

# TestFitter performance and new options

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# Introduction

## Motivation

Distances between planes  $\sim O(100 \text{ mm})$  + scattering angles  $\sim O(0.1 \text{ mrad})$   
 $\Rightarrow$  track displacement due to scattering  $\sim O(10 \text{ }\mu\text{m})$  (for beam energy of few GeV)

Effect comparable with position resolution ( $1 - 2 \text{ }\mu\text{m}$ ) !

$\Rightarrow$  significantly influences the measurement, straight line fit is not sufficient...

## Analytical approach

Describes the performance of the telescope including multiple scattering (!)

### Simplifying assumptions:

- sensors (and all other material eg. windows) are very thin layers
- small scattering angles (Gaussian approximation)
- Gaussian position measurement errors
- perfect alignment

Analytical approach: track fitting by solving matrix equation

$\Rightarrow$  error on the position reconstructed at DUT given by telescope geometry only

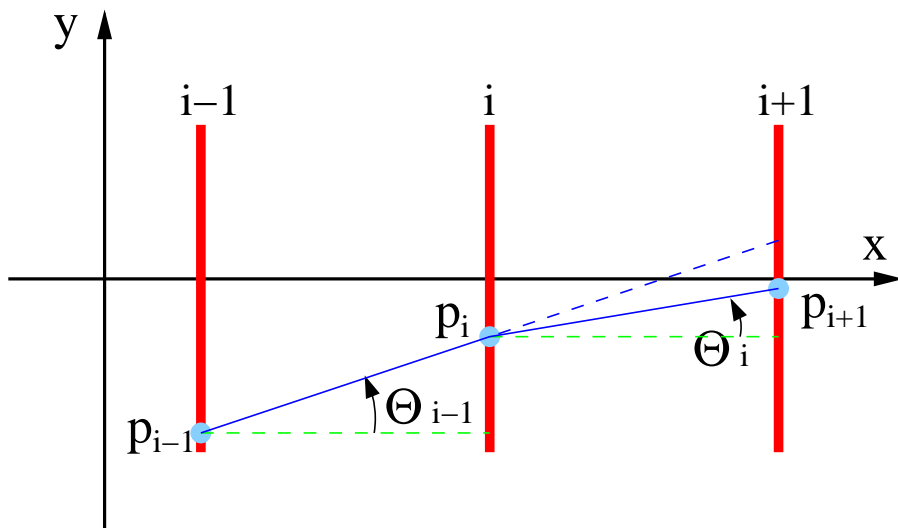
# Introduction

## Analytical approach

We can determine track position in each plane (including DUT), i.e.  $N$  parameters ( $p_i, i = 1 \dots N$ ), from  $M < N$  measured positions in telescope planes.

We use constraints on multiple scattering!

Contribution of plane  $i$  to  $\chi^2$  of the fit



$$\Delta\chi_i^2 = \left( \frac{y_i - p_i}{\sigma_i} \right)^2 + \left( \frac{\Theta_i - \Theta_{i-1}}{\Delta\Theta_i} \right)^2$$

position measurement                      multiple scattering

where:  $\Theta_i = \frac{p_{i+1} - p_i}{x_{i+1} - x_i}$

Both terms present for planes  $i \neq 1, i_{DUT}, N$ ,  
first term missing for DUT, second for first and last plane

Constraint from the beam direction also taken into account.

$\chi^2$  minimum can be found by solving the matrix equation - fast!

# Introduction

## Optimization

The chosen approach is to check all possible hit combinations.

Without optimization this would be very CPU time consuming ( $t \sim (N_{hit})^{N_{plane}}$ )

⇒ 3 hit (or 2 hit when using beam constraint) combinations checked first

If  $\chi^2$  too large, all combinations including these hits can be skipped ( $t \sim (N_{hit})^3$ )

Other options improving performance:

- **UseNominalResolution**: same matrix used for all events (no missing hits)
- **UseBeamConstraint**:  $\chi^2$  can be calculated already for 2 hits ( $t \sim (N_{hit})^2$ )
- **AllowAmbiguousHits**: only one loop over all fit possibilities (no missing hits allowed)

Unfortunately, performance very poor for recent data.

New option introduced: **UseSlope** gave large improvement, but only for “full tracks”

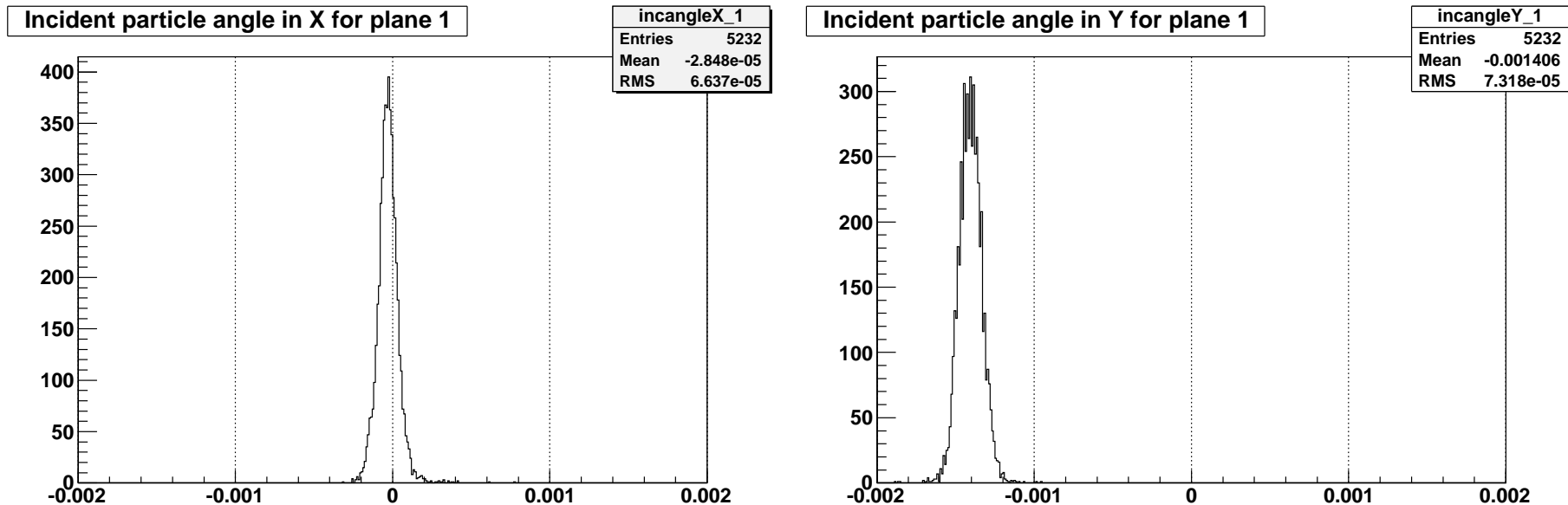
# Performance

Reasons for poor performance studied for run 10233 (6 digital sensor planes)

## UseBeamConstraint

One of the main assumptions of the analytical approach was that the beam was exactly perpendicular to the sensor plane.

This is not the case in the new data:



Fit is still OK. But [UseBeamConstraint](#) option could not be used

# Performance

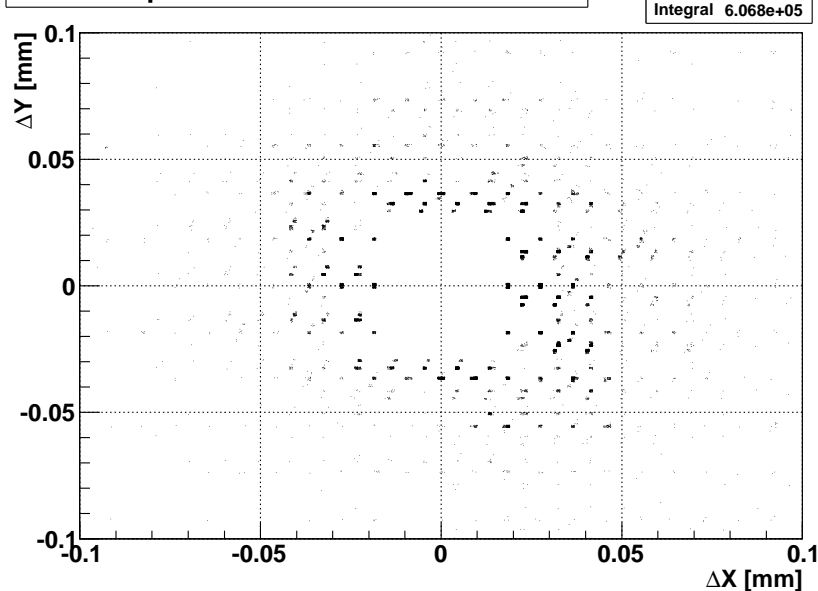
## AllowAmbiguousHits

All hit combinations passing  $\chi^2$  cut were stored (given hit could be used more than once).

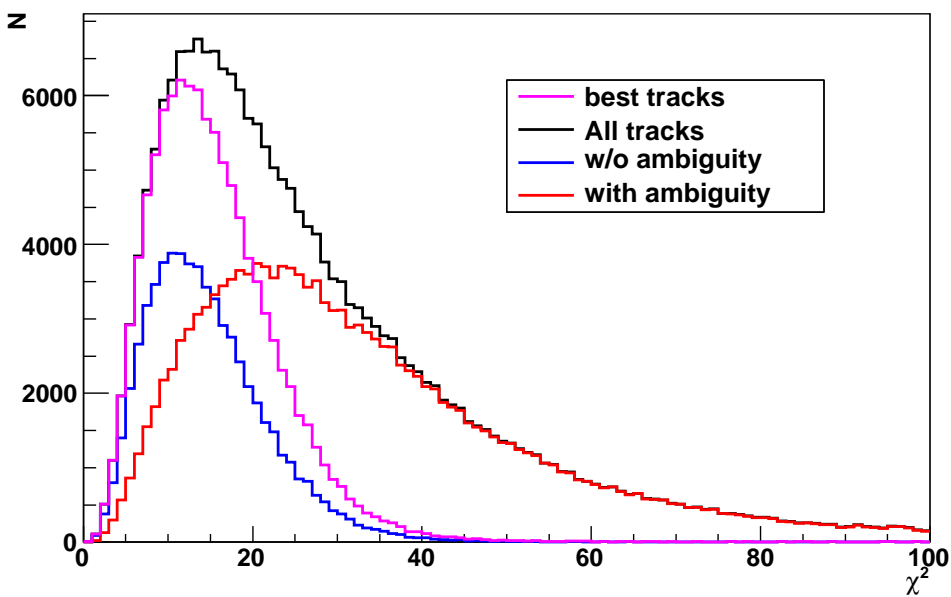
In the new data number of fitted tracks more than doubled with this option!

Correlated hit pairs (“ghosts” ?)  $\Rightarrow$  some track candidates differ by one or two hits only.

Hit separation between two tracks



Chi2 for all tracks



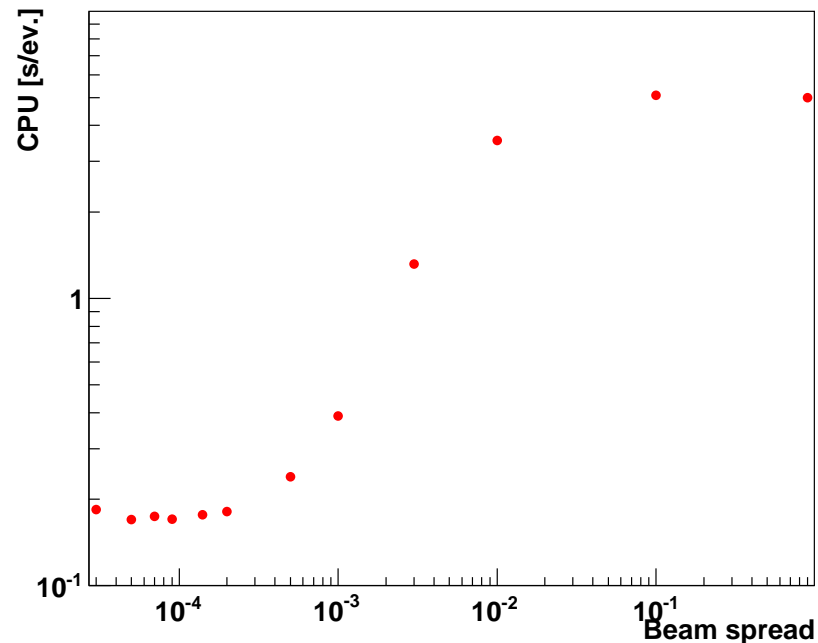
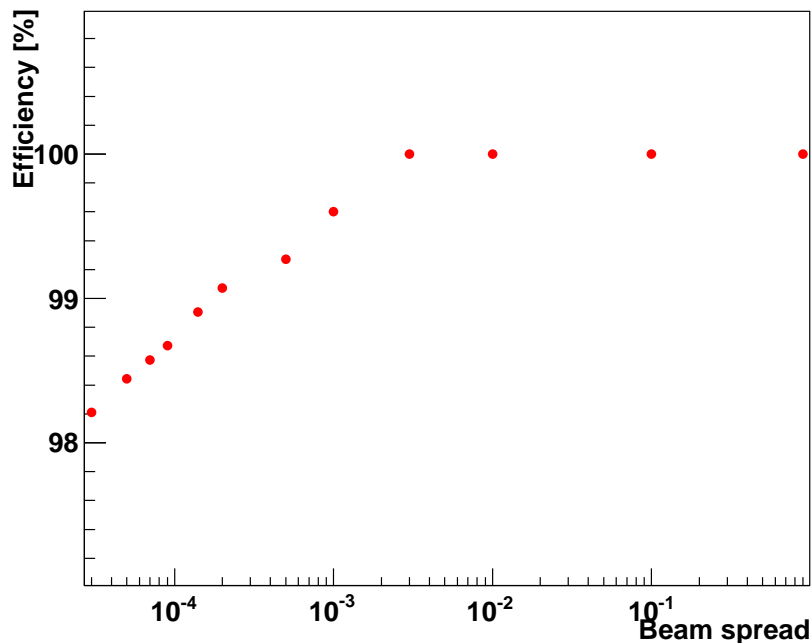
# New development

## UseBeamConstraint

Fitting algorithm was modified to take into account possible beam tilt.

Two new control cards: `BeamSlopeX` and `BeamSlopeY`

Results for “worst case” - fit to 4-6 planes (`AllowMissingHits = 2`):



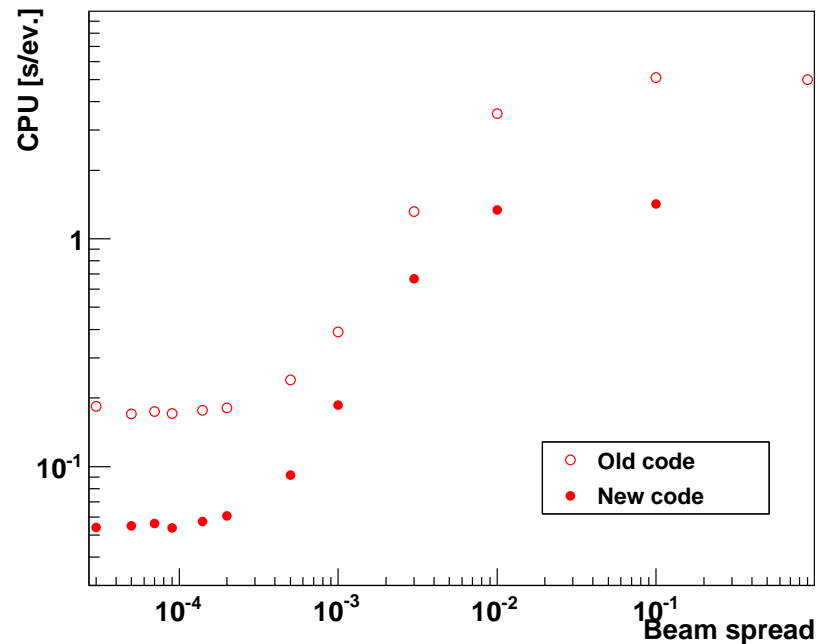
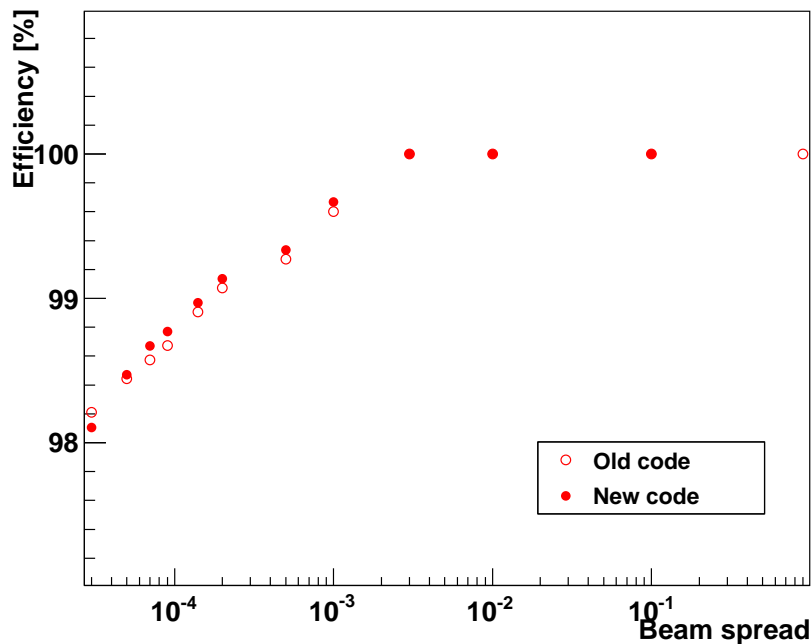
Performance restored  $\Rightarrow$  improvement by factor  $\sim 20$       **Very high efficiency (safe)!**

# New development

## AllowAmbiguousHits

New track selection algorithm logic. One loop over all track possibilities only.

Works in all cases, also when not all planes are hit ( $\text{AllowMissingHits} > 0$ ) and independent on `AllowAmbiguousHits` flag. Improvement by factor  $\langle N_{track} \rangle$





# New development

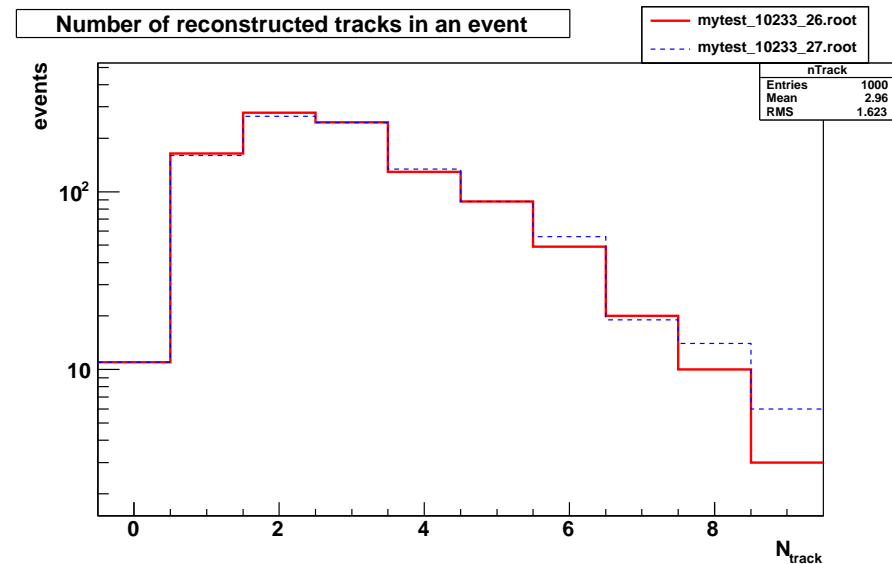
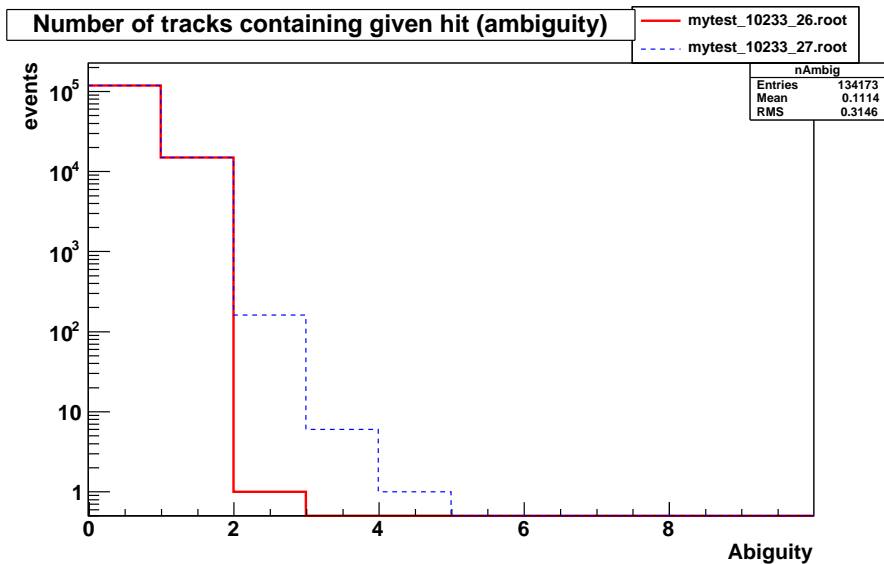
## AllowAmbiguousHits

New option:

**MaximumAmbiguousHits** - maximum number of hits which can be shared by two tracks

For the considered run, **MaximumAmbiguousHits=1** resulted only in 1 extra track in 1000 events (total of 2970 tracks) - **safe**.

Comparison of **MaximumAmbiguousHits=1** and **MaximumAmbiguousHits=2**



For higher **MaximumAmbiguousHits** values “ghost” tracks appear... (2971 → 3052)

# New development

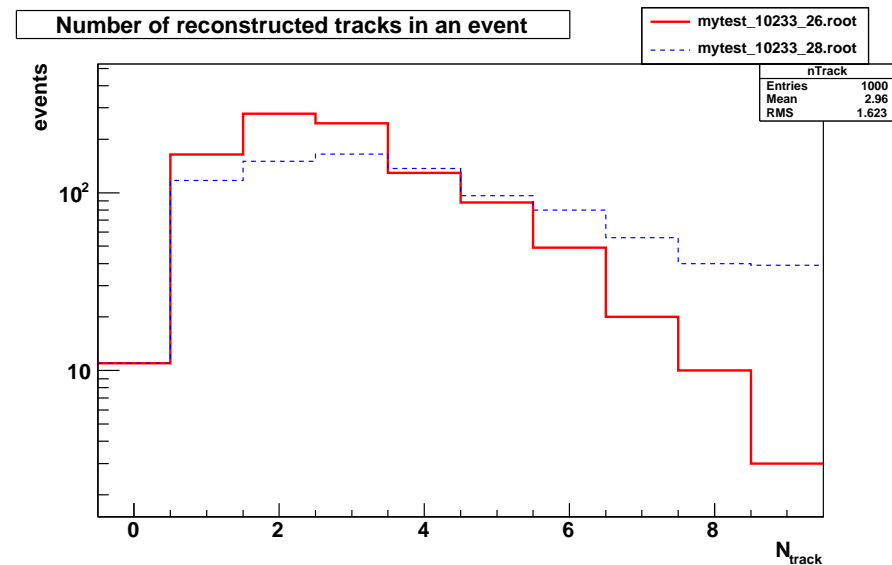
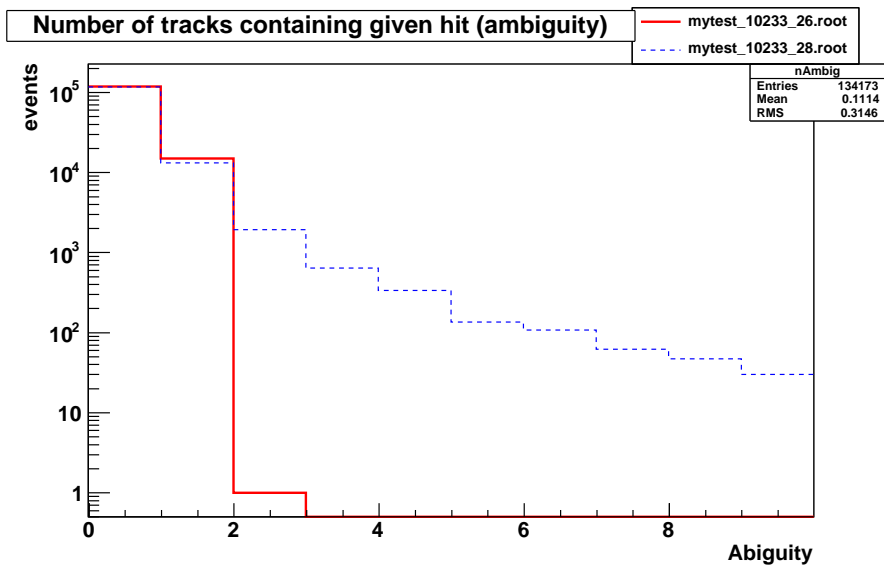
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Comparison of **MaximumAmbiguousHits=1** and **MaximumAmbiguousHits=3**



For higher **MaximumAmbiguousHits** values “ghost” tracks appear... (2971 → 5232)

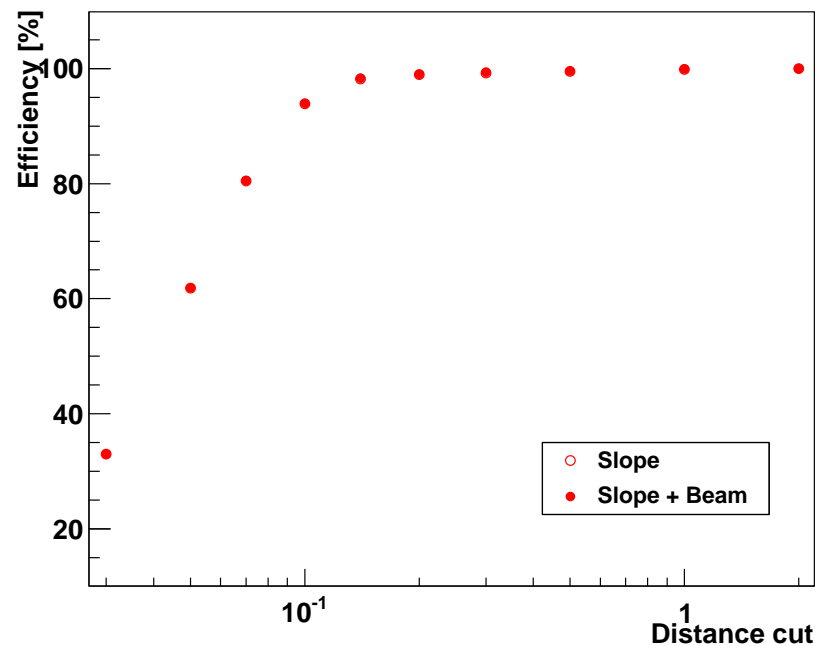
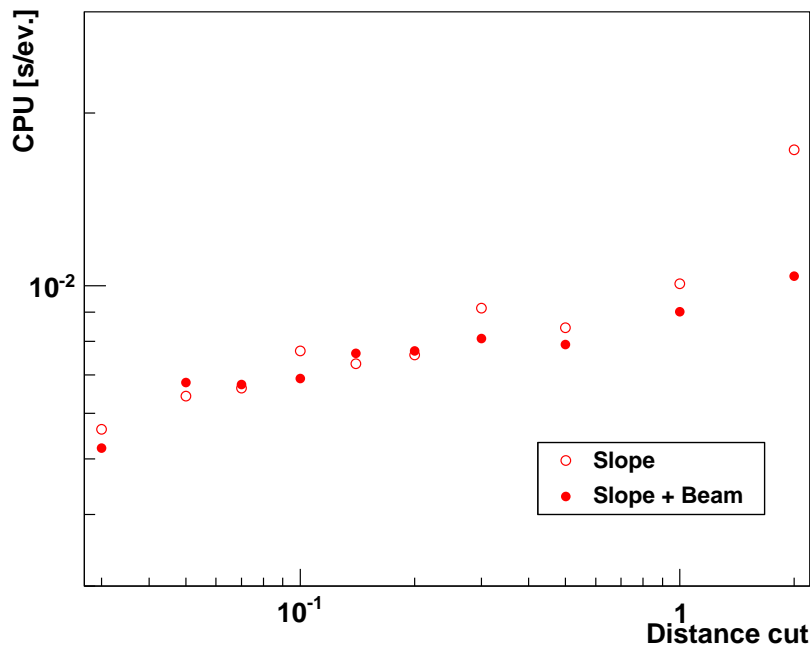
# New development

## UseSlope

Number of considered track possibilities reduced by taking only hits within the assumed distance from the expected track (from the first hit position and the beam direction).

**New version !** Now consistent with the rest of the code.

Works also with **missing hits**. Uses **beam direction** information (**UseBeamConstraint=true**)



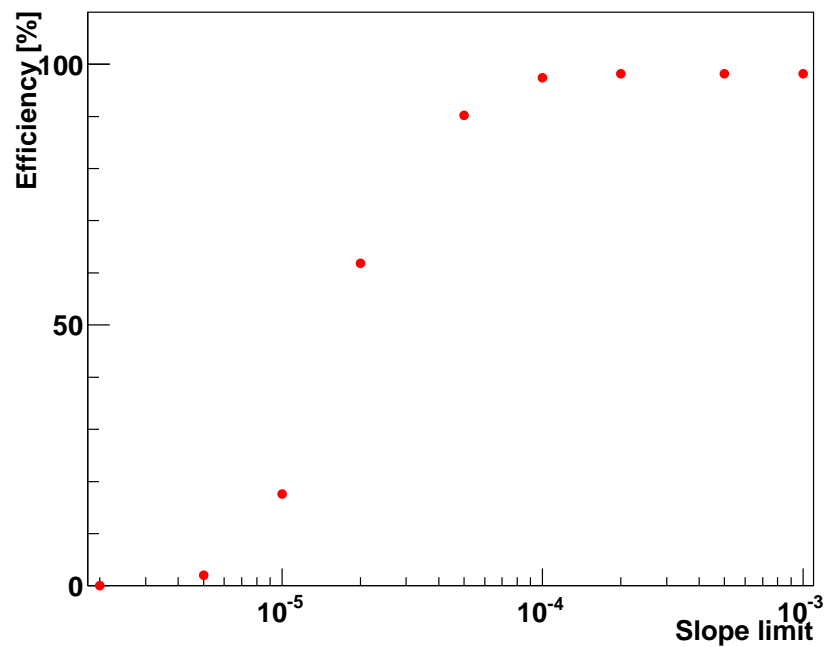
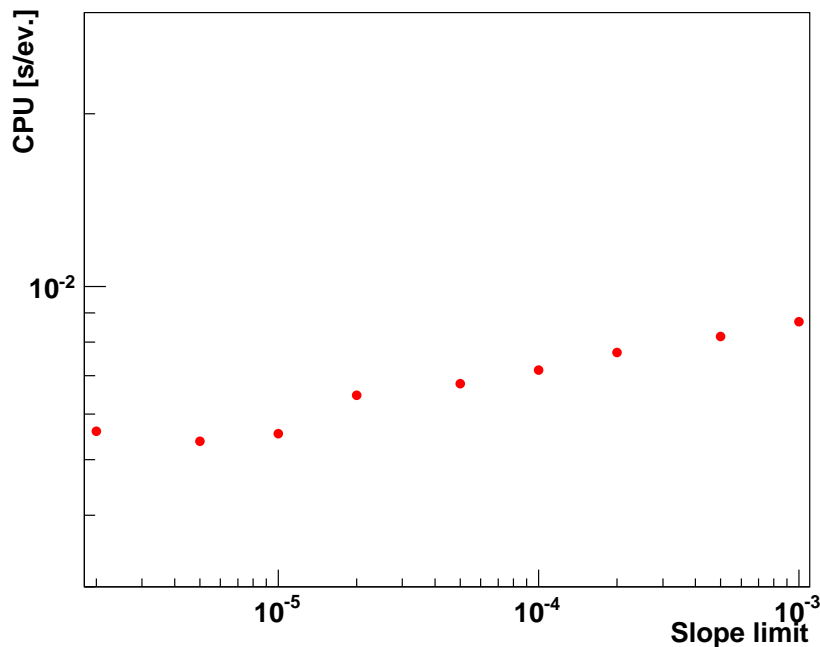
**Be careful: significant efficiency losses if cut too tight!**

## New development

### UseSlope

Number of considered track possibilities can be also reduced by constraining scattering in subsequent planes (ie. slope changes; based on measured hit position).

Should be used with care, especially at low energies!



Significant efficiency losses if cut too tight!

# Summary

Large parts of code rewritten.

Large performance improvemet, especially for tracks with missing hits

Measured CPU time per event (my laptop: 1.6GHz, 2GB RAM)  
(run 10233, 20 hits per plane, 3 tracks per event;  $\chi^2 < 100$ )

setup	full tracks only	AllowSkipHits=2
Old version	0.38	5.0
New version	0.19	1.4
+ UseBeamConstraint	0.01	0.06
+ UseSlope	0.002	0.008

UseSlope should be used with care!      Preselection only!

For well defined measurement  $\chi^2$  cut should decide about track selection.

New options to make it more flexible (beam slope, max. ambiguous hits)