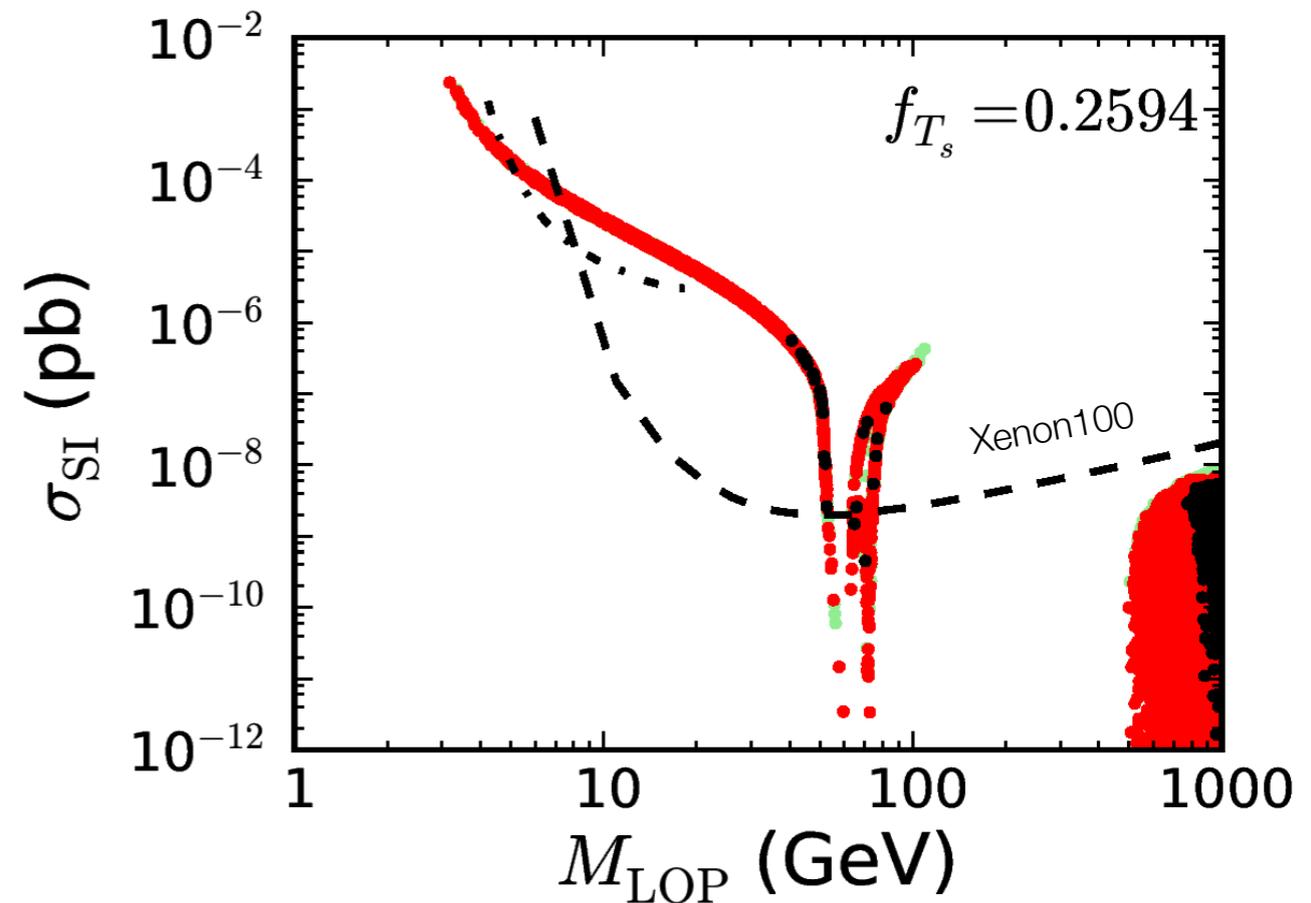


green: points valid at the input scale  $\Lambda = MZ$ ,  
 red: points which remain valid up to  $\Lambda = 10 \text{ TeV}$ ,  
 black: points valid up to the GUT scale of  $10^{16} \text{ GeV}$

[Goudelis, Herrmann, Stal, 1303.3010]

Most recent update: **A. Ilnicka, M. Krawczyk, T. Robens, 1508.01671**

- **Direct DM** searches eliminate  $m_{H_0} < 115 \text{ GeV}$  DM region apart from  $m_{H_0} \sim m_h/2$

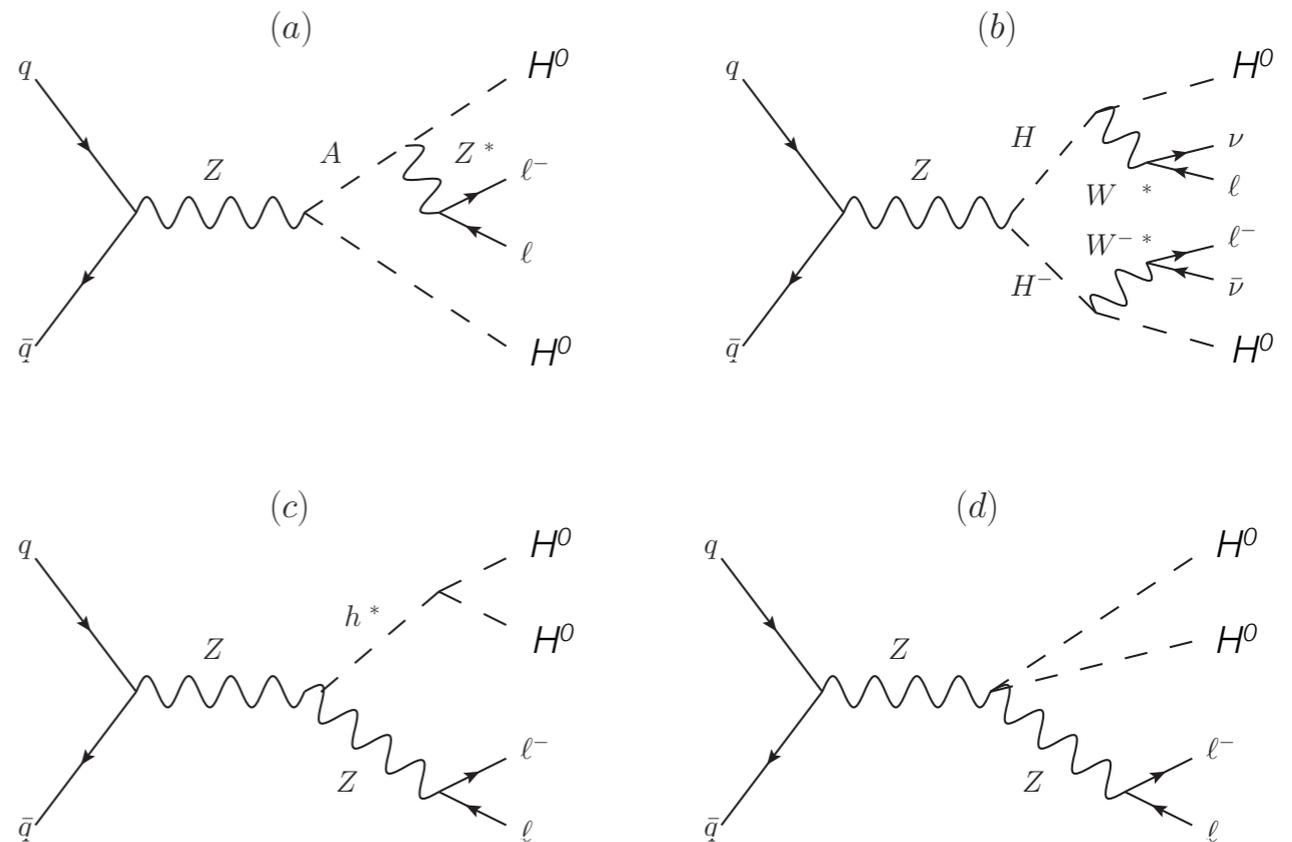


# IDM @ LHC

# LHC signatures (assuming $m_{H^0} < m_{A^0}$ )

- At the LHC, inert scalars can be pair-produced via virtual Z or W exchange ( $H^+H^-$  also via  $\gamma$ )
- The unstable  $A^0$  or  $H^\pm$  then decay into the  $H^0$  plus a Z or W
- Most promising signatures:  
SF or DF dileptons  $l^+l^- + E_T^{\text{miss}}$   
(same flavor or different flavor)

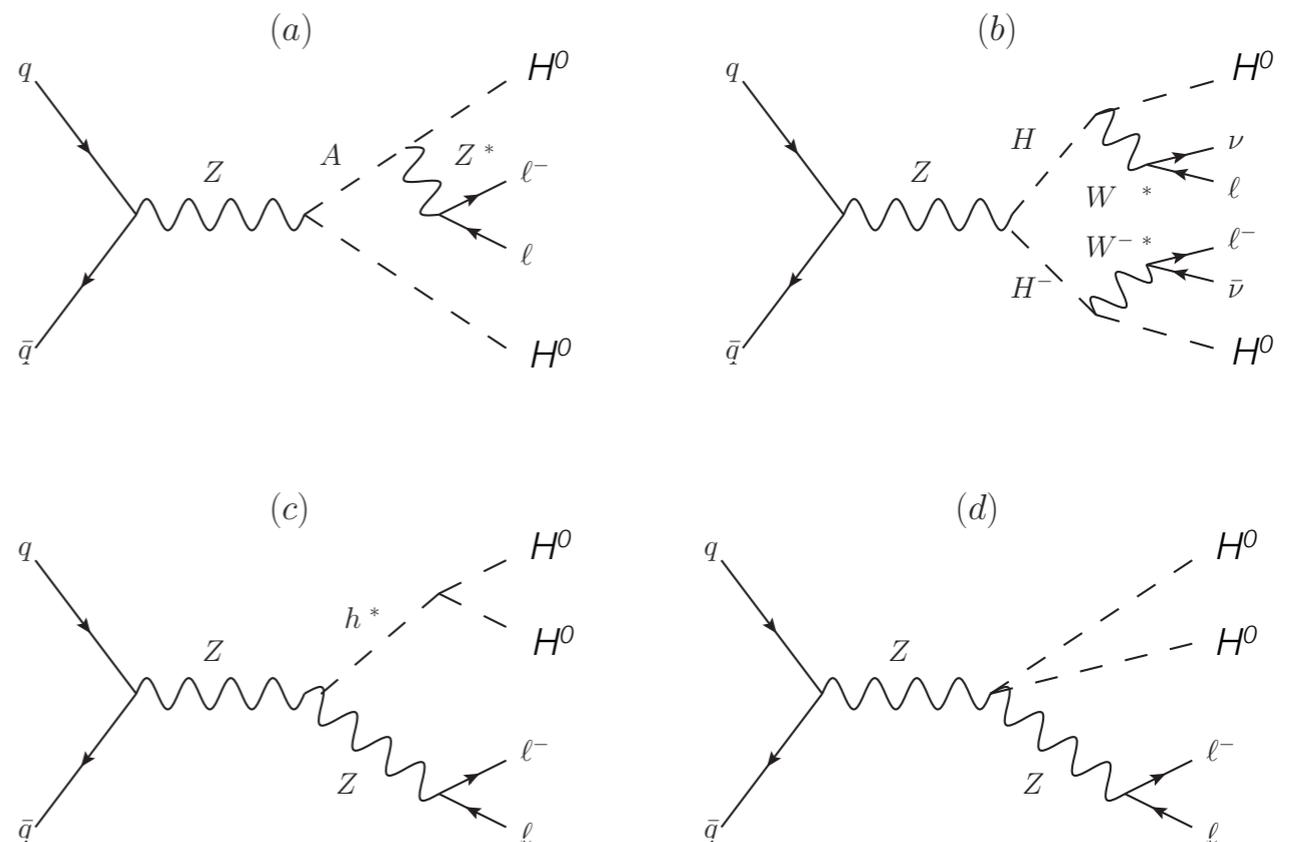
[E. Dolle et al., arXiv:0909.0394](#)



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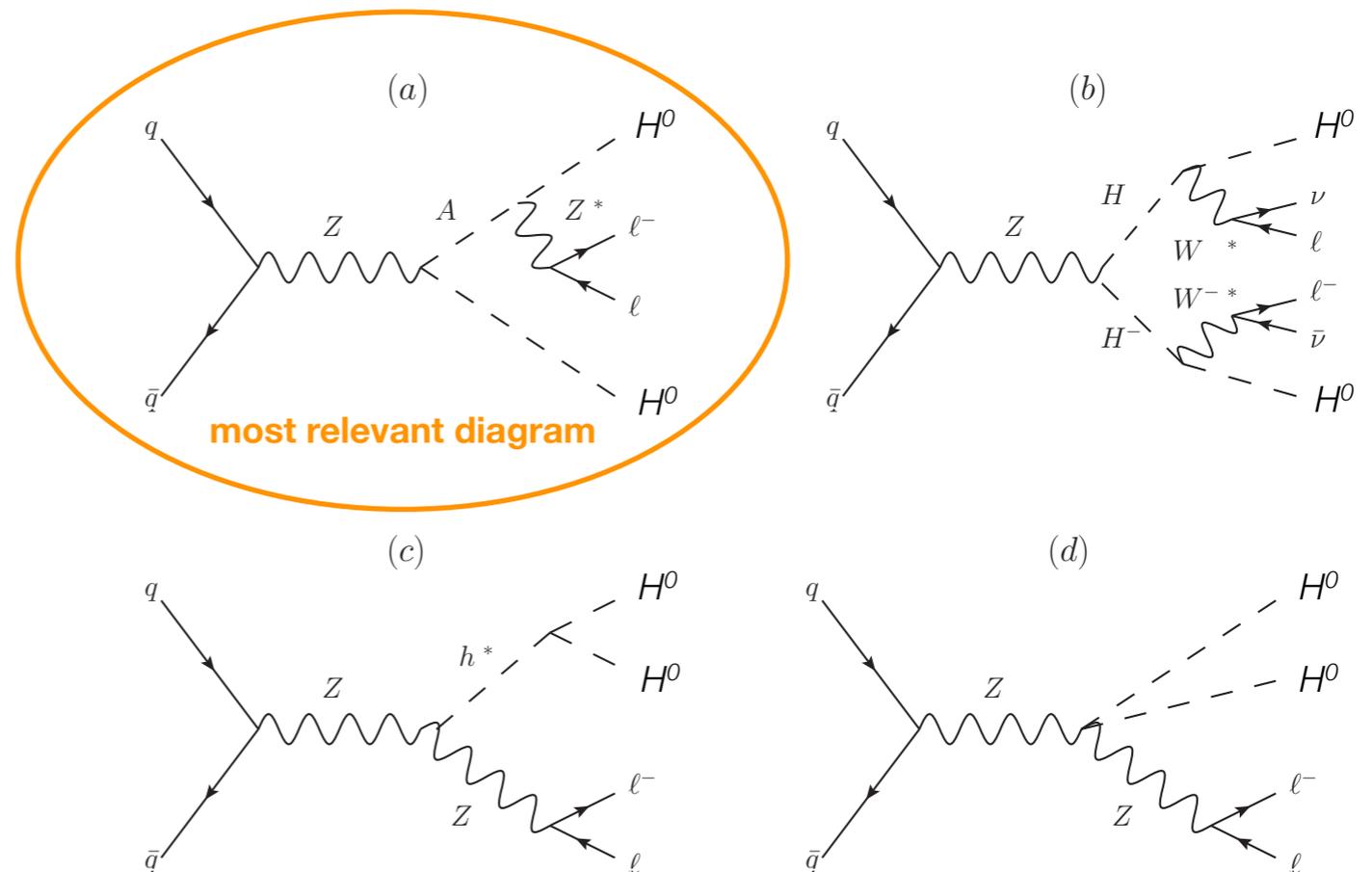


- Both ATLAS + CMS have searched for opposite-sign dileptons +  $E_T^{\text{miss}}$  at Run 1. While no interpretation was given for the IDM, note that
  - the **SUSY equivalent of process (a)** is  $q\bar{q} \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0$  with  $\tilde{\chi}_2^0 \rightarrow Z^{(*)} \tilde{\chi}_1^0$
  - **process (b)** resembles the signature of chargino-pair production  $\tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0$
  - **process (c)** is Zh production with  $h \rightarrow \text{inv.}$ ; (also (a) can look like Zh,  $h \rightarrow \text{inv.}$ )
  - processes (c) and (d) are negligible, contribution from (b) is small.

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# Recasting $l^+l^- + E_T^{\text{miss}}$ analyses for the IDM

- Implemented 2 ATLAS dilepton analyses in the MA5 PAD  
(PAD = Public Analysis Database)

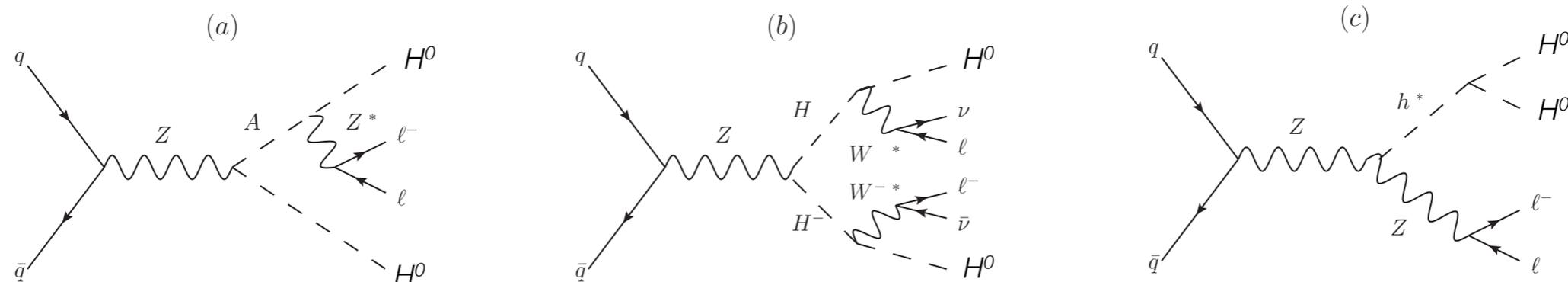


- **SUSY-2013-11: Chargino, neutralino and slepton search** [arXiv:1403.5294]

Various signal regions optimized for chargino, neutralino, slepton signals or mass regions; all leptonic signal regions require  $|m_{ll} - m_Z| > 10 \text{ GeV}$ , i.e. on-shell Z bosons are vetoed; mostly relevant for  $m_A < m_H + m_Z$

- **HIGG-2013-03:  $ZH \rightarrow l^+l^- + \text{inv. search}$**  [arXiv:1402.3244]

Requires  $|m_{ll} - m_Z| < 15 \text{ GeV}$ ; can be matched onto processes (c) and (d), and for  $m_{A0} - m_{H0} > m_Z$  also onto (a); relevant for  $m_A > m_H + m_Z$



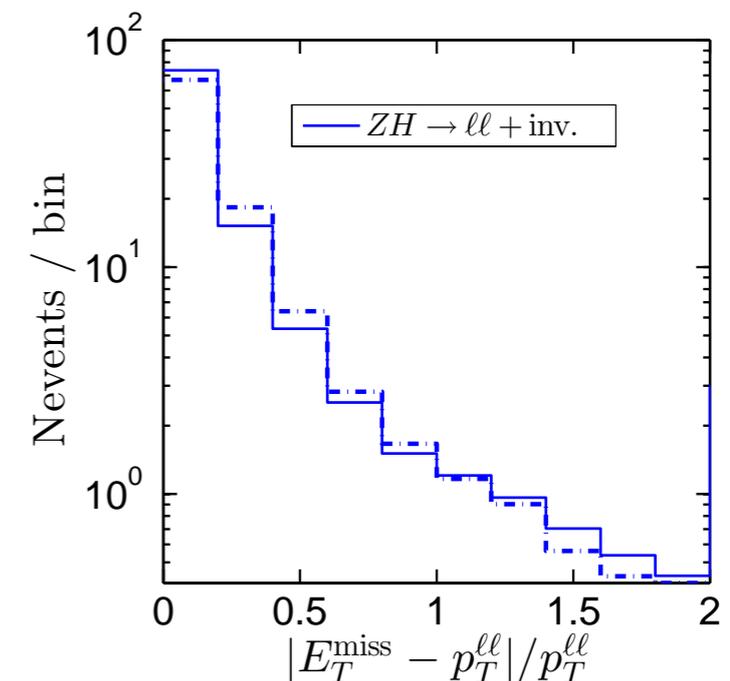
# ATLAS-HIGG-2013-03

[arXiv:1402.3244]

- ▶ ATLAS search for invisible decays of the Higgs boson in the **2 lepton + MET** final state
- ▶ only one SR, where it is required:
  - $|m_{\ell\ell} - m_{Z^0}| < 15 \text{ GeV}$
  - $E_T^{\text{miss}} > 90 \text{ GeV}$
  - $\Delta\phi(p_T^{\ell\ell}, E_T^{\text{miss}}) > 2.6$
  - $\Delta\phi(\ell, \ell) < 1.7$
  - $|E_T^{\text{miss}} - p_T^{\ell\ell}|/p_T^{\ell\ell} < 0.2$
  - **no jet**
  - $\Delta\phi(E_T^{\text{miss}}, p_T^{\text{miss}}) < 0.2$  (avoid fake MET from misreconstructed energy in the calorimeter)

▶ validation results include:

cut	ATLAS result	MA5 result
Initial number of events		838.9
2 OS leptons		256.2
$ m_{\ell\ell} - m_{Z^0}  < 15 \text{ GeV}$	243	244.1
$E_T^{\text{miss}} > 90 \text{ GeV}$	103	105.1
$\Delta\phi(p_T^{\ell\ell}, E_T^{\text{miss}}) > 2.6$		91.7
$\Delta\phi(\ell, \ell) < 1.7$		82.9
$\Delta\phi(E_T^{\text{miss}}, p_T^{\text{miss}}) < 0.2$		76.5
$ E_T^{\text{miss}} - p_T^{\ell\ell} /p_T^{\ell\ell} < 0.2$		63.2
jet veto	$44 \pm 1 \pm 3$	54.8



# Recasting $l^+l^- + E_T^{\text{miss}}$ analyses for the IDM

arXiv:1503.07367

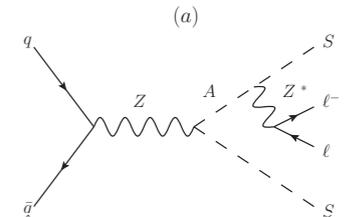
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Requires  $|m_{\tilde{l}} - m_Z| < 15 \text{ GeV}$ ; can be matched onto (c) and (d), and for  $m_{A^0} - m_{H^0} > m_Z$  also onto (a)



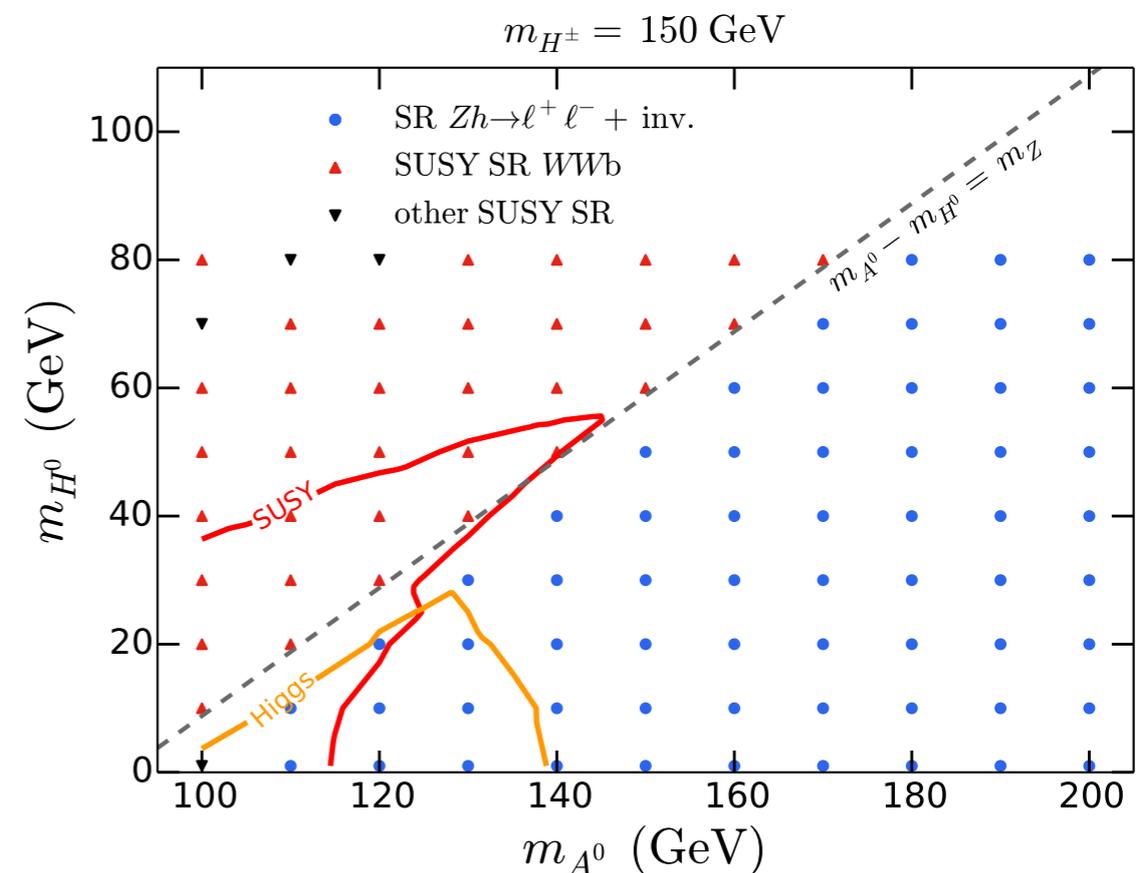
- The MadAnalysis 5 codes and detailed validation notes are **publicly available**

[10.7484/INSPIREHEP.DATA.HLMR.T56W.2](https://arxiv.org/abs/10.7484/INSPIREHEP.DATA.HLMR.T56W.2)  
[10.7484/INSPIREHEP.DATA.RT3V.9PJK](https://arxiv.org/abs/10.7484/INSPIREHEP.DATA.RT3V.9PJK)

- **Simulated signal in  $(m_{H^0}, m_{A^0})$  plane** for fixed  $m_{H^\pm}$  and  $\lambda_L = 0$

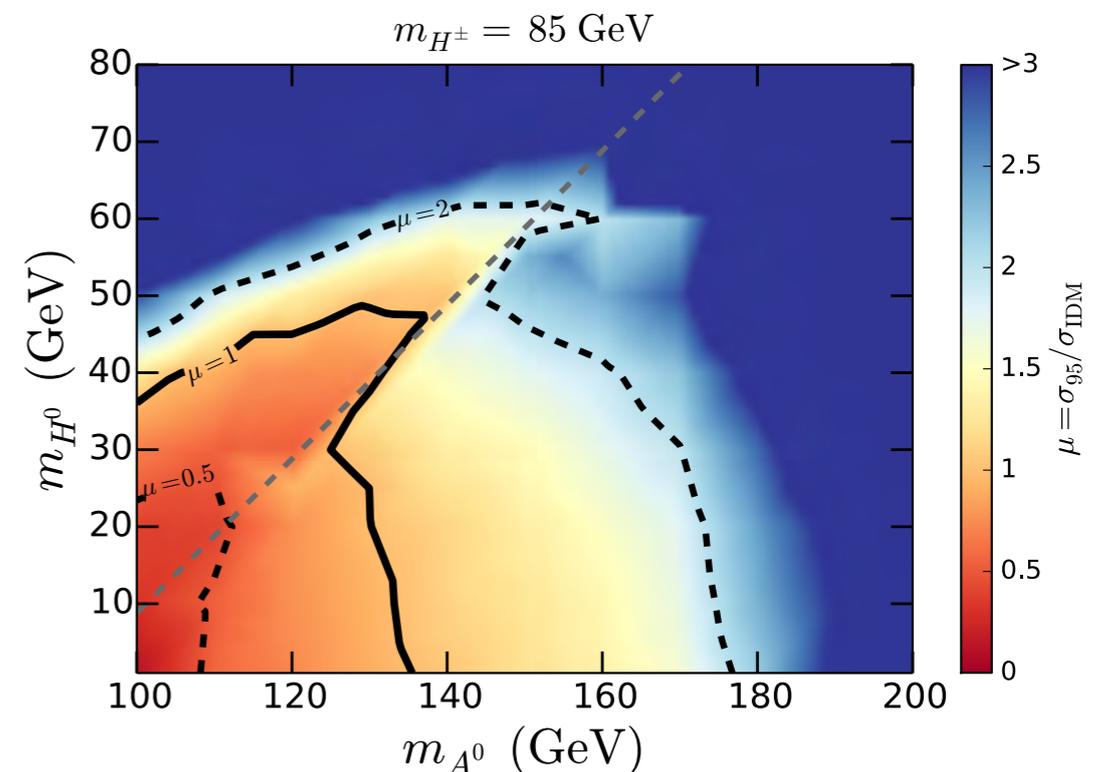
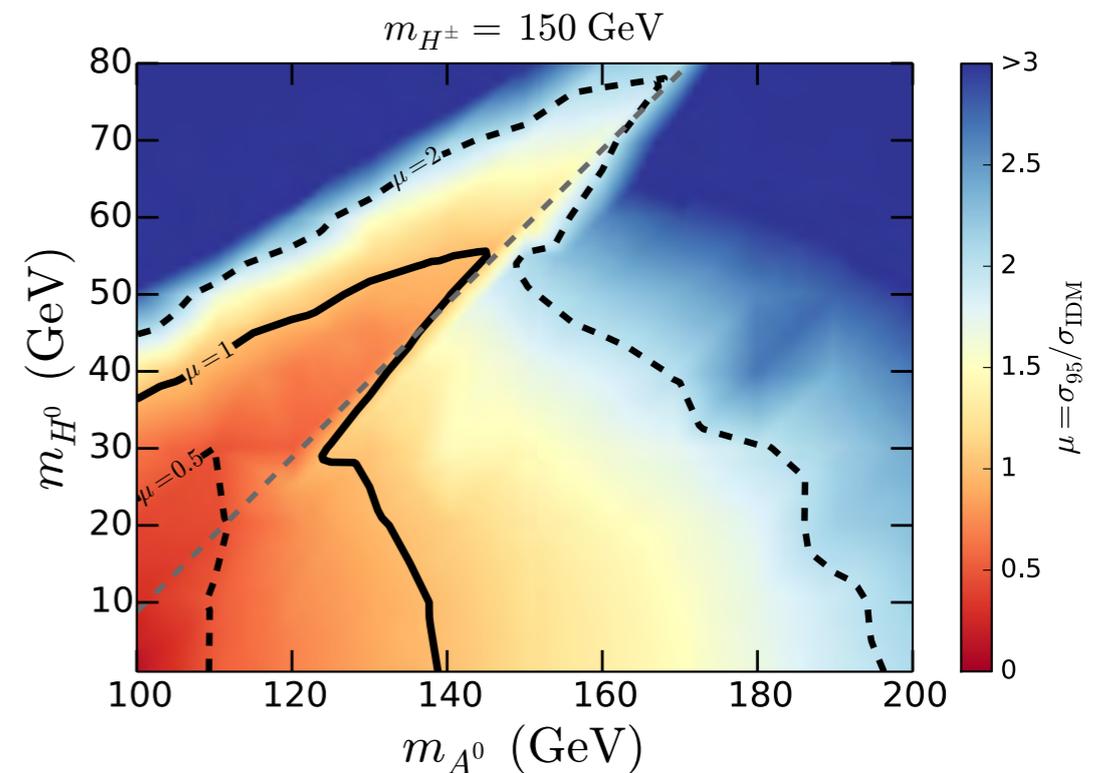
MadGraph5 + Feynrules + CalcHEP + Delphes3 + MadAnalysis5

- Background numbers taken from the experimental papers to compute CLs



# Comments

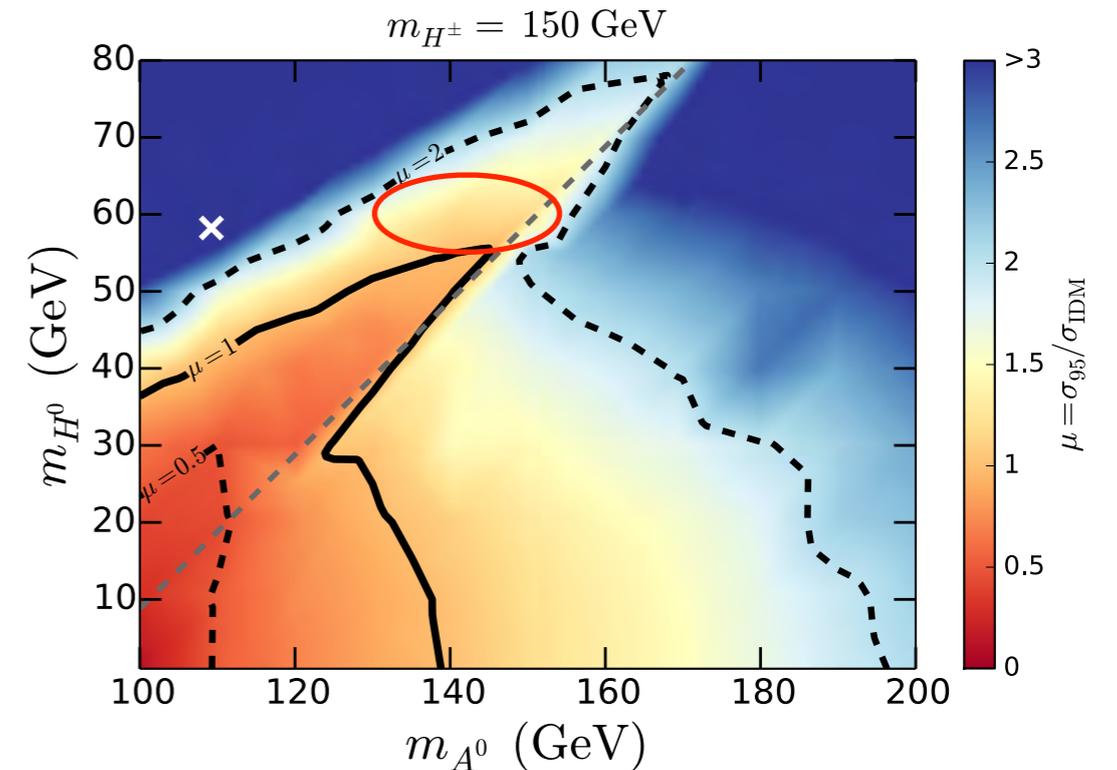
- The Run 1 ATLAS searches **exclude**, at 95% CL,  $m_{H^0} < 35$  GeV for  $m_{A^0} \approx 100$  GeV.
- The limit becomes stronger for heavier  $A^0$ , **up to  $m_{H^0} \approx 45-55$  GeV** for  $m_{A^0} \approx 140-145$  GeV (depending on  $m_{H^\pm}$ )
- The  **$m_{A^0}$  dependence** comes from the fact that the leptons from  $A^0 \rightarrow ZH^0$ ,  $Z \rightarrow l^+l^-$  are harder for heavier  $A^0$ .  
(and softer for lighter  $A^0$  / smaller mass differences)
- **$m_{H^\pm}$  dependence**: Xsection is larger for lighter  $H^\pm$ , but decay leptons are very soft and don't pass the signal selection cuts. Also,  $A^0 \rightarrow WH^\pm$  competes with  $A^0 \rightarrow ZH^0$ , when kinematically allowed, reducing the signal.



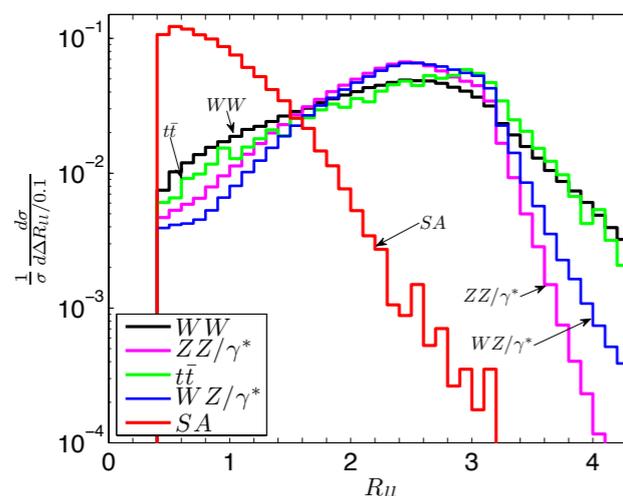
# Outlook for Run 2

- Naive rescaling of signal and BG numbers:  
at 13 TeV and  $L=100 \text{ fb}^{-1}$  the 95% CL reach should go up to  $\mu \approx 1.2$  (**1.6**) above (below) the line of  $m_A = m_H + m_Z$   
→ starts testing the funnel region  $m_H \sim m_h/2$
- Exploration of benchmark points in 1508:0167 seems difficult → high luminosity option?

Take point I with  $m_H = 57.5 \text{ GeV}$  and  $m_A = 113 \text{ GeV}$ :  
 $\sigma(\text{pp} \rightarrow \text{HA}) = 371 \text{ fb}$  but incl.  $\text{BR}(Z \rightarrow \text{ll}) \sim 7\%$  and a cut acceptance of  $\sim 1\%$  this reduces to  $\sim 0.25 \text{ fb}$  visible XS



- The experimental analyses we recasted are **not optimized for the IDM signal**



Could improve sensitivity by exploiting angular separation of signal and backgrounds (cf. Dolle et al., 0909.0394)

Perhaps exploit  $m_{ll}$  inv. mass distribution?

→ **Dedicated analysis at Run 2 would be highly interesting**

# Benchmarks submitted to Higgs Cross Section Working Group

all benchmarks:  $A \rightarrow ZH = 100\%$

- **Benchmark I: low scalar mass**

$$M_H = 57.5 \text{ GeV}, M_A = 113.0 \text{ GeV}, M_{H^\pm} = 123 \text{ GeV}$$

$$HA : 0.371(4)\text{pb}, H^+ H^- : 0.097(1)\text{pb}$$

- **Benchmark II: low scalar mass**

$$M_H = 85.5 \text{ GeV}, M_A = 111.0 \text{ GeV}, M_{H^\pm} = 140, \text{ GeV}$$

$$HA : 0.226(2)\text{pb}, H^+ H^- : 0.0605(9)\text{pb}$$

- **Benchmark III: intermediate scalar mass**

$$M_H = 128.0 \text{ GeV}, M_A = 134.0 \text{ GeV}, M_{H^\pm} = 176.0, \text{ GeV}$$

$$HA : 0.0765(7)\text{pb}, H^+ H^- : 0.0259(3)\text{pb};$$

# Benchmark: high masses

- **Benchmark IV: high scalar mass, mass degeneracy**

$$M_H = 363.0 \text{ GeV}, M_A = 374.0 \text{ GeV}, M_{H^\pm} = 374.0 \text{ GeV}$$

$$H, A : 0.00122(1)\text{pb}, H^+H^- : 0.00124(1)\text{pb}$$

- **Benchmark V: high scalar mass, no mass degeneracy**

$$M_H = 311.0 \text{ GeV}, M_A = 415.0 \text{ GeV}, M_{H^\pm} = 447.0 \text{ GeV}$$

$$H, A : 0.00129(1)\text{pb}, H^+H^- : 0.000553(7)\text{pb}$$

# Parameters tested at LHC: masses

- **LHC@13 TeV** does not depend on  $\lambda_2$ , only marginally on  $\lambda_{345}$
  - all **relevant couplings follow from ew parameters (+ derivative couplings)**  $\Rightarrow$  in the end a kinematic test
  - only in exceptional cases  $\lambda_{345}$  important; did not find such points
- $\Rightarrow$  **high complementarity between astroparticle physics and collider searches**

(holds for  $M_H \geq \frac{M_h}{2}$ )

# IDM @ high energy $e^+e^-$ colliders

# Benchmark Points

$BP$	$m_H$	$m_A$	$m_{H^\pm}$
$BP1$	57.5	113.0	123
$BP2$	85.5	111.0	140
$BP3$	128.0	134.0	176.0

Benchmark Points: [Ilnicka, Krawczyk and Robens 2015](#)

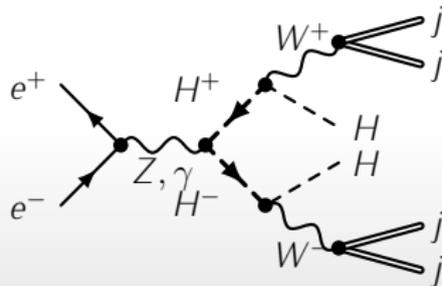
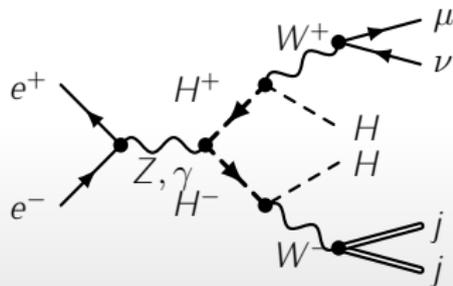
We analyse the following decay processes:

- $e^+e^- \rightarrow H^+H^- \rightarrow W^+W^-HH \rightarrow \mu\nu jjHH, jjjjHH$
- $e^+e^- \rightarrow HA \rightarrow HHZ \rightarrow HH\mu\mu, HHjj$

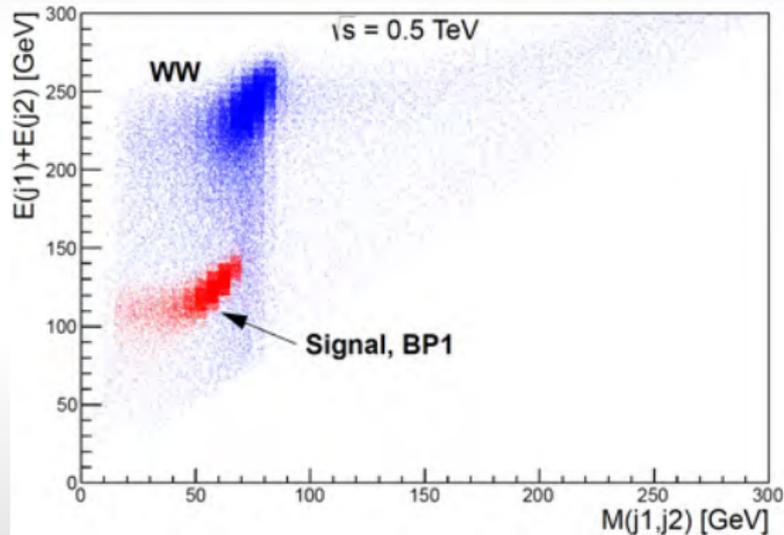
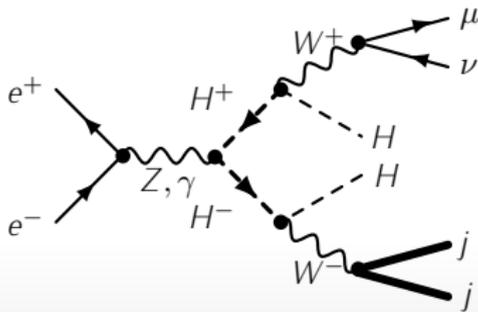
$$e^+ e^- \rightarrow H^+ H^-$$

## Signal and background cross sections

Process	Signal			Background			
	BP1	BP2	BP3	WW	ZZ	Z+jets	$t\bar{t}$
$\sigma$ [fb] @ 500 GeV	164.4	141.8	89.2	7807	583	16790	595
$\sigma$ [fb] @ 1 TeV	56.2	54.6	50.6	3180	233	4304	212



# Correlation between the sum of energies of two jets and their invariant mass



Consider pair production of charged scalars

$$e^+ e^- \rightarrow H^+ H^-$$

- the energies of the charged scalars are given by the beam energy
- their Lorentz boost factor is uniquely defined by their mass

$$\gamma = E_{beam}/M_{H^\pm}$$

Charged scalars decay to dark matter scalar and virtual  $W^\pm$

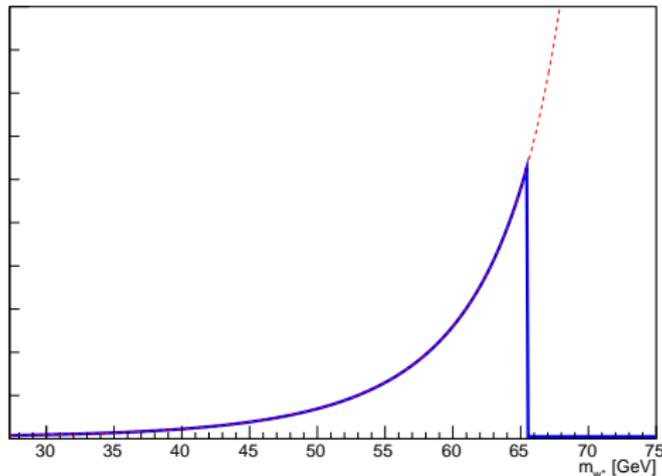
$$H^\pm \rightarrow H W^\pm$$

For all considered benchmark scenarios, the scalar mass difference

$$m_{H^\pm} - m_H \ll m_W$$

$\Rightarrow$  produced  $W^\pm$  are always virtual ( $W^*$ )

Truncated Breit-Wigner distribution for  $m_{W^*}$



Most likely is the  $W^*$  production with the maximum virtuality

$$m_{W^*} \approx m_{H^\pm} - m_H$$

⇒ expect a peak in the two jet invariant mass distribution

# Decay kinematics

The Lorentz boost of  $W^*$  is unknown, but if it is produced with the highest possible virtuality, it is **almost at rest** in the  $H^\pm$  frame  
 $\Rightarrow$  we can use  **$H^\pm$  Lorentz boost factor** to transform jet energies

In the  $W^*/H^\pm$  rest frame:

$$E_{j_1}^* = E_{j_2}^* = \frac{1}{2} m_{W^*} \approx \frac{1}{2} (m_{H^\pm} - m_H)$$

In the laboratory frame:

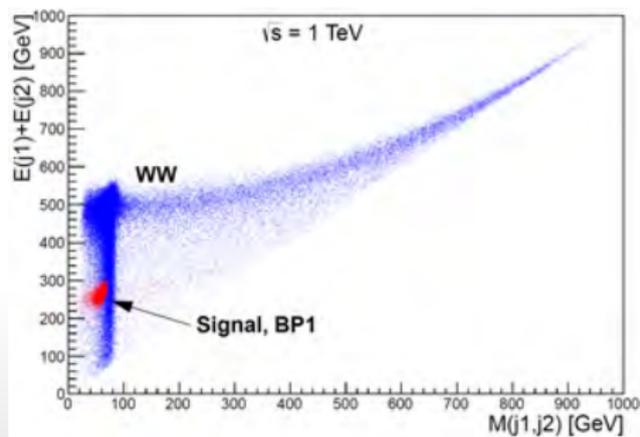
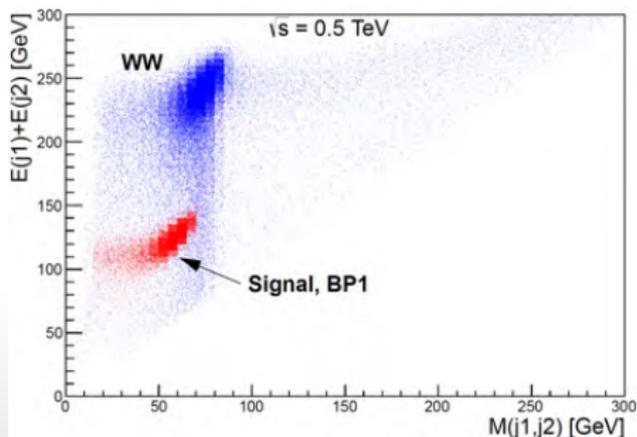
$$E_{j_{1,2}} = \gamma (E_j^* \pm \beta p_j^* \cos \theta^*)$$

Single jet energy strongly depends on the decay angle  $\theta^*$ .

But for the sum of two energies we have

$$E_{j_1} + E_{j_2} = 2 \gamma E_j^* = \gamma (m_{H^\pm} - m_H) = E_{beam} \left( 1 - \frac{m_H}{m_{H^\pm}} \right) = \text{const}$$

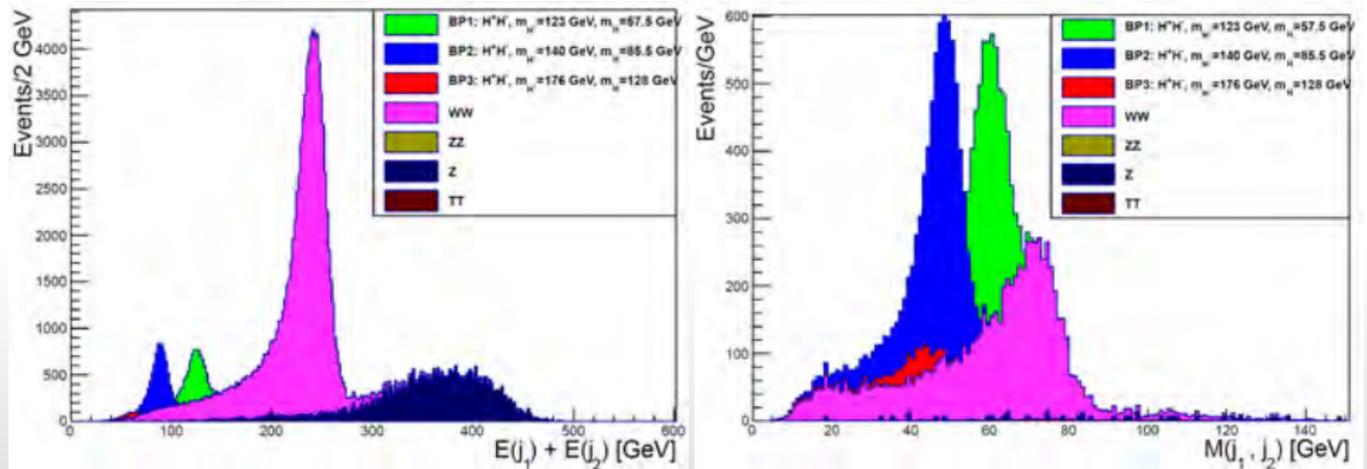
# Correlation between the sum of energies of two jets and their invariant mass



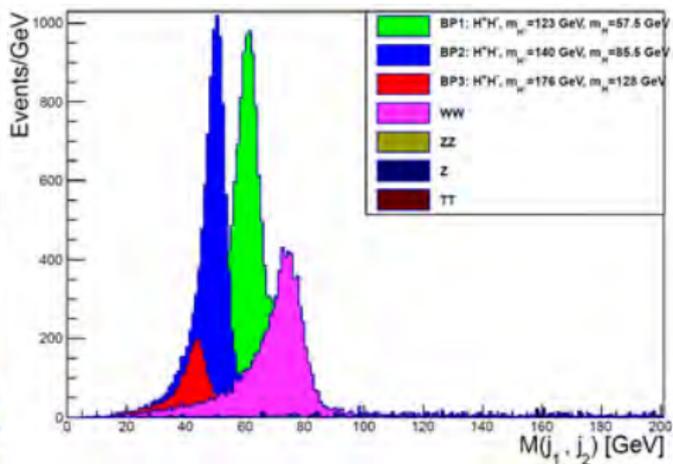
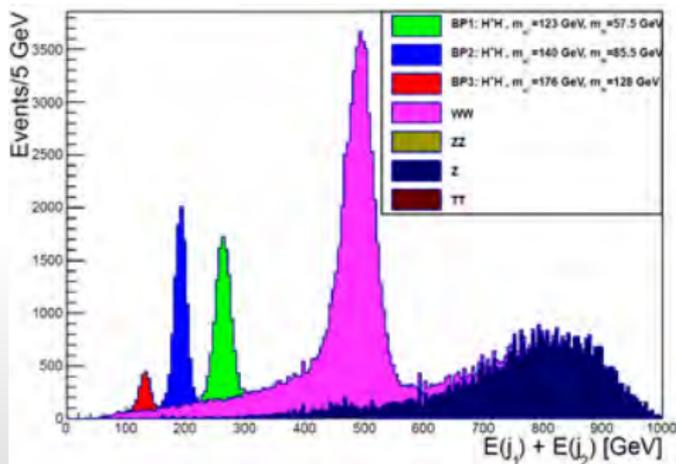
## Selection cuts for semi-leptonic final state

$H^+H^-$ analysis, semi-leptonic final state selection		
Selection cut	$\sqrt{s} = 0.5$ TeV	$\sqrt{s} = 1$ TeV
One lepton	$E_T > 10$ GeV	$E_T > 10$ GeV
Two jets	$E_T > 10$ GeV	$E_T > 10$ GeV
$E_T^{\text{miss}}$	$E_T^{\text{miss}} > 20$ GeV	$E_T^{\text{miss}} > 20$ GeV
$E(j_1) + E(j_2)$	$E(j_1) + E(j_2) < 150$ GeV	$E(j_1) + E(j_2) < 350$ GeV

Sum of the energies and invariant mass of two jets in semileptonic final state at  $\sqrt{s} = 0.5$  TeV



Sum of the energies and invariant mass of two jets in semileptonic final state at  $\sqrt{s} = 1$  TeV



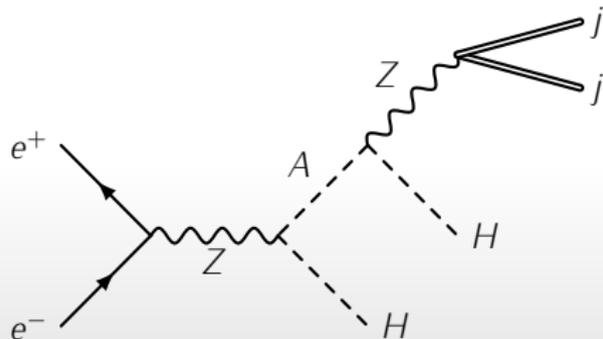
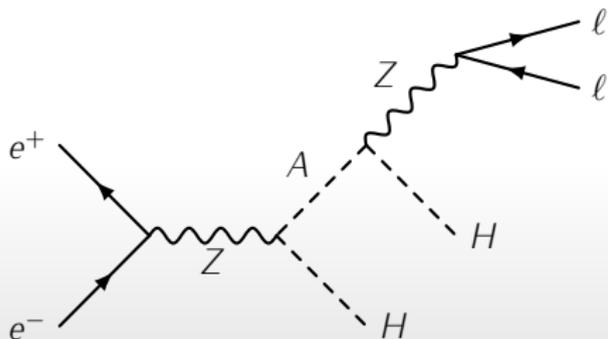
If inert charged scalars with masses  $\sim M_Z$  do exist, we should clearly see them at ILC/CLIC:

- Production cross section is model-independent depends only on the mass, charge and spin of the produced particle  
 $\Rightarrow$  we can test, if it is a scalar...
- Well defined kinematics  $\Rightarrow$  high signal selection efficiency
  - 20 – 64% for  $\sqrt{s}=0.5$  TeV
  - 59 – 86% for  $\sqrt{s}=1$  TeVand good background suppression
- Signal to background ratio  $S/B$  after mass window cut
  - 0.35 – 4 for  $\sqrt{s}=0.5$  TeV
  - 2.5 – 11 for  $\sqrt{s}=1$  TeV
- Final statistical significance  $S/\sqrt{S+B}$ 
  - 11 – 66 for  $\sqrt{s}=0.5$  TeV
  - 33 – 87 for  $\sqrt{s}=1$  TeV

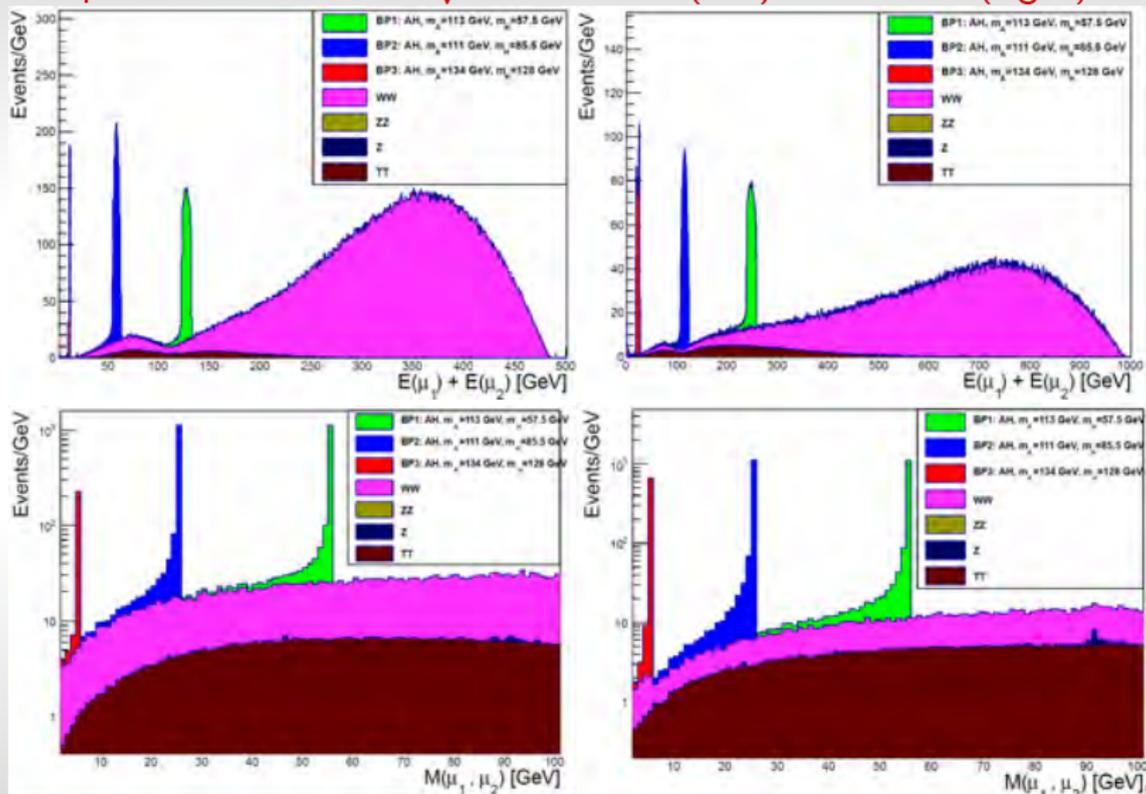
$$e^+e^- \rightarrow AH$$

## Signal and background cross sections

	$\sqrt{s} = 0.5 \text{ TeV}$			$\sqrt{s} = 1 \text{ TeV}$		
Process	$e^+e^- \rightarrow AH$			$e^+e^- \rightarrow AH$		
Benchmark point	BP1	BP2	BP3	BP1	BP2	BP3
Cross section [fb]	90	85.8	68.4	25	24.8	23.6



Sum of the energies (up) and invariant mass (down) of two lepton in leptonic final state at  $\sqrt{s} = 0.5$  TeV (left) and 1 TeV (right).



For the charged scalar production  $e^+e^- \rightarrow H^+H^-$

- Semi-leptonic channel  $e^+e^- \rightarrow l\nu jjHH$ 
  - two jet invariant mass:  $m_{jj} = m_{W^*} \approx m_{H^\pm} - m_H$
  - sum of two jet energies:  $E_{jj} = E_{beam} (1 - R)$ , where  $R = m_H/m_{H^\pm}$
- Fully hadronic channel  $e^+e^- \rightarrow jjjjHH$ 

As both  $W^*$  have the same Lorentz boost, jet with the highest energy (lab) comes from the same  $W^*$  as the jet with the lowest energy

$\Rightarrow$  we can reconstruct both  $W^*$  easily

  - two jet invariant masses:  $m_{14} = m_{23} = m_{W^*} \approx m_{H^\pm} - m_H$
  - sum of four jet energies:  $E_{4j} = 2 E_{beam} (1 - R)$

For the neutral scalar production  $e^+e^- \rightarrow HA$

- For leptonic channel  $e^+e^- \rightarrow llHH$ 

two lepton invariant mass:  $m_{ll} = m_{Z^*} \approx m_A - m_H$
- For hadronic channel  $e^+e^- \rightarrow jjHH$ 

two jet invariant mass:  $m_{jj} = m_{Z^*} \approx m_A - m_H$

Expected **statistical precision** of scalar mass determination with  $500 \text{ fb}^{-1}$

Scalar	$\sqrt{s}$ [TeV]	BP1	BP2	BP3
$m_{H^\pm}$	theo.	123	140	176
	0.5	$117.1 \pm 3.6$	$136.8 \pm 3.5$	$167.4 \pm 3.5$
	1	$112.7 \pm 2.4$	$131.4 \pm 1.9$	$172.2 \pm 2.1$
$m_H$	theo.	57.5	85.5	128
	0.5	$58.5 \pm 1.8$	$88.9 \pm 2.3$	$127.2 \pm 2.7$
	1	$53.0 \pm 1.1$	$81.5 \pm 1.2$	$129.1 \pm 1.6$
$m_A$	theo.	113	111	134
	0.5	$113.9 \pm 1.8$	$114.3 \pm 2.3$	$133.1 \pm 2.7$
	1	$104.6 \pm 1.1$	$105.0 \pm 1.2$	$134.8 \pm 1.6$

The systematic shifts observed between the assumed (theo.) scalar masses and the fit results are due to the simplified approach used.

Can be corrected for based on the simulation results.

- Inert Doublet Model is one of the simplest extensions of the Standard Model providing a candidate for dark matter.
  - Second scalar doublet is not involved in mass generation and does not couple to fermions
  - IDM with inert scalar masses of the order of  $M_Z$  still in agreement with all existing data

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- LHC signatures similar to some SUSY scenarios, but cross sections small
  - Run 1 limits on  $m_H$  extend to  $\sim 50$  GeV only
  - Dedicated benchmark points prepared for LHC Run 2

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- LHC signatures similar to some SUSY scenarios, but cross sections small
  - Run 1 limits on  $m_H$  extend to  $\sim 50$  GeV only
  - Dedicated benchmark points prepared for LHC Run 2
- IDM should be clearly visible at high energy  $e^+e^-$  collider for low and intermediate mass scenarios
  - Well constrained kinematics allows for efficient selection
  - Scalar masses can be reconstructed with 1 – 4 % precision

Number of events in signal and background processes after all selection cuts at integrated luminosity of  $500 \text{ fb}^{-1}$ .

$H^+H^-$ , semi-leptonic final state at $\mathcal{L} = 500 \text{ fb}^{-1}$								
	$\sqrt{s} = 0.5 \text{ TeV}$				$\sqrt{s} = 1 \text{ TeV}$			
	S	B	S/B	$S/\sqrt{S+B}$	S	B	S/B	$S/\sqrt{S+B}$
BP 1	4887	3307	1.5	54	8709	2736	3.2	81
BP 2	5402	1342	4	66	8166	720	11	87
BP 3	478	1380	0.35	11	1534	602	2.5	33

# Selection cuts and cut efficiencies for fully leptonic final state

<i>HA</i> analysis, leptonic final state selection		
Selection cut	$\sqrt{s} = 0.5$ TeV	$\sqrt{s} = 1$ TeV
2 leptons	$E_T > 1$ GeV	$E_T > 5$ GeV
$E_T^{\text{miss}}$	$10 < E_T^{\text{miss}} < 120$ GeV	$10 < E_T^{\text{miss}} < 250$ GeV
$m_{\ell_1, \ell_2}$	$ m_{\ell_1, \ell_2} - m_Z  > 20$ GeV	$ m_{\ell_1, \ell_2} - m_Z  > 20$ GeV

<i>HA</i> analysis, leptonic final state selection							
Cut eff.	BP1	BP2	BP3	WW	ZZ	Z	TT
Total eff.@ 0.5 TeV	0.99	1	0.22	0.67	0	1.5e-05	0.26
Total eff.@ 1 TeV	0.98	0.98	0.65	0.45	2e-06	4.2e-05	0.42

Number of events in signal and background processes after all selection cuts at integrated luminosity of  $500 \text{ fb}^{-1}$

$HA$ , leptonic final state at $\mathcal{L} = 500 \text{ fb}^{-1}$								
	$\sqrt{s} = 0.5 \text{ TeV}$				$\sqrt{s} = 1 \text{ TeV}$			
	S	B	S/B	$S/\sqrt{S+B}$	S	B	S/B	$S/\sqrt{S+B}$
BP 1	1214	105	11.6	33	1220	55	22	34
BP 2	1223	71	17.2	34	1211	31	38.7	34
BP 3	225	34	6.6	14	666	13	50	26